



Searching for Liveness Property Violations in Concurrent Systems with ACO



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Motivation

- Concurrent software is **difficult to test ...**
- ... and it is in the heart of a lot of **critical systems**



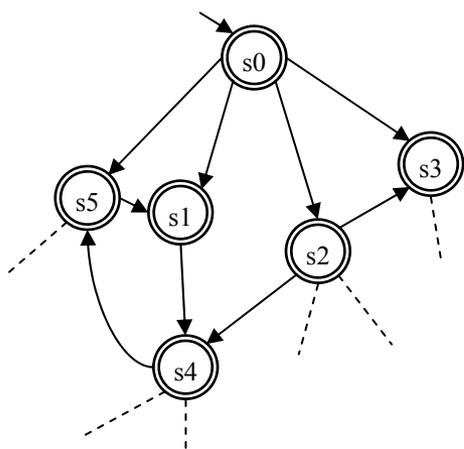
- Techniques for **proving the correctness** of concurrent software are **required**
- **Model checking** → fully automatic
- In the past the work using metaheuristics focused on **safety properties**
- In this work we focus on **liveness properties**



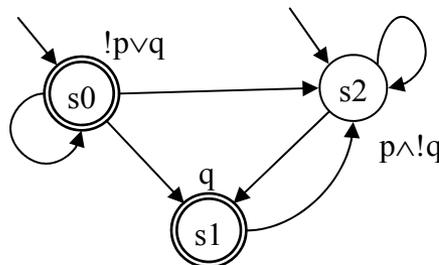
Explicit State Model Checking

- **Objective:** Prove that model M satisfies the property f : $M \models f$
- **HSF-SPIN:** the property f is an **LT**L formula

Model M



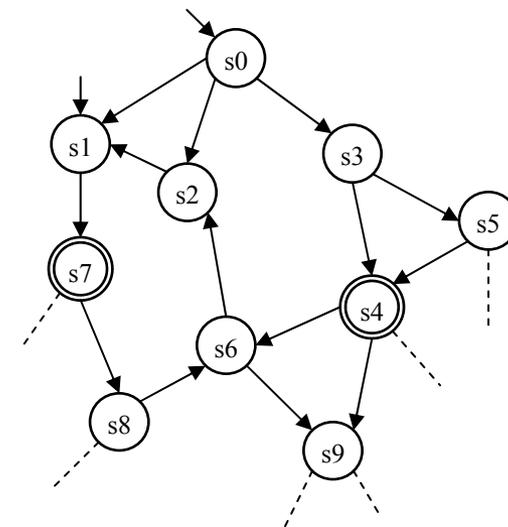
LTL formula $\neg f$
(never claim)



\cap

Intersection Büchi automaton

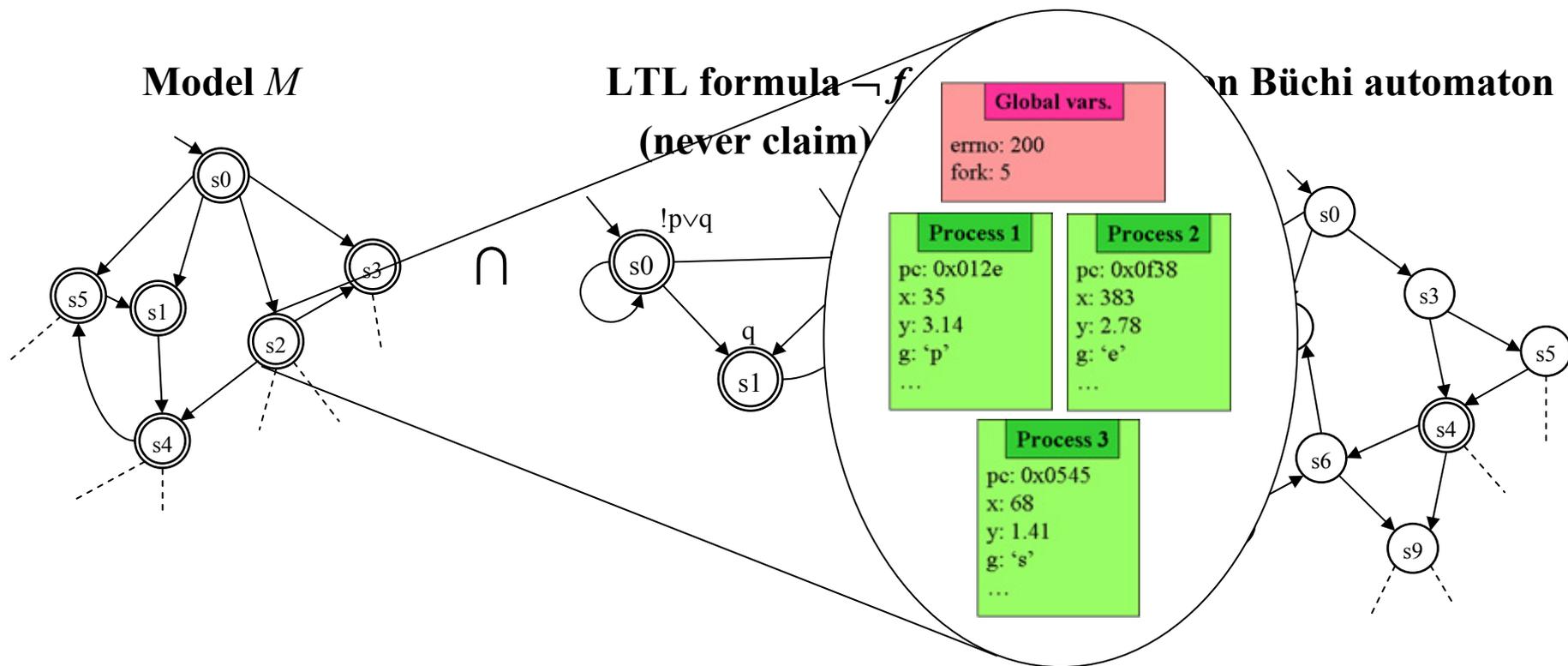
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Explicit State Model Checking

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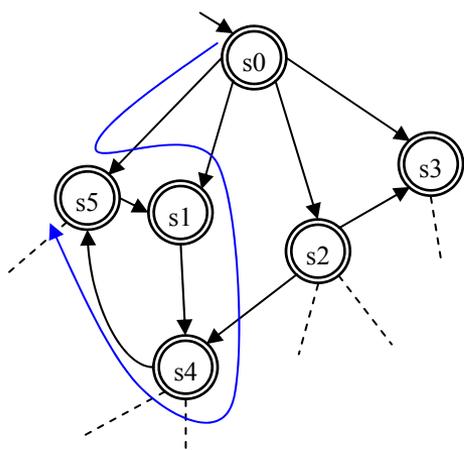




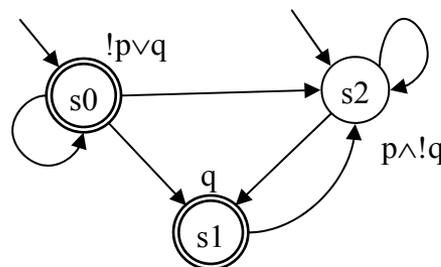
Explicit State Model Checking

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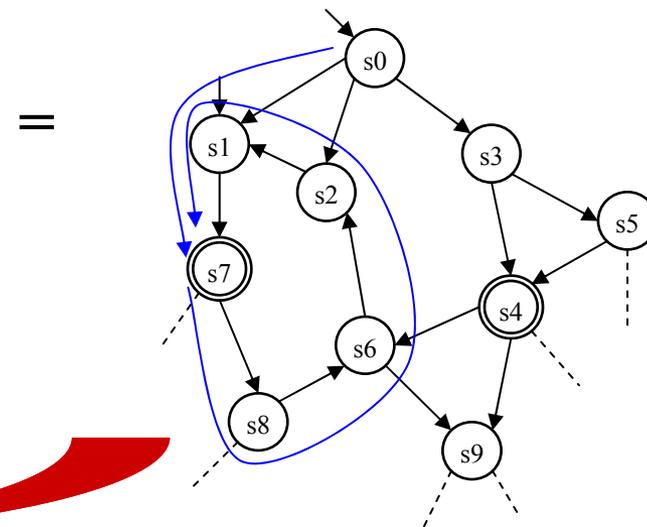
Model M



LTL formula $\neg f$
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Intersection Büchi automaton

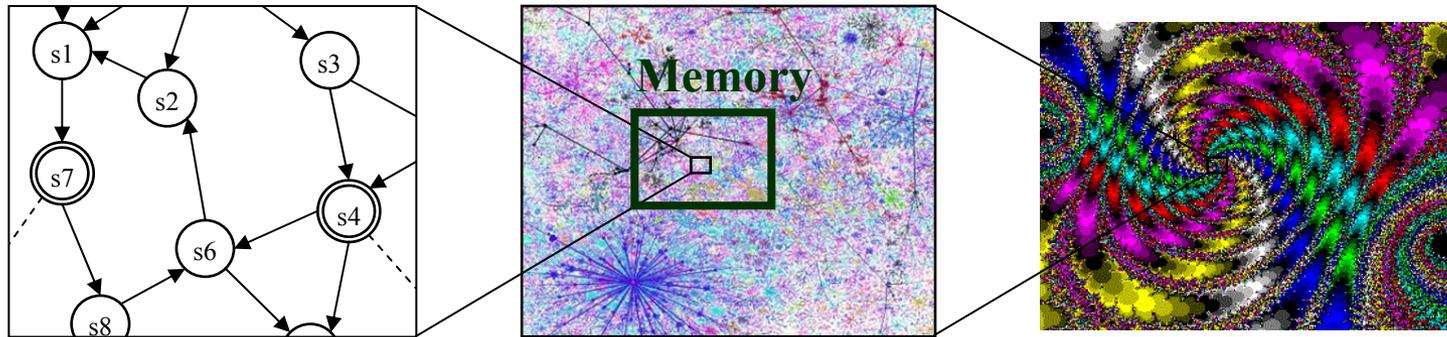


Using Nested-DFS



State Explosion Problem

- Number of states **very large** even for small models

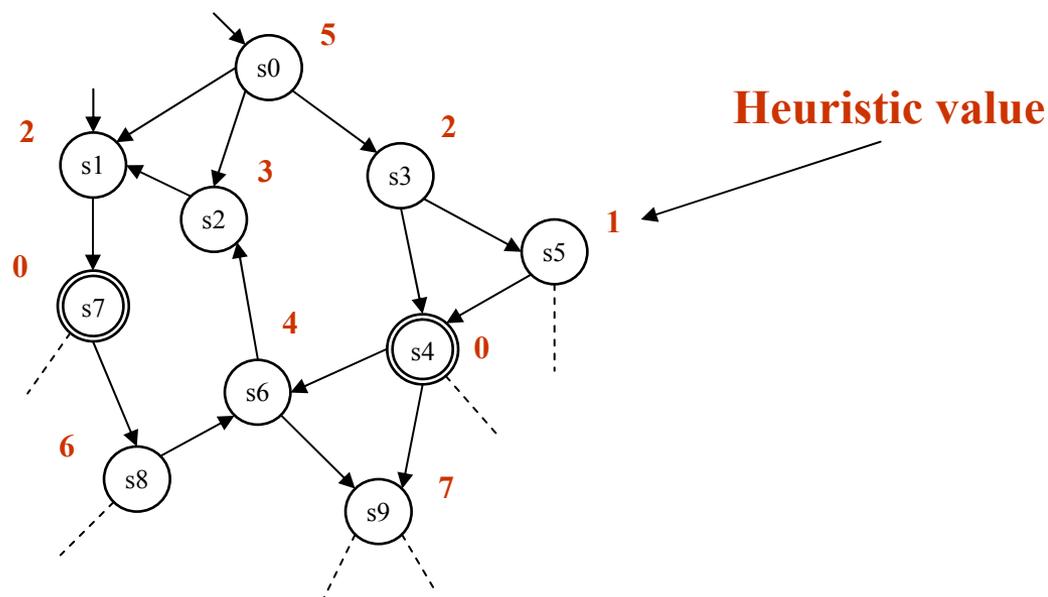


- Example: Dining philosophers with n philosophers $\rightarrow 3^n$ states
20 philosophers \rightarrow **1039 GB** for storing the states
- **Solutions:** collapse compression, minimized automaton representation, bitstate hashing, partial order reduction, symmetry reduction
- Large models cannot be verified but **errors can be found**



Heuristic Model Checking

- The search for errors can be directed by using **heuristic information**



- Different kinds of heuristic functions have been proposed in the past:
 - **Formula-based** heuristics
 - **Structural** heuristics
 - **Deadlock-detection** heuristics
 - **State-dependent** heuristics

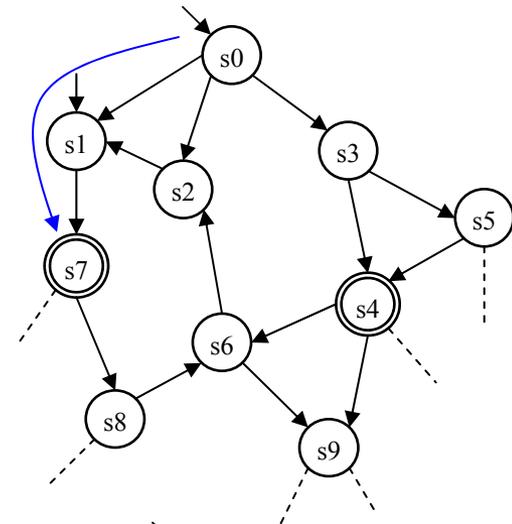


Safety and Liveness Properties

Safety property

$$\forall \sigma \in S^\omega : \sigma \not\models \mathcal{P} \Rightarrow (\exists i \geq 0 : \forall \beta \in S^\omega : \sigma_i \beta \not\models \mathcal{P})$$

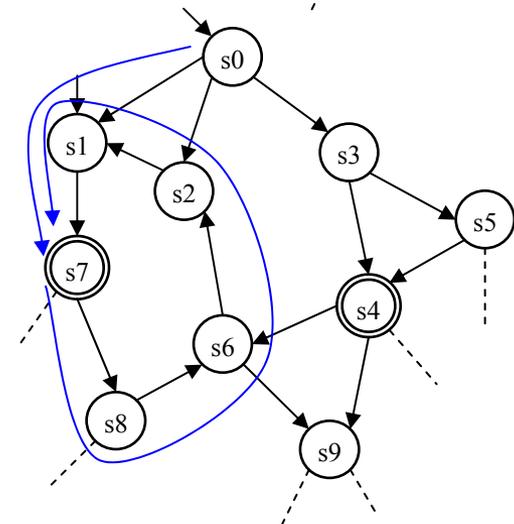
- Counterexample \equiv path to **accepting state**
- Graph exploration algorithms can be used: **DFS** and **BFS**



Liveness property

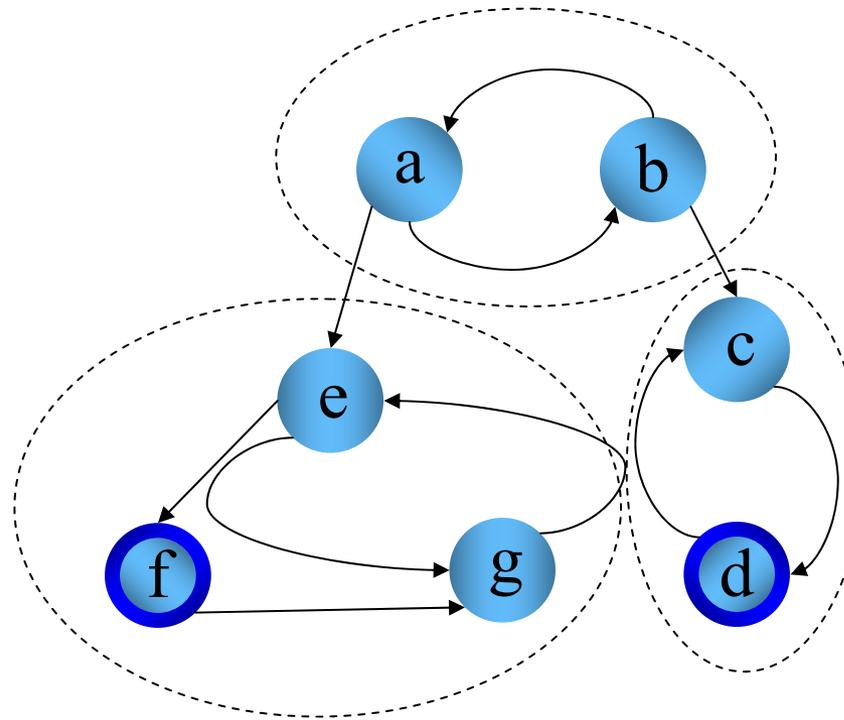
$$\forall \alpha \in S^* : \exists \beta \in S^\omega, \alpha\beta \models \mathcal{P}$$

- Counterexample \equiv path to **accepting cycle**
- It is not possible to apply DFS or BFS



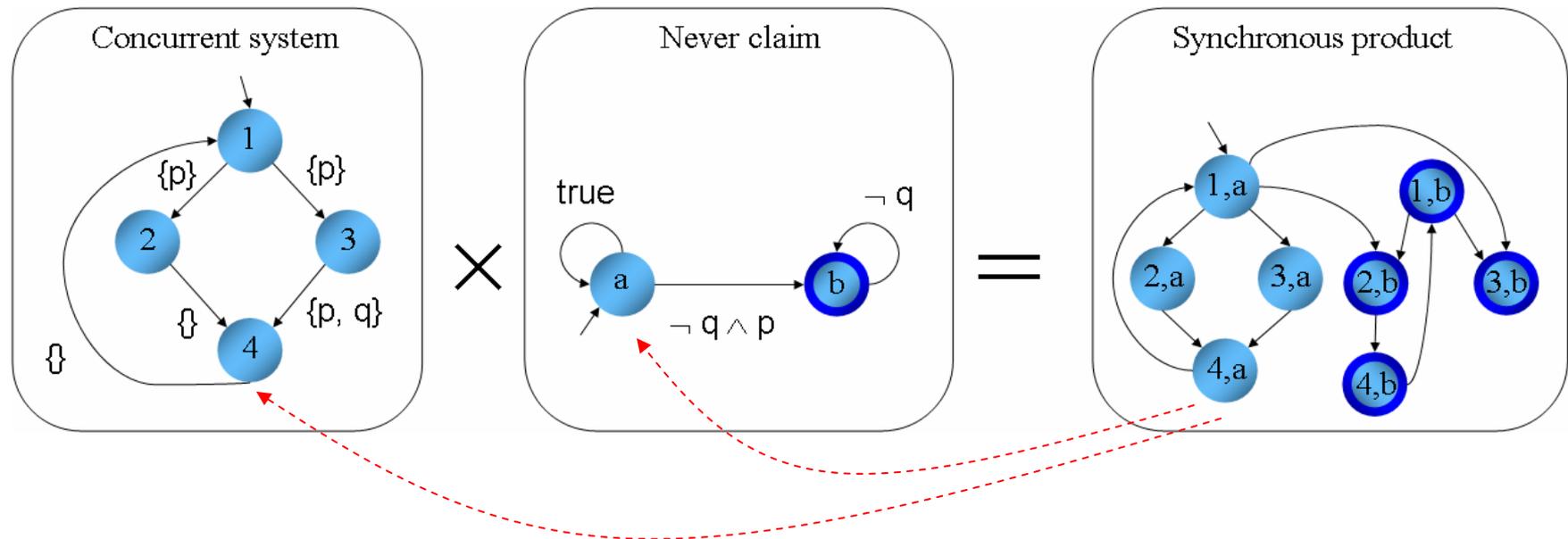


Strongly Connected Components



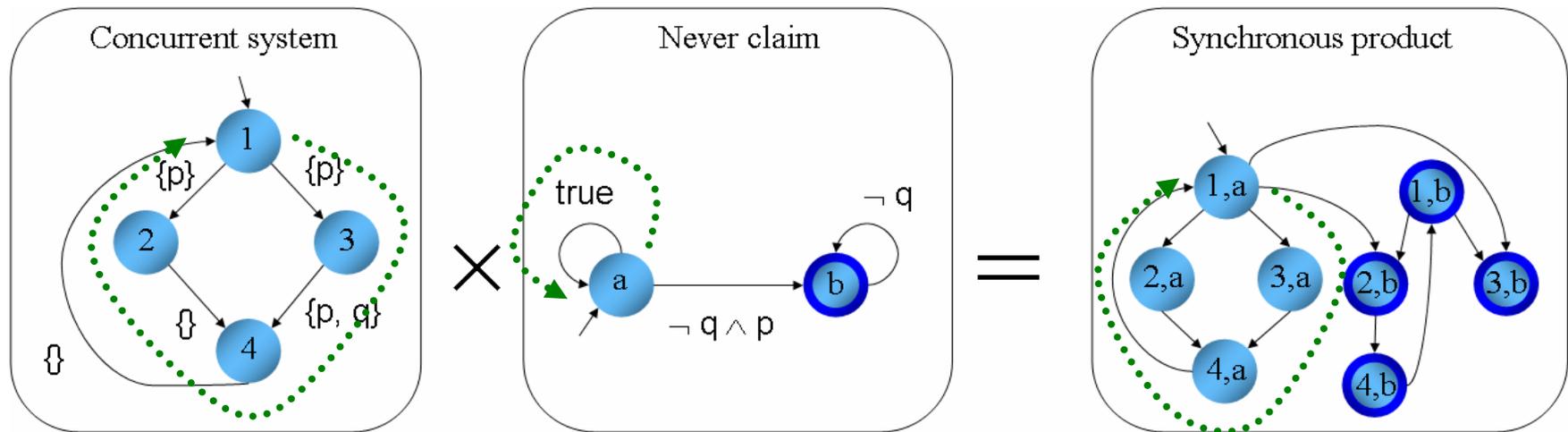


Strongly Connected Components



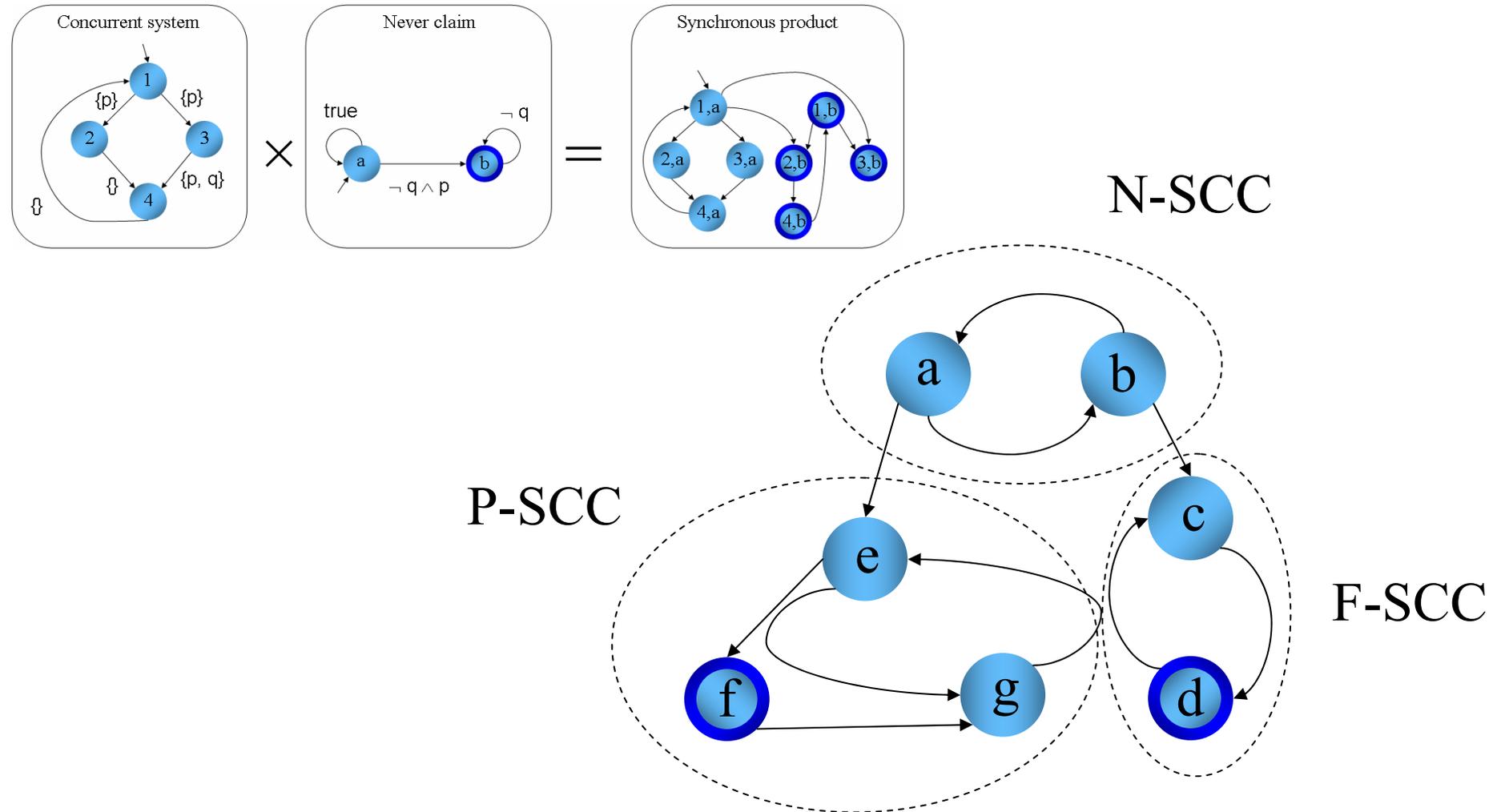


Strongly Connected Components





Strongly Connected Components





Optimization/Search Techniques

OPTIMIZATION/SEARCH TECHNIQUES

EXACT

APPROXIMATED

Ad Hoc Heuristics

METAHEURISTICS

Based on Calculus

- Newton
- Gradient

Enumeratives

- Depth First Search
- Branch and Bound

Trajectory-based

- SA
- VNS
- TS

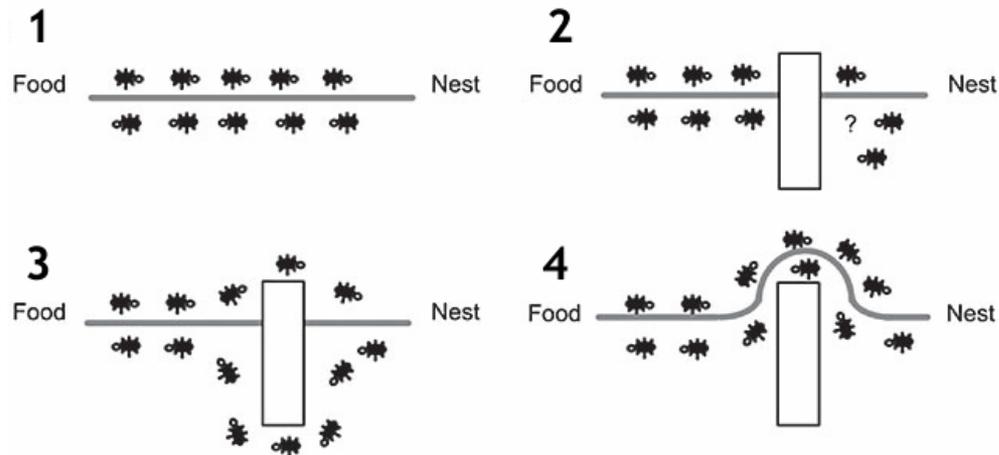
Population-based

- EA
- ACO
- PSO



ACO: Introduction

- **Ant Colony Optimization (ACO)** metaheuristic is inspired by the foraging behaviour of real ants



- **ACO Pseudo-code**

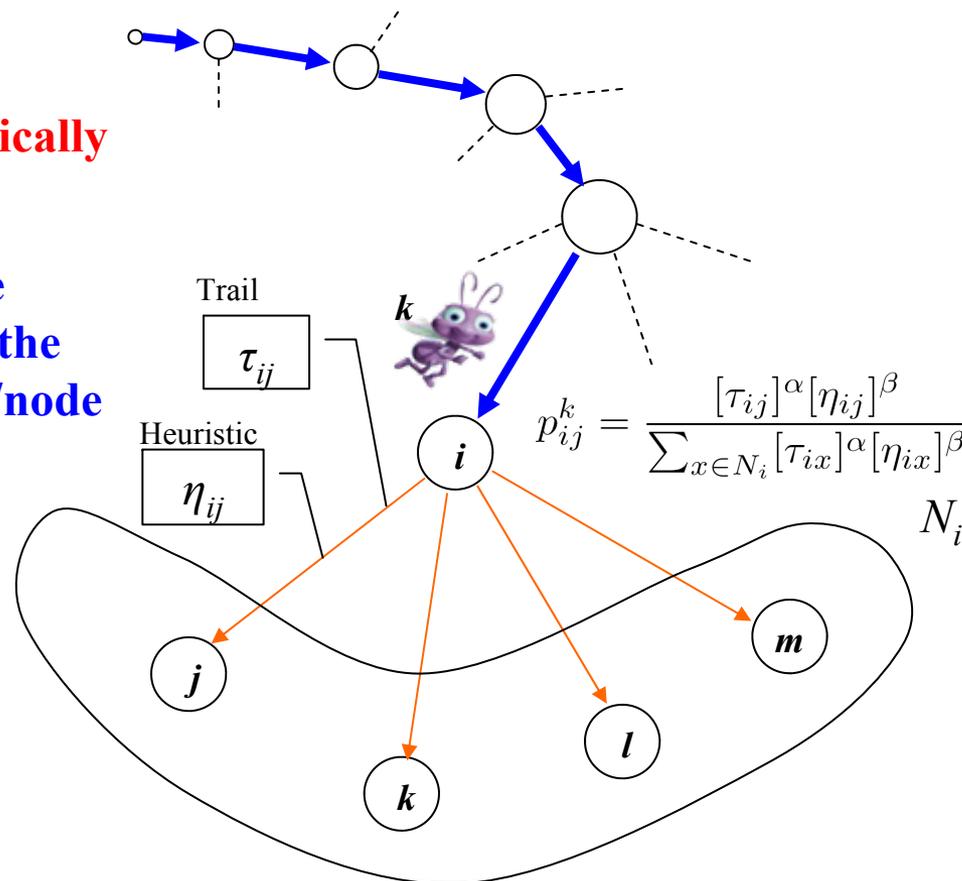
```

procedure ACOMetaheuristic
  ScheduleActivities
    ConstructAntsSolutions
    UpdatePheromones
    DaemonActions // optional
  end ScheduleActivities
end procedure
  
```



ACO: Construction Phase

- The ant selects its next node **stochastically**
- The probability of selecting one node depends on the **pheromone trail** and the **heuristic value** (optional) of the edge/node
- The ant stops when a complete solution is built





ACO: Pheromone Update

- **Pheromone update**

- **During the construction phase**

$$\tau_{ij} \leftarrow (1 - \xi)\tau_{ij} \quad \text{with} \quad 0 \leq \xi \leq 1$$

- **After the construction phase**

$$\tau_{ij} \leftarrow (1 - \rho)\tau_{ij} + \Delta\tau_{ij}^{bs} \quad \text{with} \quad 0 \leq \rho \leq 1$$

- **Trail limits (particular of MMAS)**

- **Pheromones are kept in the interval $[\tau_{\min}, \tau_{\max}]$**

$$\tau_{max} = \frac{Q}{\rho}$$

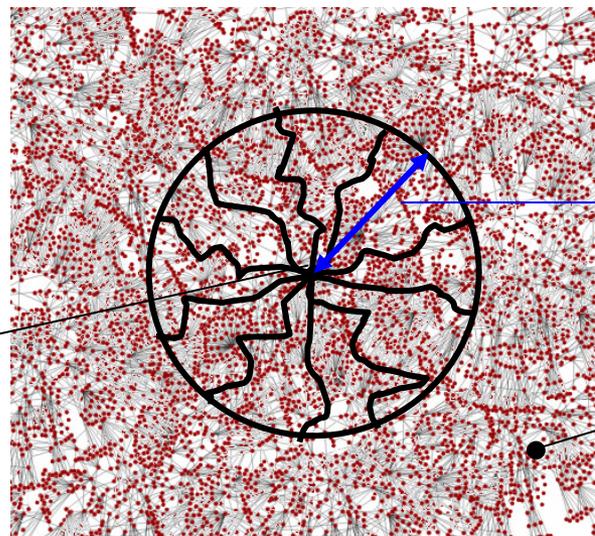
$$\tau_{min} = \frac{\tau_{max}}{a}$$



ACOhg: Huge Graphs Exploration

The length of the ant paths is limited by λ_{ant}

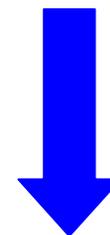
Initial node



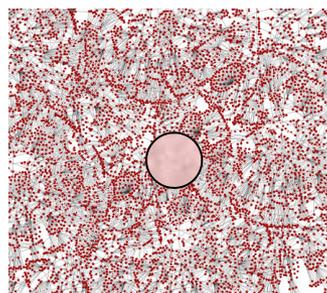
λ_{ant}

What if...?

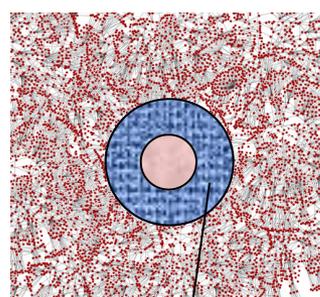
Objective node



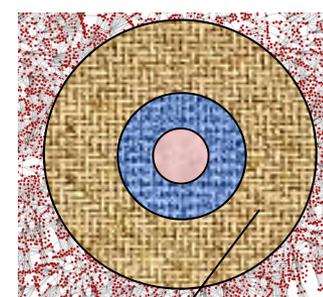
Starting nodes for path construction change



After σ_s steps



Second stage



Third stage



ACOhg-live

- The search is an alternation of two phases

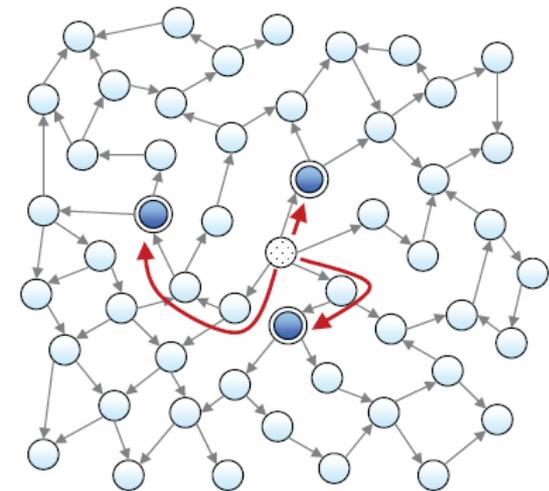
- **First phase:** search for accepting states
- **Second phase:** search for cycles from the accepting states

ACOhg-live Pseudocode

```

1: repeat
2:   accept = acohg1.findAcceptingStates(); {First phase}
3:   for node in accept do
4:     acohg2.findCycle(node); {Second phase}
5:     if acohg2.cycleFound() then
6:       return acohg2.acceptingPath();
7:     end if
8:   end for
9:   acohg1.insertTabu(accept);
10: until empty(accept)
11: return null;

```



First phase

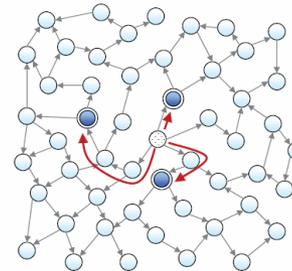


ACOhg-live

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- **First phase:** search for accepting states

- **Second phase:** search for cycles from the accepting states

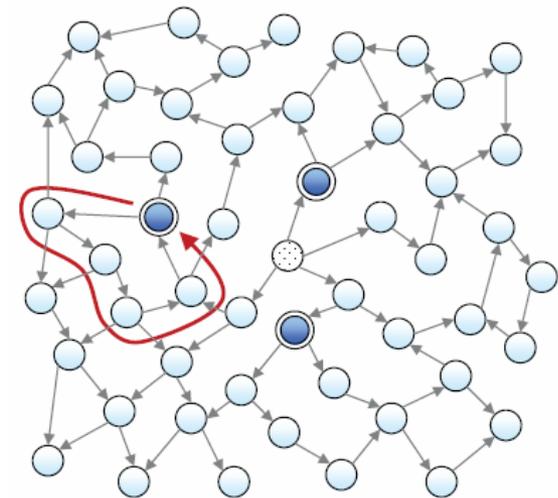


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Second phase

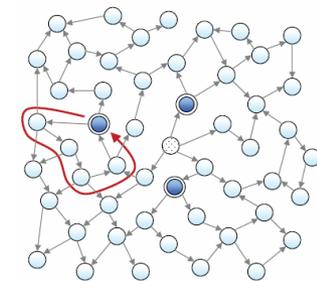
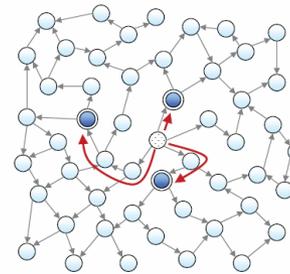


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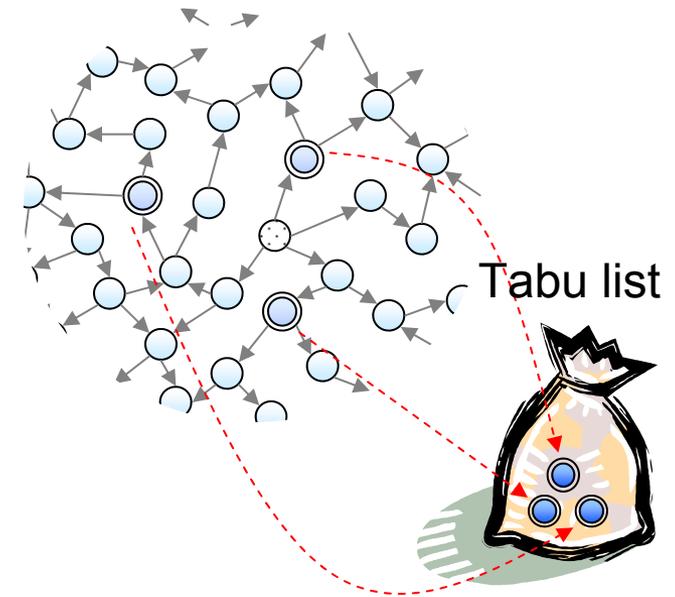


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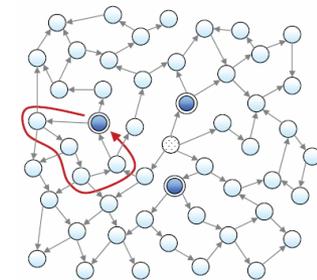
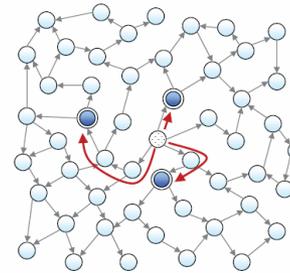


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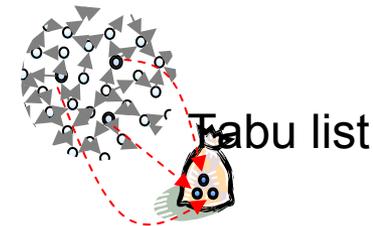
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- Improvement using SCCs



- **First phase:** accepting states in N-SCC are ignored

- **Both phases:** cycle detected in F-SCC is a violation



Promela Models

- We used **11 Promela models** for the experiments

Model	LoC	Scalable	Processes	LTL formula (liveness)
<code>alter</code>	64	no	2	$\Box(p \rightarrow \Diamond q) \wedge \Box(r \rightarrow \Diamond s)$
<code>giopj</code>	740	yes	$j+6$	$\Box(p \rightarrow \Diamond q)$
<code>phi j</code>	57	yes	$j+1$	$\Box(p \rightarrow \Diamond q)$
<code>elev j</code>	191	yes	$j+3$	$\Box(p \rightarrow \Diamond q)$
<code>sgc</code>	1001	no	20	$\Diamond p$

- Parameters for **ACOhg-live**

Parameter	<i>msteps</i>	<i>colsize</i>	λ_{ant}	σ_s	ξ	<i>a</i>	ρ	α	β
1st phase	100	10	20	4	0.7	5	0.2	1.0	2.0
2nd phase		20	4		0.5				

- **Formula-based and finite state machine heuristics**
- **ACOhg-live implemented in HSF-SPIN**
- **100 independent executions and statistical validation**



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phi j	57	j=20,30,40	j+1	$\square(p \rightarrow \diamond q)$
elevj	191	yes	j+3	$\square(p \rightarrow \diamond q)$
sgc	1001	j=10,15,20	20	$\diamond p$

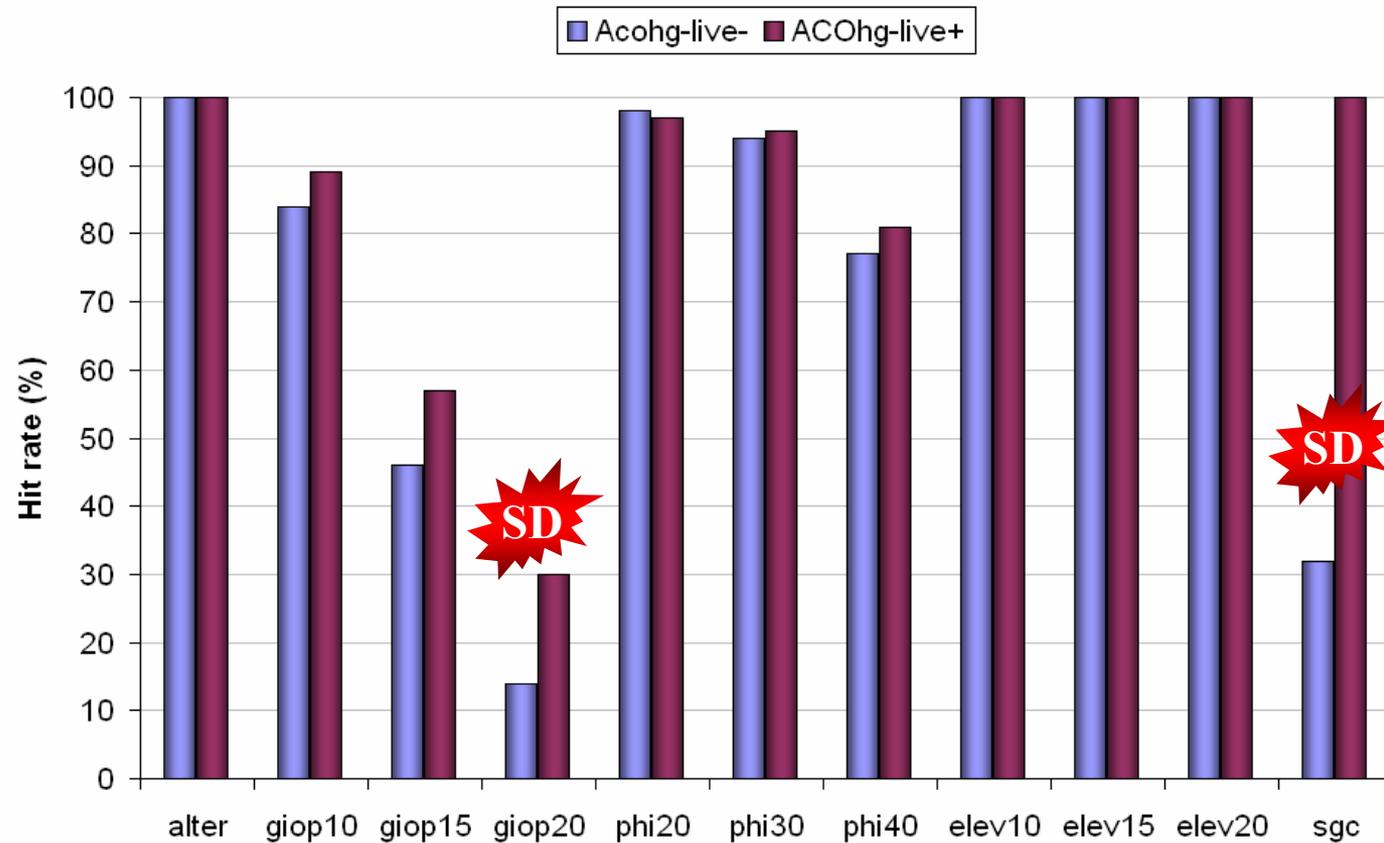
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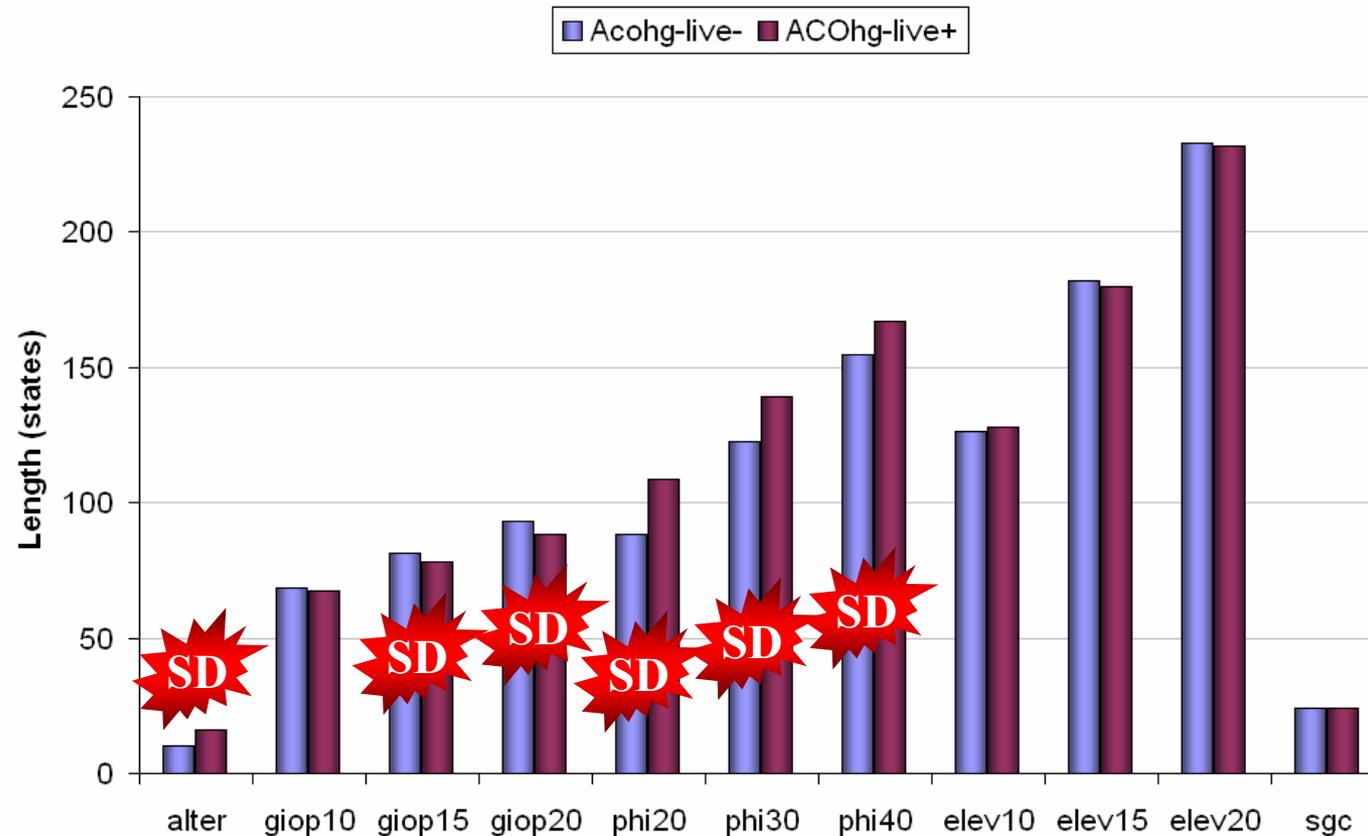


Results I: Influence of the SCC Improvement



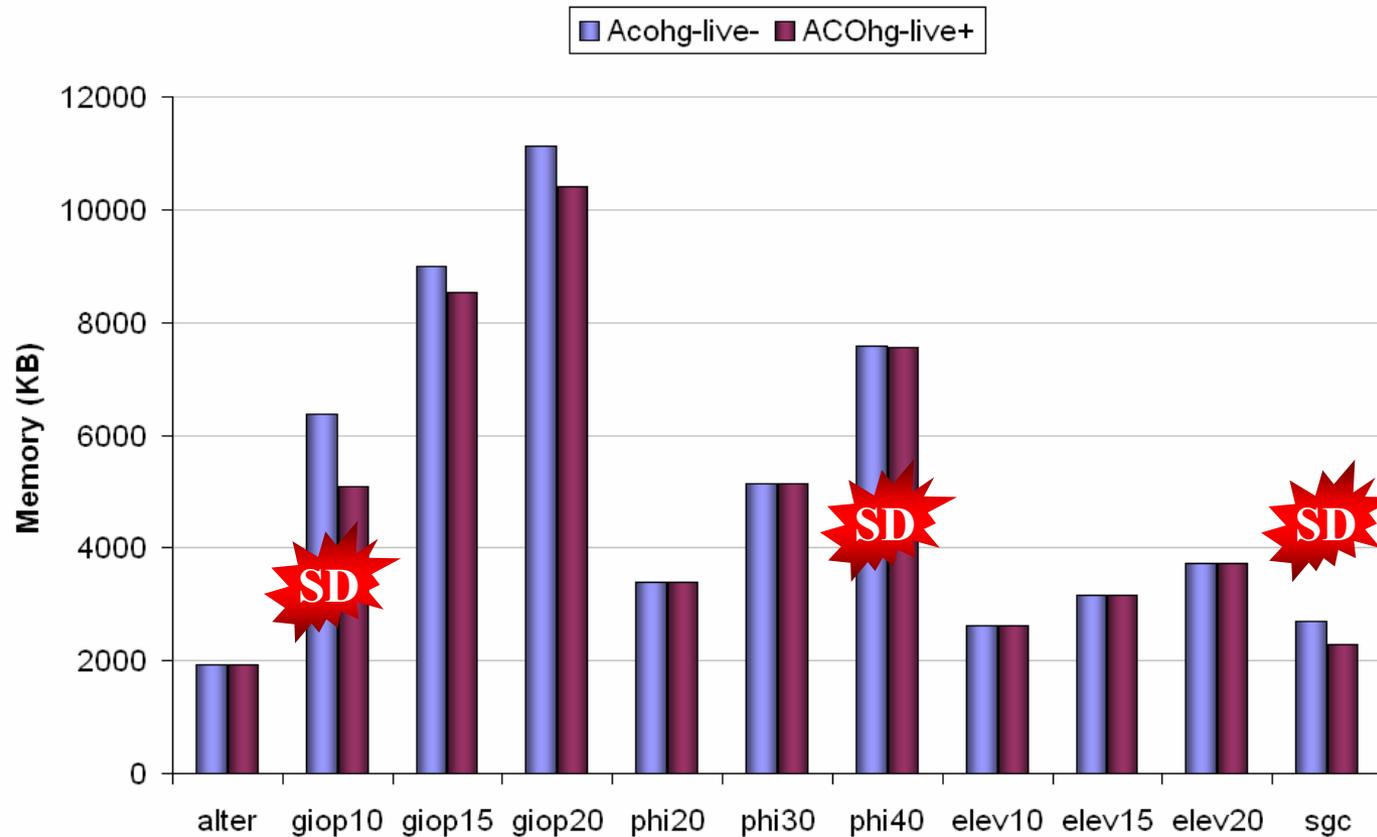


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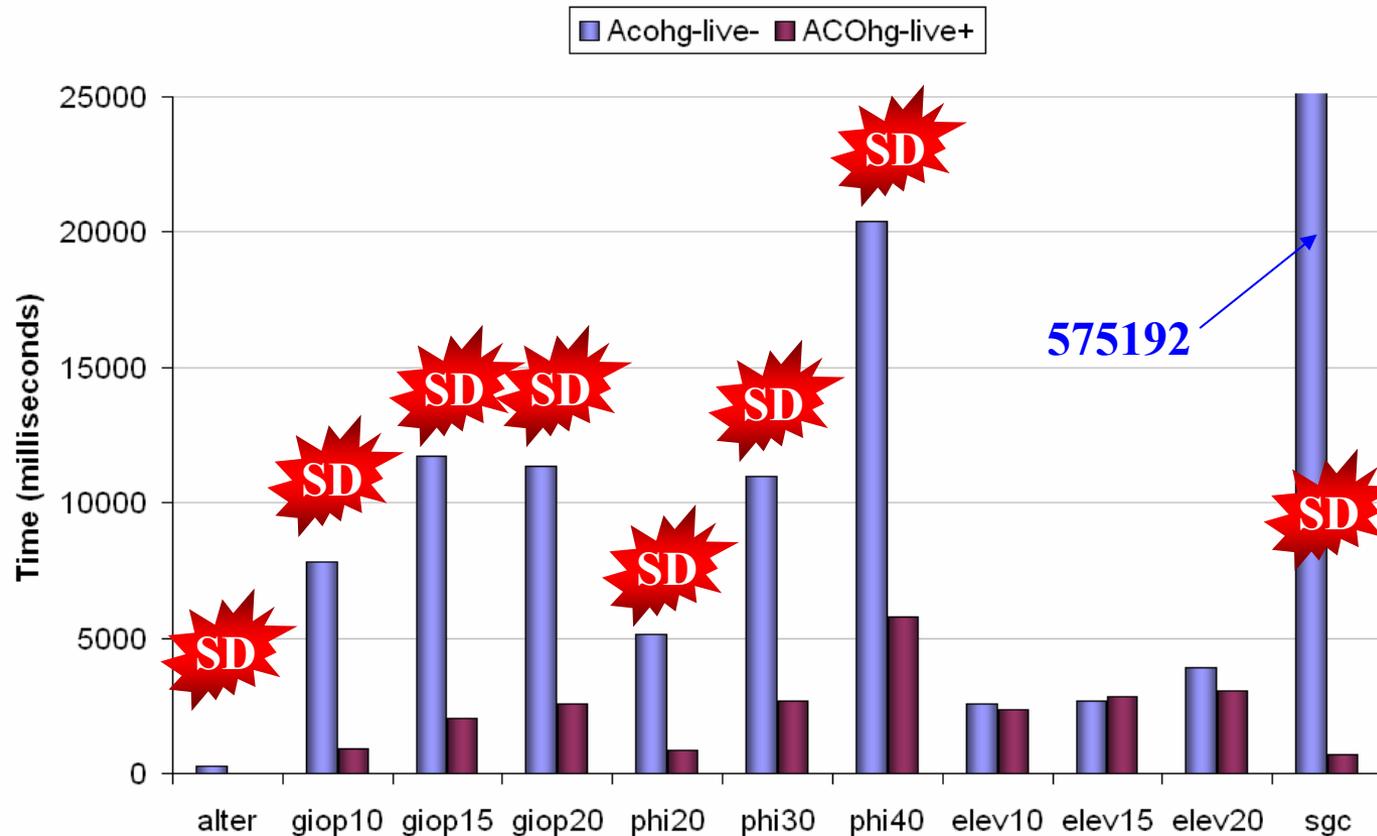


Results I: Influence of the SCC Improvement





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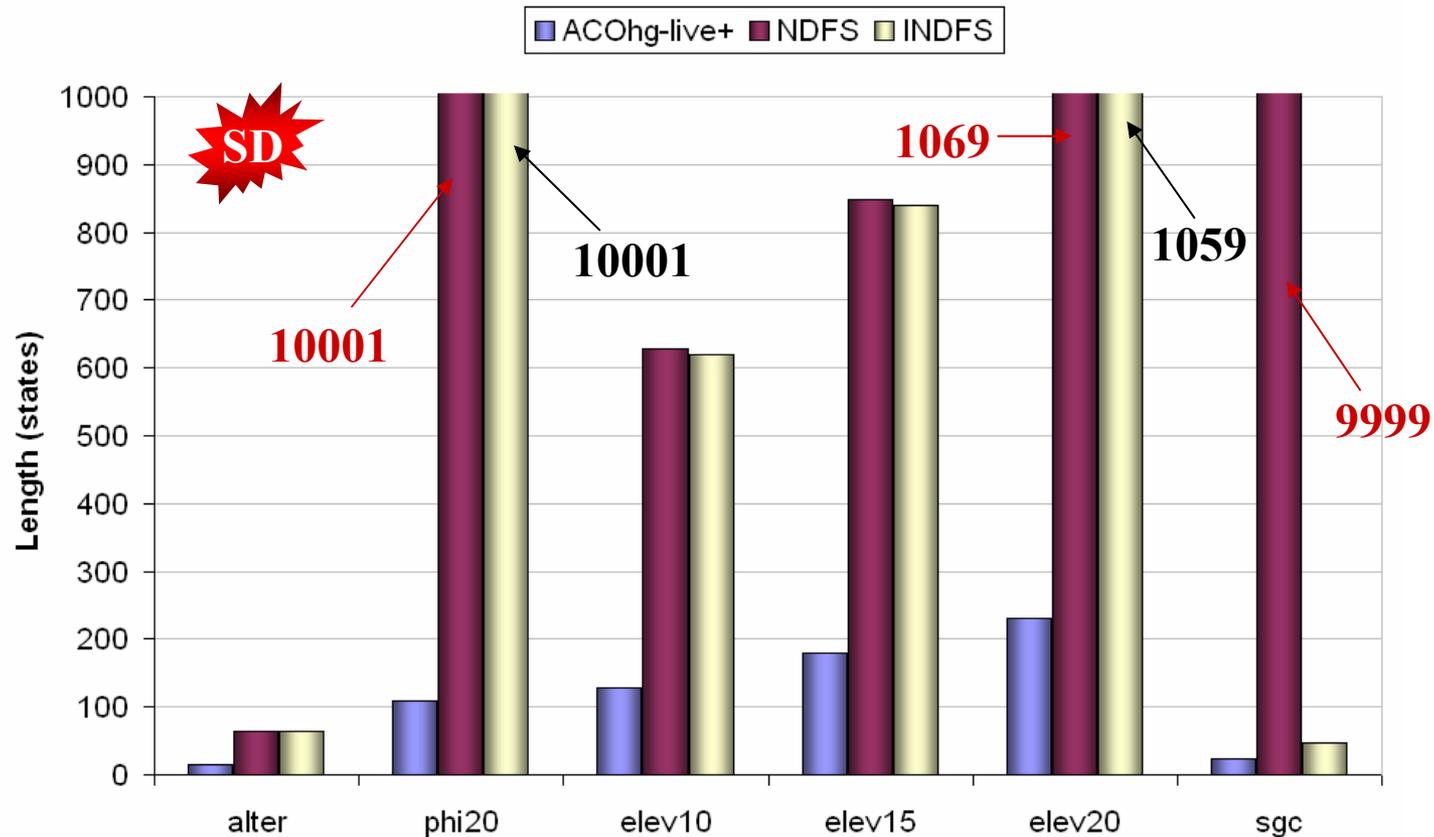


Results II: ACOhg-live⁺ vs. NDFS and INDFS

Models	ACOhg-live ⁺	NDFS	INDFS
alter	●	●	●
giop10	●	✗	✗
giop15	●	✗	✗
giop20	●	✗	✗
phi20	●	●	●
phi30	●	✗	✗
phi40	●	✗	✗
elev10	●	●	●
elev15	●	●	●
elev20	●	●	●
sgc	●	●	●

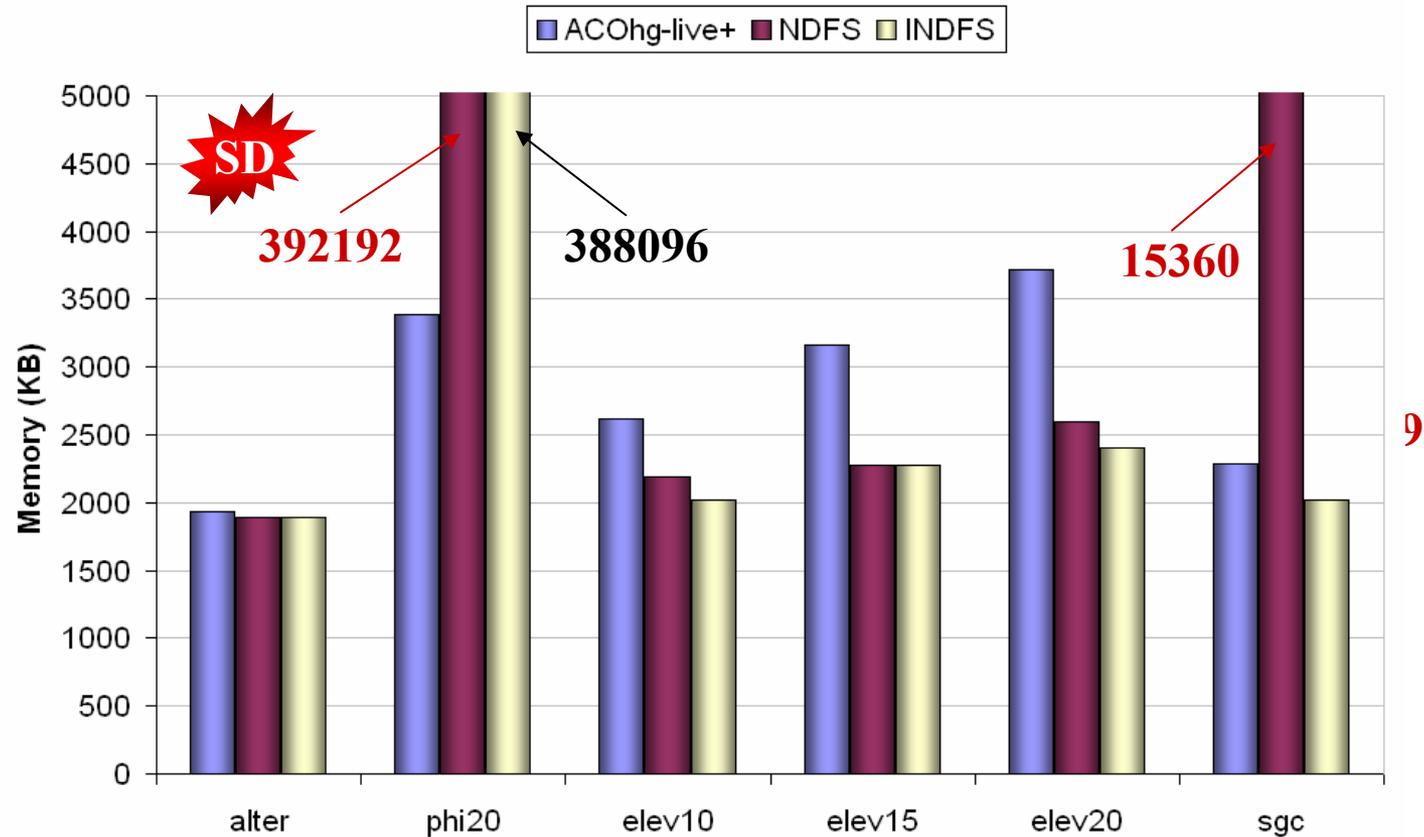


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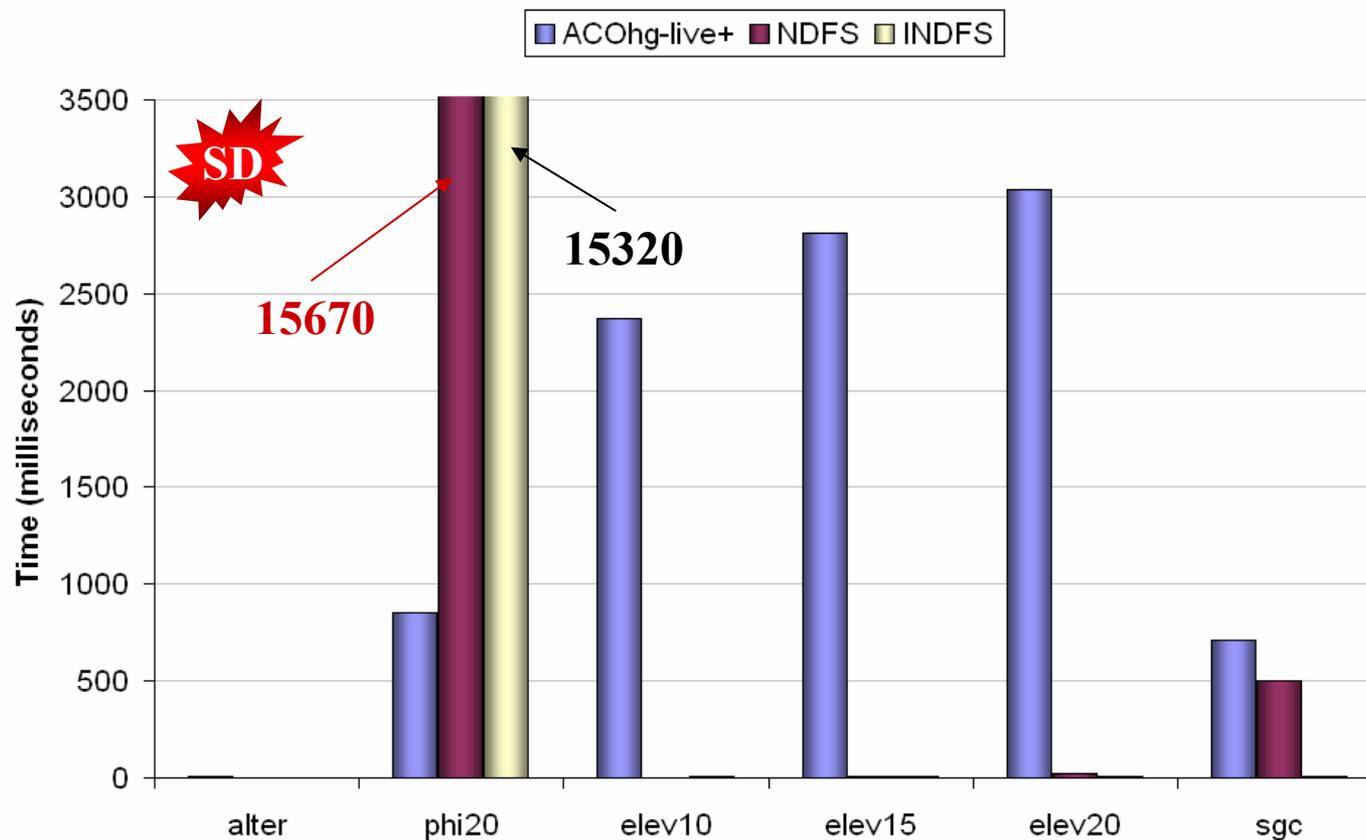


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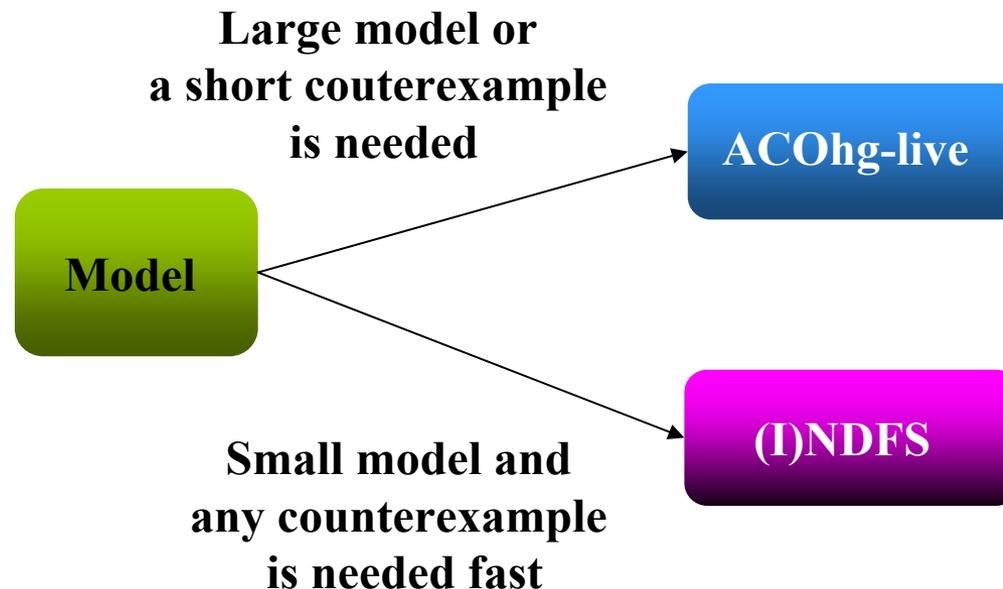
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How to use ACOhg-live

- ACOhg-live should be used in the **first/middle stages** of the software development, when software errors are expected
- ACOhg-live can also be used in other phases of the software development for **testing** concurrent software





Conclusions & Future Work

Conclusions

- ACOhg-live is the **first algorithm** based on metaheuristics (to the best of our knowledge) applied to the search for liveness errors in concurrent models
- The improvement based on the SCCs of the never claim **outperforms** the efficacy of ACOhg-live
- ACOhg-live is able to **outperform (Improved) Nested-DFS** in efficacy and efficiency in the search for liveness errors

Future Work

- Analysis of parameterization for **reducing the parameters**
- Include ACOhg-live into **JavaPathFinder** for finding liveness errors in Java programs
- Combine ACOhg-live with techniques for **reducing the memory** required for the search such as **partial order reduction** (work in progress)

Searching for Liveness Property Violations in Concurrent Systems with ACO



Thanks for your attention !!!

