

# *Finding Liveness Errors with ACO*



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# Motivation

- Nowadays **software is very complex**
- An error in a software system can imply the **loss of lot of money ...**



... and even **human lives**

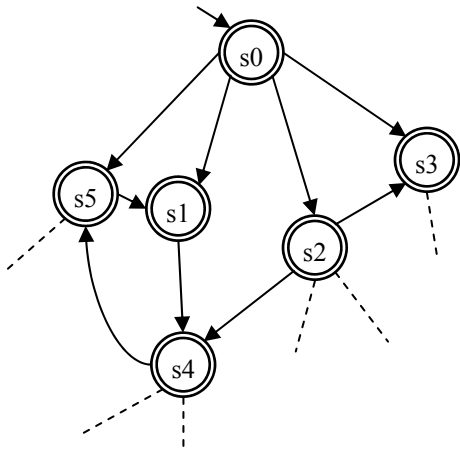
- Techniques for **proving the correctness of the software are required**
- **Model checking** → fully automatic



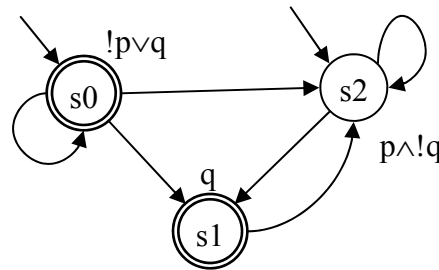
# Explicit State Model Checking

- **Objective:** Prove that model  $M$  satisfies the property  $f: M \models f$
- **HSF-SPIN:** the property  $f$  is an **LTL formula**

Model  $M$

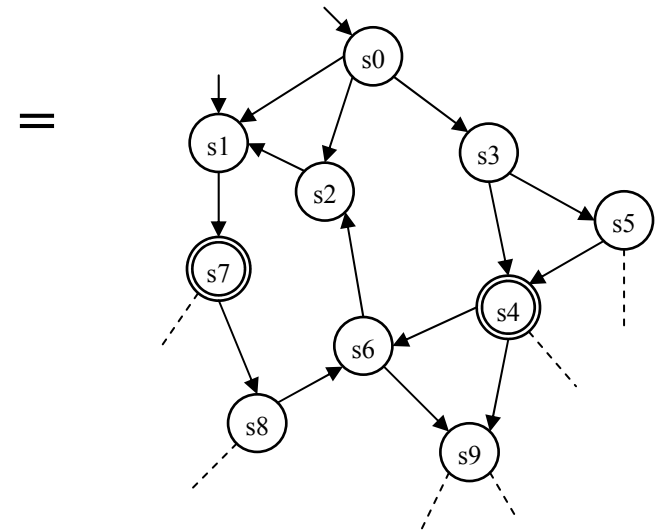


LTL formula  $\neg f$



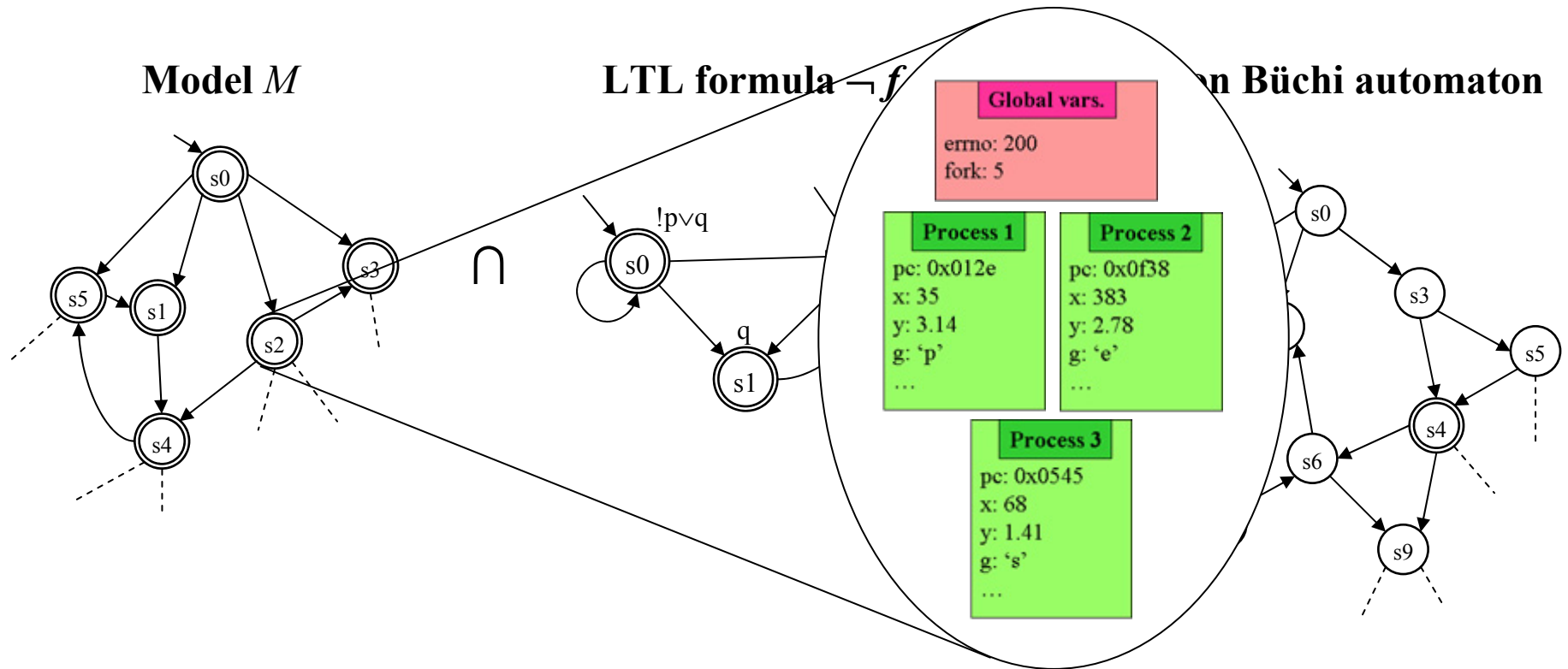
$\cap$

Intersection Büchi automaton



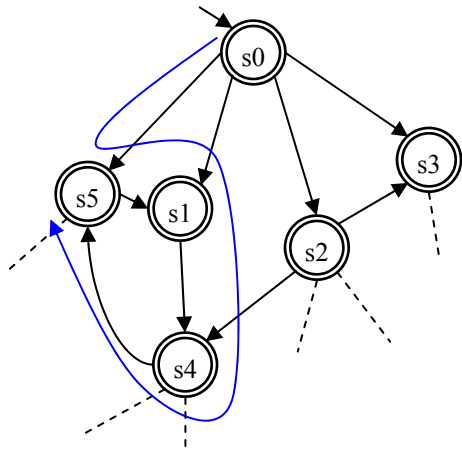
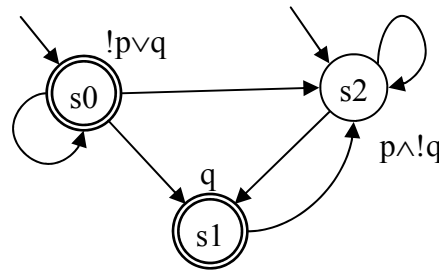
# Explicit State Model Checking

- **Objective:** Prove that model  $M$  satisfies the property  $f: M \models f$
- **HSF-SPIN:** the property  $f$  is an **LTl** formula

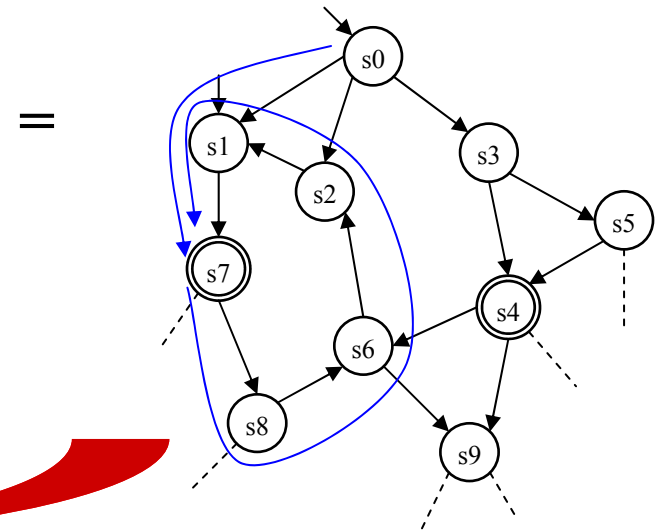


# Explicit State Model Checking

- **Objective:** Prove that model  $M$  satisfies the property  $f: M \models f$
- **HSF-SPIN:** the property  $f$  is an **LTL formula**

Model  $M$ LTL formula  $\neg f$ 

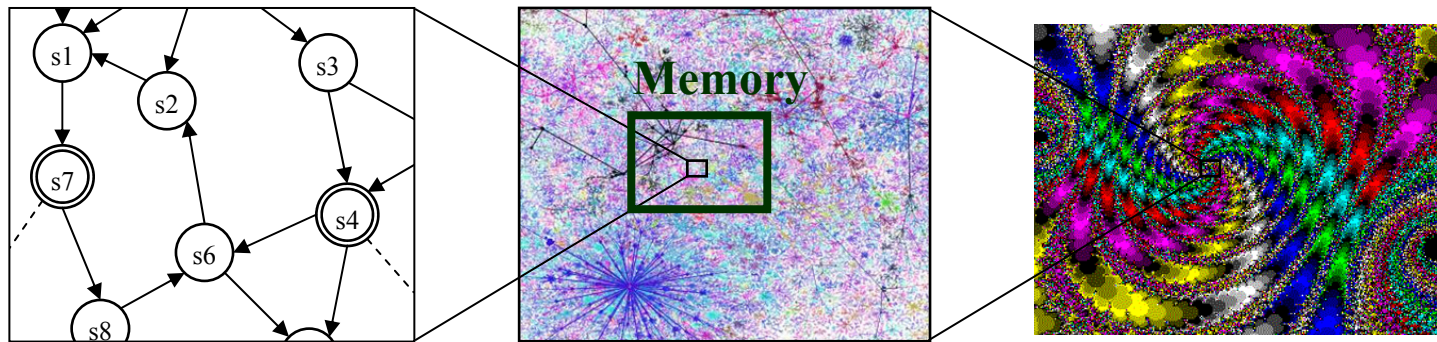
Intersection Büchi automaton



Using Nested-DFS

# State Explosion Problem

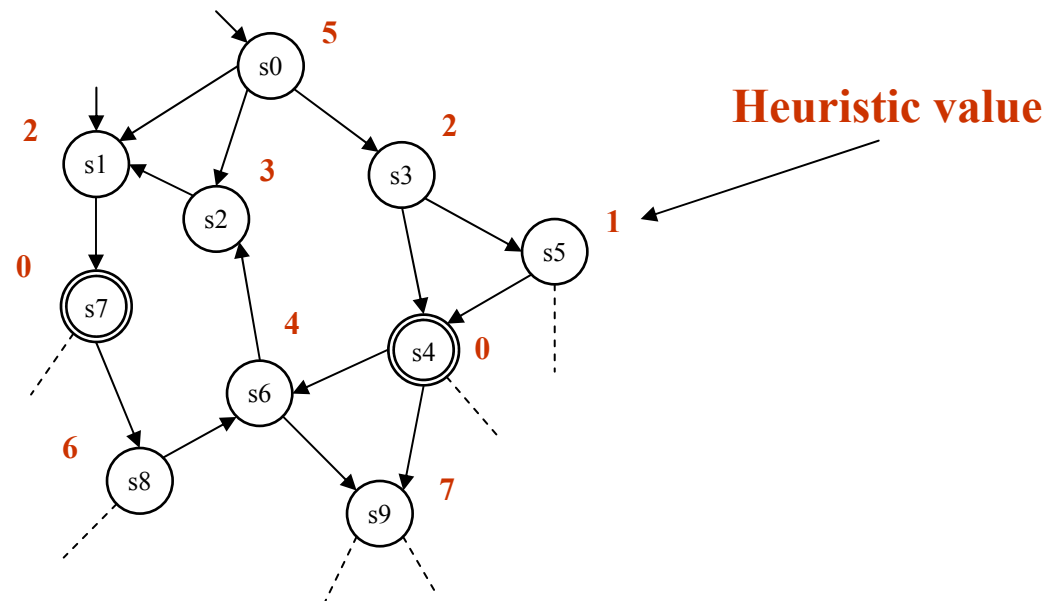
- Number of states **very large** even for small models



- Example: Dining philosophers with  $n$  philosophers  $\rightarrow 3^n$  states  
20 philosophers  $\rightarrow$  **1039 GB** for storing the states
- **Solutions:** collapse compression, minimized automaton representation, bitstate hashing, partial order reduction, symmetry reduction
- Large models cannot be verified but **errors can be found**

# Heuristic Model Checking

- The search for errors can be directed by using **heuristic information**



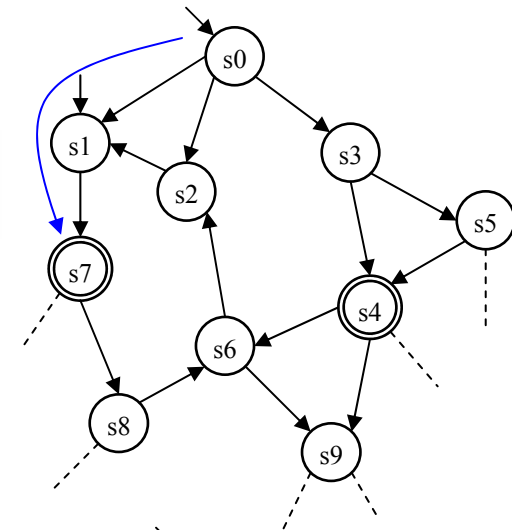
- Different kinds of heuristic functions have been proposed in the past:
  - Formula-based** heuristics
  - Structural** heuristics
  - Deadlock-detection** heuristics
  - State-dependent** heuristics

# Safety and Liveness Properties

## Safety property

$$\forall \sigma \in S^\omega : \sigma \not\vdash \mathcal{P} \Rightarrow (\exists i \geq 0 : \forall \beta \in S^\omega : \sigma_i \beta \not\vdash \mathcal{P})$$

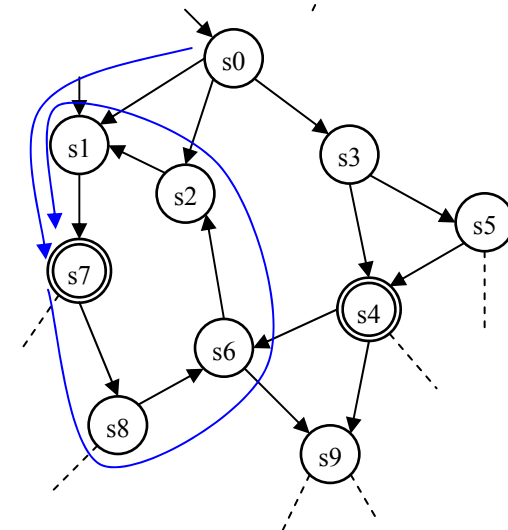
- Counterexample  $\equiv$  path to **accepting state**
- Graph exploration algorithms can be used: **DFS** and **BFS**



## Liveness property

$$\forall \alpha \in S^* : \exists \beta \in S^\omega, \alpha\beta \vdash \mathcal{P}$$

- Counterexample  $\equiv$  path to **accepting cycle**
- It is not possible to apply DFS or BFS



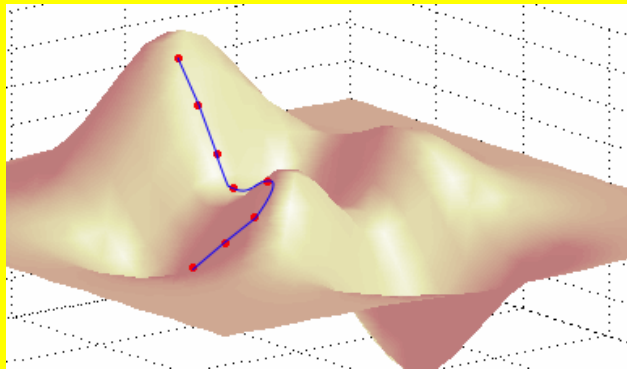


# Metaheuristic Algorithms

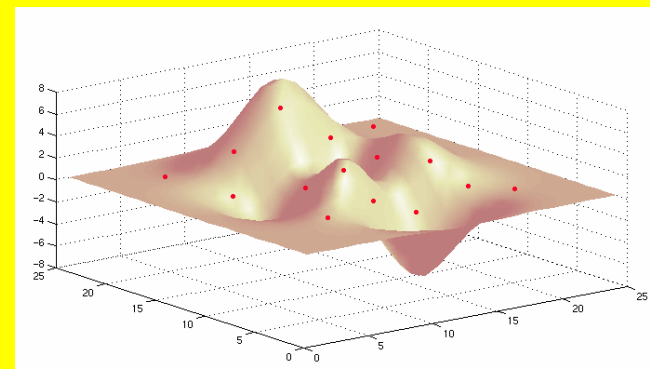
- Designed to solve **optimization problems**
  - Maximize or minimize a given function: the **fitness function**
- They can find **“good”** solutions with a **“reasonable”** amount of resources

## Metaheuristic Algorithms

Single solution



Population



# Metaheuristics Classification

## Single solution

Greedy Randomized  
Adaptive Search  
Procedure

Iterated Local  
Search

Variable  
Neighborhood  
Search

Tabu  
Search

Simulated  
Annealing

Iterative  
Improvement

Guided Local  
Search

## Population

Estimation of  
Distribution  
Algorithms

Evolutionary  
Computation

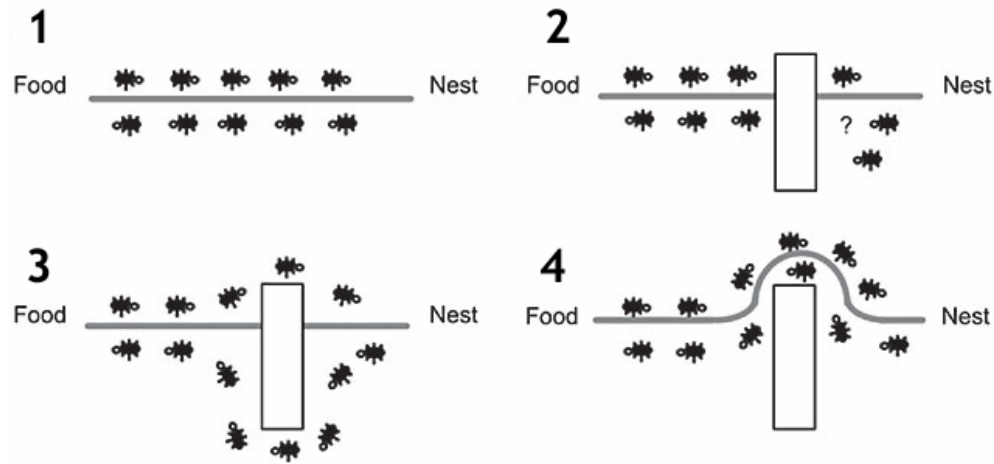
Scatter  
Search

Ant Colony  
Optimization

Particle Swarm  
Optimization

# ACO: Introduction

- **Ant Colony Optimization (ACO)** metaheuristic is inspired by the foraging behaviour of real ants



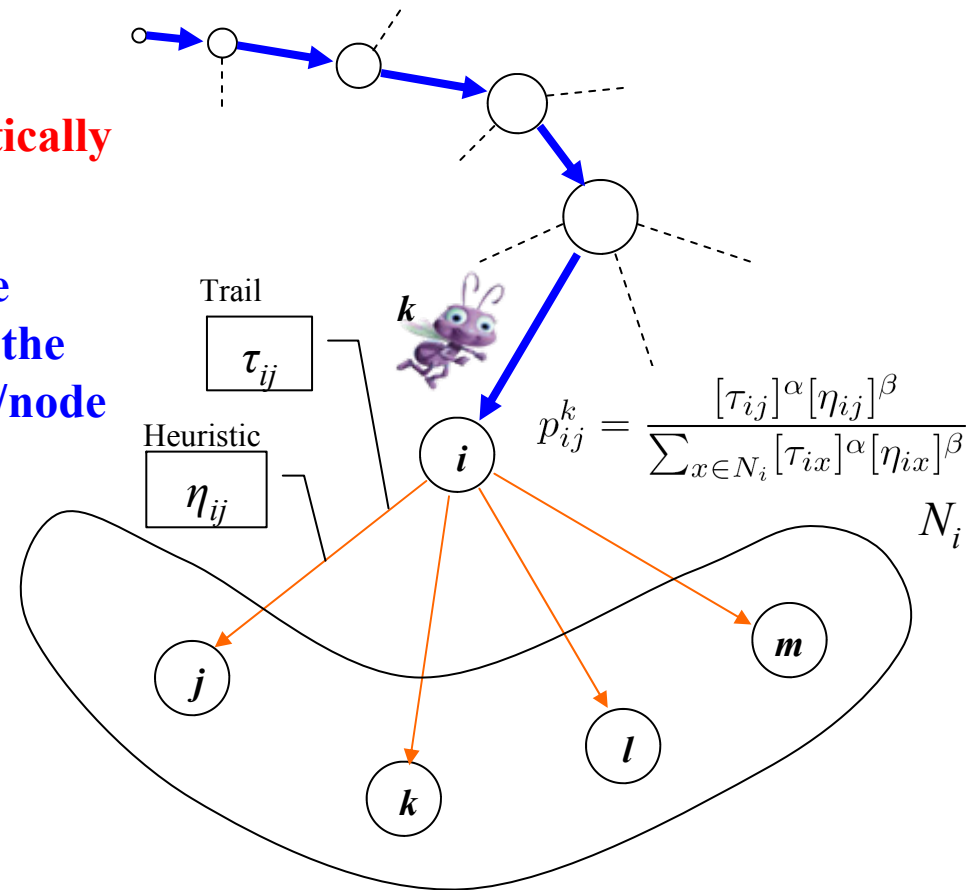
- **ACO Pseudo-code**

```

procedure ACOMetaheuristic
  ScheduleActivities
    ConstructAntsSolutions
    UpdatePheromones
    DaemonActions // optional
  end ScheduleActivities
end procedure
  
```

# ACO: Construction Phase

- The ant selects its next node **stochastically**
- The probability of selecting one node depends on the **pheromone trail** and the **heuristic value** (optional) of the edge/node
- The ant stops when a complete solution is built



# ACO: Pheromone Update

- **Pheromone update**

- **During the construction phase**

$$\tau_{ij} \leftarrow (1 - \xi)\tau_{ij} \quad \text{with} \quad 0 \leq \xi \leq 1$$

- **After the construction phase**

$$\tau_{ij} \leftarrow (1 - \rho)\tau_{ij} + \Delta\tau_{ij}^{bs} \quad \text{with} \quad 0 \leq \rho \leq 1$$

- **Trail limits (particular of MMAS)**

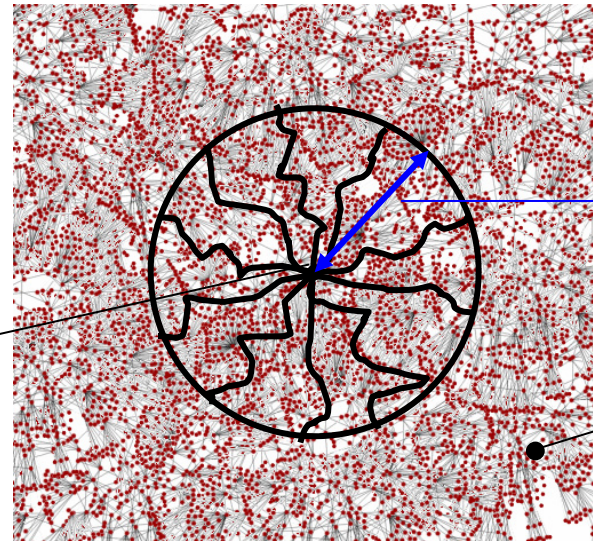
- **Pheromones are kept in the interval  $[\tau_{\min}, \tau_{\max}]$**

$$\tau_{max} = \frac{Q}{\rho} \qquad \tau_{min} = \frac{\tau_{max}}{a}$$

# ACOhg: Huge Graphs Exploration

The length of the ant  
paths is limited by  $\lambda_{\text{ant}}$

Initial node

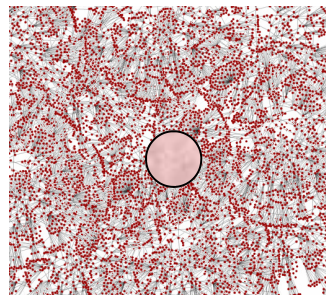


$\lambda_{\text{ant}}$

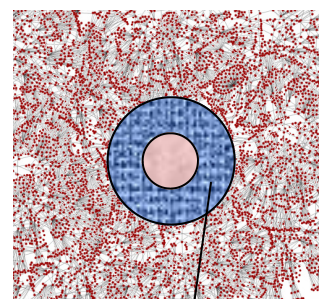
What if...?  
Objective node



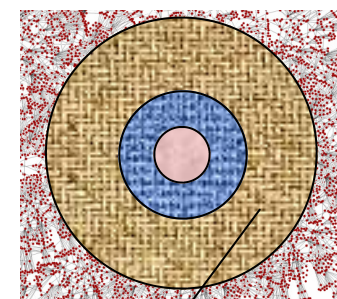
Starting nodes for path construction change



After  $\sigma_s$  steps



Second stage



Third stage

# ACOhg-live

- The search is an alternation of two phases

- **First phase:** search for accepting states
- **Second phase:** search for cycles from the accepting states

## ACOhg-live Pseudocode

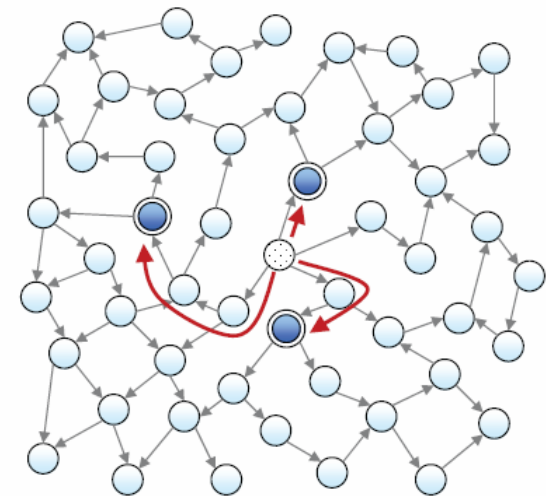
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```

1: repeat
2:   accept = acohg1.findAcceptingStates(); {First phase}
3:   for node in accept do
4:     acohg2.findCycle(node); {Second phase}
5:     if acohg2.cycleFound() then
6:       return acohg2.acceptingPath();
7:     end if
8:   end for
9:   acohg1.insertTabu(accept);
10: until empty(accept)
11: return null;

```

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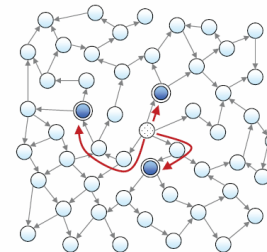
**First phase**

# ACOhg-live

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## ACOhg-live Pseudocode

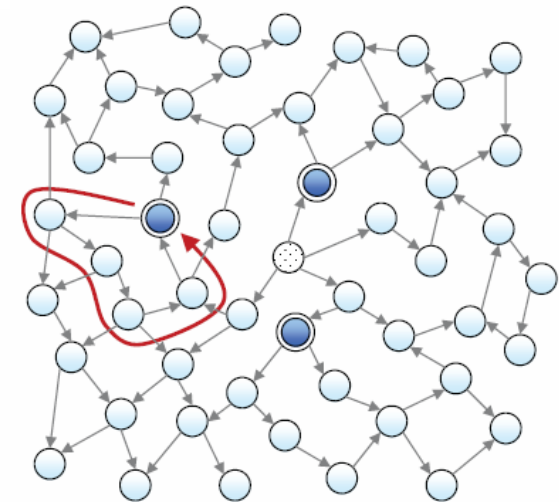
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---



**Second phase**

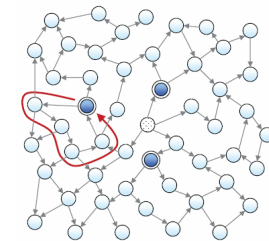
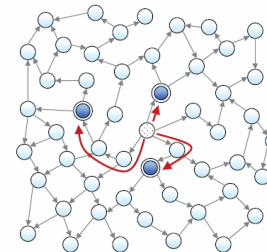


# ACOhg-live

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## ACOhg-live Pseudocode

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---

# Promela Models

- We selected **7 Promela models** for the experiments

Model	LoC	Scalable	Processes	LTL formula (liveness)
<code>alter</code>	64	no	2	$\Box(p \rightarrow \Diamond q) \wedge \Box(r \rightarrow \Diamond s)$
<code>giopij</code>	740	yes	$i+3(j+1)$	$\Box(p \rightarrow \Diamond q)$
<code>phij</code>	57	yes	$j+1$	$\Box(p \rightarrow \Diamond q)$

- Parameters for **ACOhg-live**

Parameter	<i>msteps</i>	<i>colsize</i>	$\lambda_{\text{ant}}$	$\sigma_s$	$\xi$	<i>a</i>	$\rho$	$\alpha$	$\beta$
1st phase	100	10	20	4	0.7	5	0.2	1.0	2.0
2nd phase		20	4		0.5				

- ACOhg-live implemented in **HSF-SPIN**
- 100** independent executions

# Promela Models

- We selected **7 Promela models** for the experiments

Model	LoC		Processes	LTL formula (liveness)
alter	61	<b>i=2,6,10</b> <b>j=2</b>	2	$\square(p \rightarrow \diamond q) \wedge \square(r \rightarrow \diamond s)$
giopij	740		$i+3(j+1)$	$\square(p \rightarrow \diamond q)$
phij	57	<b>j=8,14,20</b>	$j+1$	$\square(p \rightarrow \diamond q)$

- Parameters for **ACOhg-live**

Parameter	<i>msteps</i>	<i>colsize</i>	$\lambda_{\text{ant}}$	$\sigma_s$	$\xi$	<i>a</i>	$\rho$	$\alpha$	$\beta$
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- ACOhg-live** implemented in **HSF-SPIN**
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# Results I: Comparison of Heuristic Information

## • Comparison of $H_{ham}$ and $H_{fsm}$

Models	Measure	$H_{ham}$		$H_{fsm}$		Test
alter	Hit rate	100/100		100/100		-
	Length	28.54	9.44	30.68	10.72	-
	Mem. (KB)	1925.00	0.00	1925.00	0.00	-
	Time (ms)	88.90	15.03	90.00	13.86	-
giop2	Hit rate	100/100		100/100		-
	Length	43.09	5.33	43.76	5.82	-
	Mem. (KB)	2834.48	369.42	2953.76	327.48	+
	Time (ms)	817.50	560.73	747.50	408.09	-
giop6	Hit rate	100/100		100/100		-
	Length	58.41	7.16	58.77	7.21	-
	Mem. (KB)	5418.32	1161.17	5588.04	631.36	-
	Time (ms)	16049.10	15256.93	8733.50	3304.90	-
giop10	Hit rate	60/100		86/100		+
	Length	61.10	6.42	62.85	7.03	-
	Mem. (KB)	9669.80	1597.14	9316.67	700.44	+
	Time (ms)	87236.00	69218.19	43059.07	21417.74	+
phi8	Hit rate	100/100		100/100		-
	Length	52.38	9.26	51.36	6.95	-
	Mem. (KB)	2097.52	21.74	2014.32	18.87	+
	Time (ms)	2271.40	573.56	2126.10	479.64	-
phi14	Hit rate	99/100		99/100		-
	Length	74.68	8.66	76.05	9.35	-
	Mem. (KB)	2593.37	179.03	2496.07	41.81	+
	Time (ms)	9369.90	3706.83	8070.30	1530.12	+
phi20	Hit rate	99/100		98/100		-
	Length	95.28	9.97	97.39	10.14	-
	Mem. (KB)	3324.26	104.27	3244.67	91.33	+
	Time (ms)	21323.54	10600.89	18064.90	5538.30	+

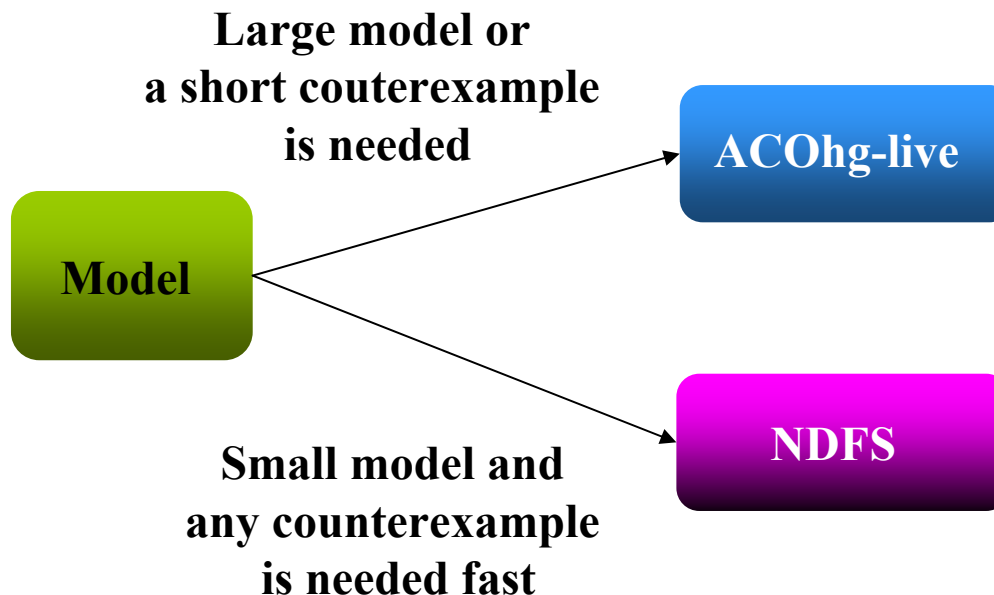
# Results II: Comparison of ACOhg-live and NDFS

## • Comparison of ACOhg-live and NDFS

Models	Measure	ACOhg-live	Nested-DFS	Test
alter	Hit rate	100/100	1/1	-
	Length	30.68	64.00	+
	Mem. (KB)	1925.00	1873.00	+
	Time (ms)	90.00	0.00	+
giop2	Hit rate	100/100	1/1	-
	Length	43.76	298.00	+
	Mem. (KB)	2953.76	7865.00	+
	Time (ms)	747.50	240.00	+
giop6	Hit rate	100/100	0/1	+
	Length	58.77	•	•
	Mem. (KB)	5588.04	•	•
	Time (ms)	8733.50	•	•
giop10	Hit rate	86/100	0/1	+
	Length	62.85	•	•
	Mem. (KB)	9316.67	•	•
	Time (ms)	43059.07	•	•
phi8	Hit rate	100/100	1/1	-
	Length	51.36	3405.00	+
	Mem. (KB)	2014.32	4005.00	+
	Time (ms)	2126.10	40.00	+
phi14	Hit rate	99/100	1/1	-
	Length	76.05	10001.00	+
	Mem. (KB)	2496.07	59392.00	+
	Time (ms)	8070.30	2300.00	+
phi20	Hit rate	98/100	1/1	-
	Length	97.39	10001.00	+
	Mem. (KB)	3244.67	392192.00	+
	Time (ms)	18064.90	17460.00	-

# How to use ACOhg-live

- ACOhg-live should be used in the **first/middle stages** of the software development, when software errors are expected
- ACOhg-live can also be used in other phases of the software development for **testing** concurrent software



# Conclusions & Future Work

## Conclusions

- ACOhg-live is the **first algorithm** based on metaheuristics (to the best of our knowledge) applied to the search for liveness errors in concurrent models
- The heuristic function based on **finite state machines** is a better guide in the second phase of ACOhg-live
- ACOhg-live is able to **outperform Nested-DFS** in efficacy and efficiency in the search for liveness errors

## Future Work

- Use of **Strongly Connected Components** of the never claim graph for improving the search (in progress)
- Analysis of parameterization for **reducing the parameters**
- Include ACOhg-live into **JavaPathFinder** for finding liveness errors in Java programs

# Finding Liveness Errors with ACO

Thanks for your attention !!!

