



# Recent Research on Search Based Software Testing



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# Optimization Problem

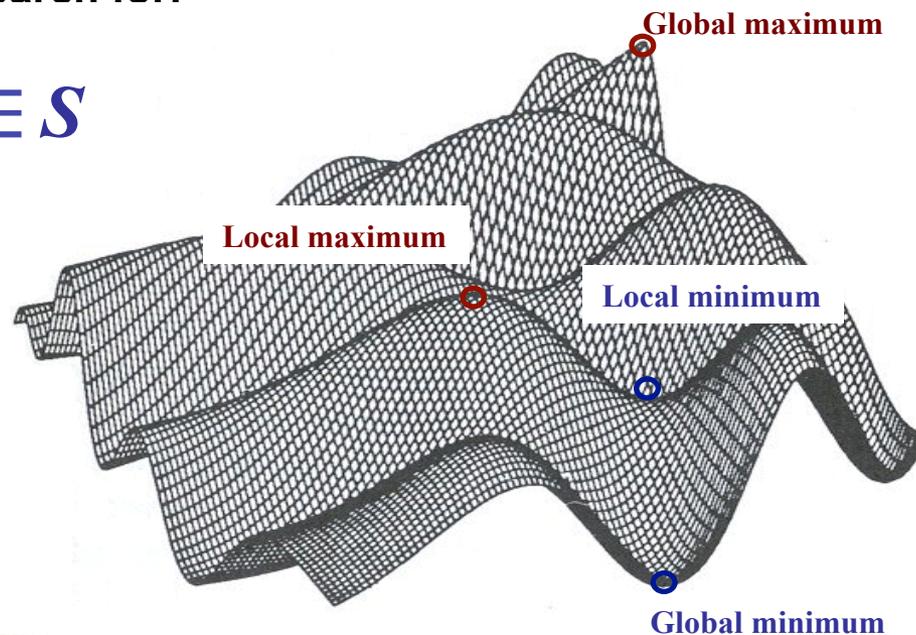
An optimization problem is a pair:  $P = (S, f)$  where:

$S$  is a set of solutions (solution or search space)

$f: S \rightarrow \mathbf{R}$  is an objective function to minimize or maximize

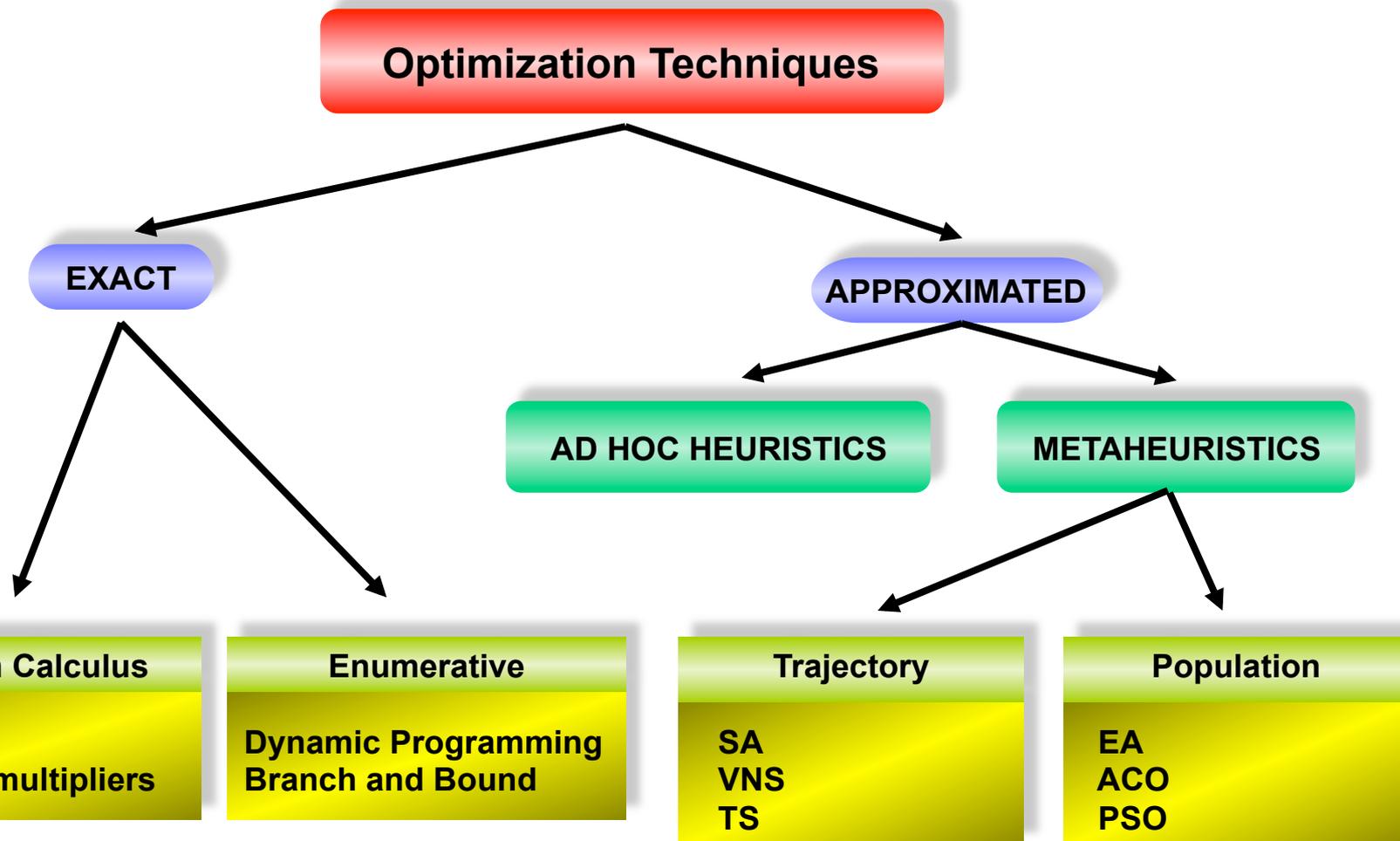
If our goal is to **minimize** the function we search for:

$$s' \in S \mid f(s') \leq f(s), \forall s \in S$$





# Optimization Techniques





# Evolutionary Algorithm

## Pseudocode of a simple EA

```
 $P$  = generateInitialPopulation ();  
evaluate ( $P$ );  
while not stoppingCondition () do  
     $P'$  = selectParents ( $P$ );  
     $P'$  = applyVariationOperators ( $P'$ );  
    evaluate( $P'$ );  
     $P$  = selectNewPopulation ( $P$ , $P'$ );  
end while  
return the best solution found
```

Three main steps: **selection, reproduction, replacement**

**Variation** operators → Make the population to **evolve**

Recombination: **exchange** of features

Mutation: generation of **new features**



# Evolutionary Algorithm

## Genetic Algorithms

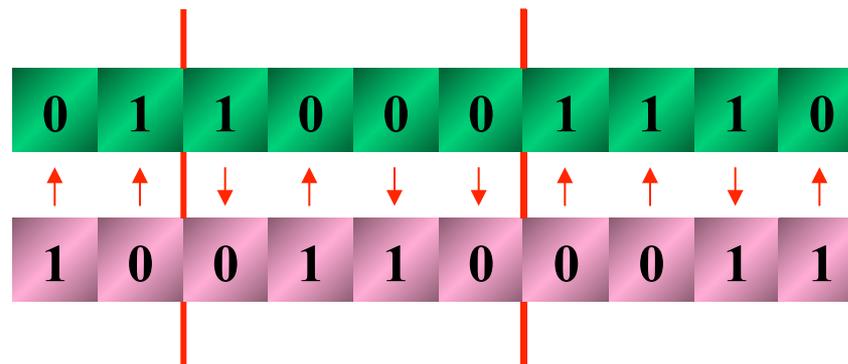
- Individuals

### Binary Chromosome



- Recombination

- One point
- Two points
- Uniform



- Mutation → bit flips





# Software Testing: Definition and Goal

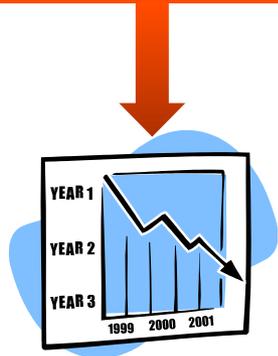
- What is software testing?
  - It is the process of running a software product or a portion of it in a controlled environment with a given input followed by the collection and analysis of the output and/or other relevant information of the execution.
- What is the **goal of software testing**?
  - To find out errors in a portion or the complete software product and/or to assure with a high probability that the software is correct (according to the requirements).



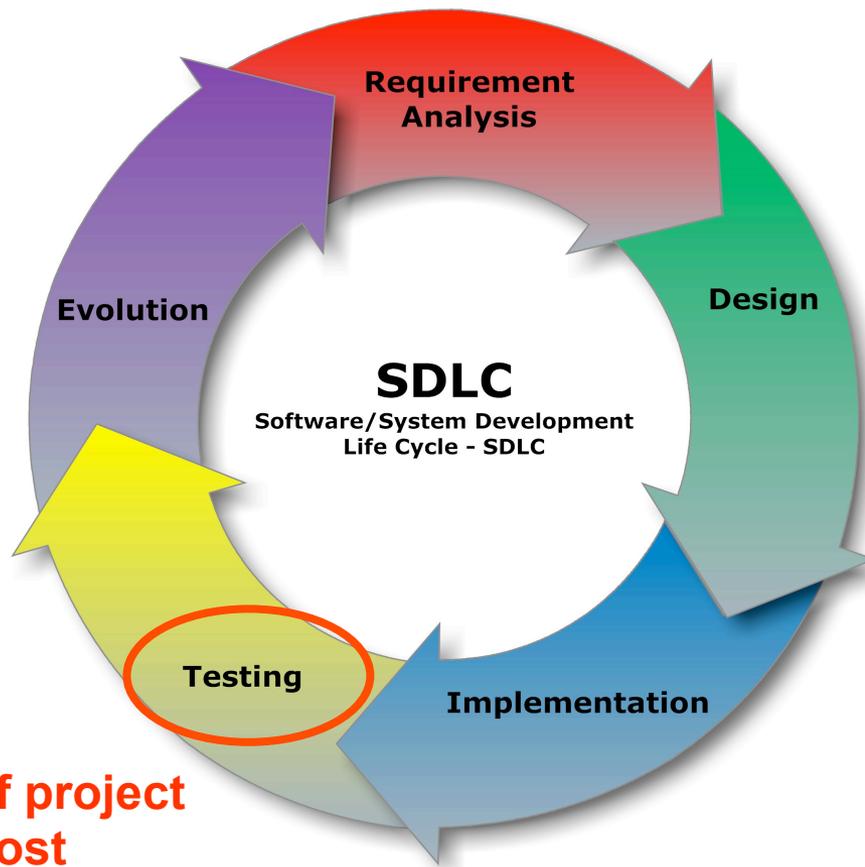
# Software Testing: Impact

Software testing is important because...

**Software errors**



**60.000 M\$ annually (0,6% GDP) in USA**



**60 % of project cost**



# Software Testing: Classification

Classification of testing techniques (by goal)

- **Unit testing**: test one module of the software.
- **Integration testing**: test the interfaces between different modules in the software.
- **System testing**: test the complete system.
- **Validation testing**: test if the software system fulfills the requirements.
- **Acceptance testing**: the client test whether the system is what s/he wants.
- **Regression testing**: after a change in the software test whether a new error has been introduced.
- **Stress testing**: test the system under a high load
- **Load testing**: test the response of the system under a normal load of work.



# Software Testing: Automatization

Test case design

Test case run

Check of results

1.0, 2.3

2.7, 5.4

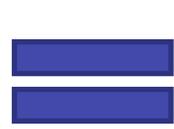
Error!



Automatic test case generation

nit, Ea  
nit,  
Selenium

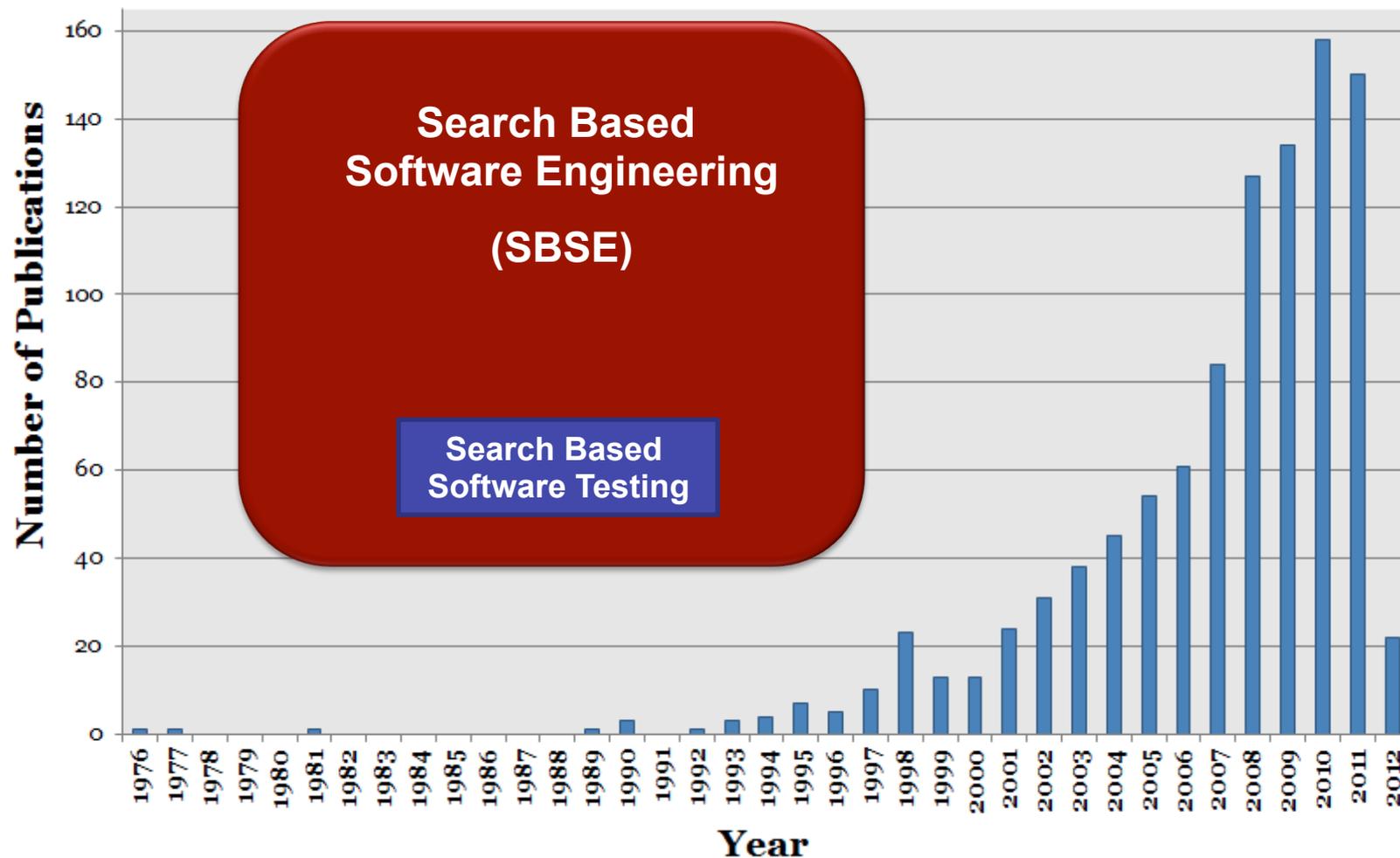
Search Techniques



Search Based Software Testing



# Search Based Software Engineering

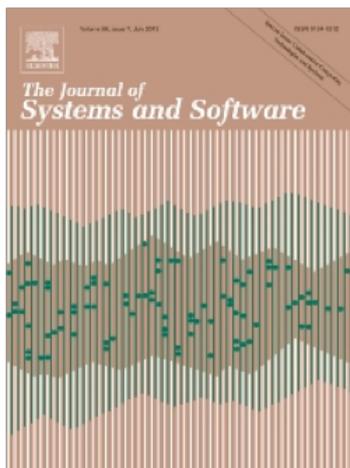




# Search Based Software Engineering

Special Issue on SBSE in Journal of Systems and Software (JSS)

Deadline: **November 15th**



Guest editors:

M. Harman & F. Chicano



<http://neo.lcc.uma.es/mase/index.php/jss-sbse>



# Our Research on SBSE

- **Software Project Scheduling**
- **White-box Software Testing**
- **Testing of Concurrent Systems (based on Model Checking)**
- **Test Sequences for Functional Testing**
- **Test Suite Minimization in Regression Testing**
- **Software Product Lines Testing**
- **Prioritized Pairwise Combinatorial Interaction Testing**
- **Testing Complexity**



# Test Suite Minimization in Regression Testing



# Test Suite Minimization

Given:

- A set of test cases  $T = \{t_1, t_2, \dots, t_n\}$
- A set of program elements to be covered (e.g., branches)  $E = \{e_1, e_2, \dots, e_k\}$
- A coverage matrix

$$M =$$

	$e_1$	$e_2$	$e_3$	...	$e_k$
$t_1$	1	0	1	...	1
$t_2$	0	0	1	...	0
...	...	...	...	...	...
$t_n$	1	1	0	...	0

$$m_{ij} = \begin{cases} 1 & \text{if element } e_j \text{ is covered by test } t_i \\ 0 & \text{otherwise} \end{cases}$$

Find a subset of tests  $X \subseteq T$  maximizing coverage and minimizing the testing cost

$$\text{minimize } \text{cost}(X) = \sum_{\substack{i=1 \\ t_i \in X}}^n c_i$$

Yoo & Harman

$$\text{maximize } \text{cov}(X) = |\{e_j \in \mathcal{E} \mid \exists t_i \in X \text{ with } m_{ij} = 1\}|$$



# Binary Search Space

- The set of solutions is the set of **binary strings** with length  $n$

0 1 0 0 1 0 1 1 1 0

- Neighborhood used: **one-change neighborhood**

- Two solutions  $x$  and  $y$  are neighbors iff  $\text{Hamming}(x,y)=1$

0 1 0 0 1 0 1 1 1 0

1 1 0 0 1 0 1 1 1 0

0 0 0 0 1 0 1 1 1 0

0 1 1 0 1 0 1 1 1 0

0 1 0 1 1 0 1 1 1 0

0 1 0 0 0 0 1 1 1 0

0 1 0 0 1 1 1 1 1 0

0 1 0 0 1 0 0 1 1 0

0 1 0 0 1 0 1 0 1 0

0 1 0 0 1 0 1 1 0 0

0 1 0 0 1 0 1 1 1 1



# Elementary Landscapes: Characterizations

- An **elementary landscape** is a landscape for which

$$\text{avg}_{y \in N(x)} \{f(y)\} = \alpha f(x) + \beta \quad \forall x \in X$$

Depend on the  
problem/instance

where

$$\text{avg}_{y \in N(x)} \{f(y)\} \stackrel{\text{def}}{=} \frac{1}{d} \sum_{y \in N(x)} f(y)$$

Linear relationship

- **Grover's wave equation**

$$\text{avg}_{y \in N(x)} \{f(y)\} = f(x) + \frac{\lambda}{d} (\bar{f} - f(x))$$

$$\alpha = 1 - \frac{\lambda}{d}$$

$$\beta = \frac{\lambda}{d} \bar{f}$$

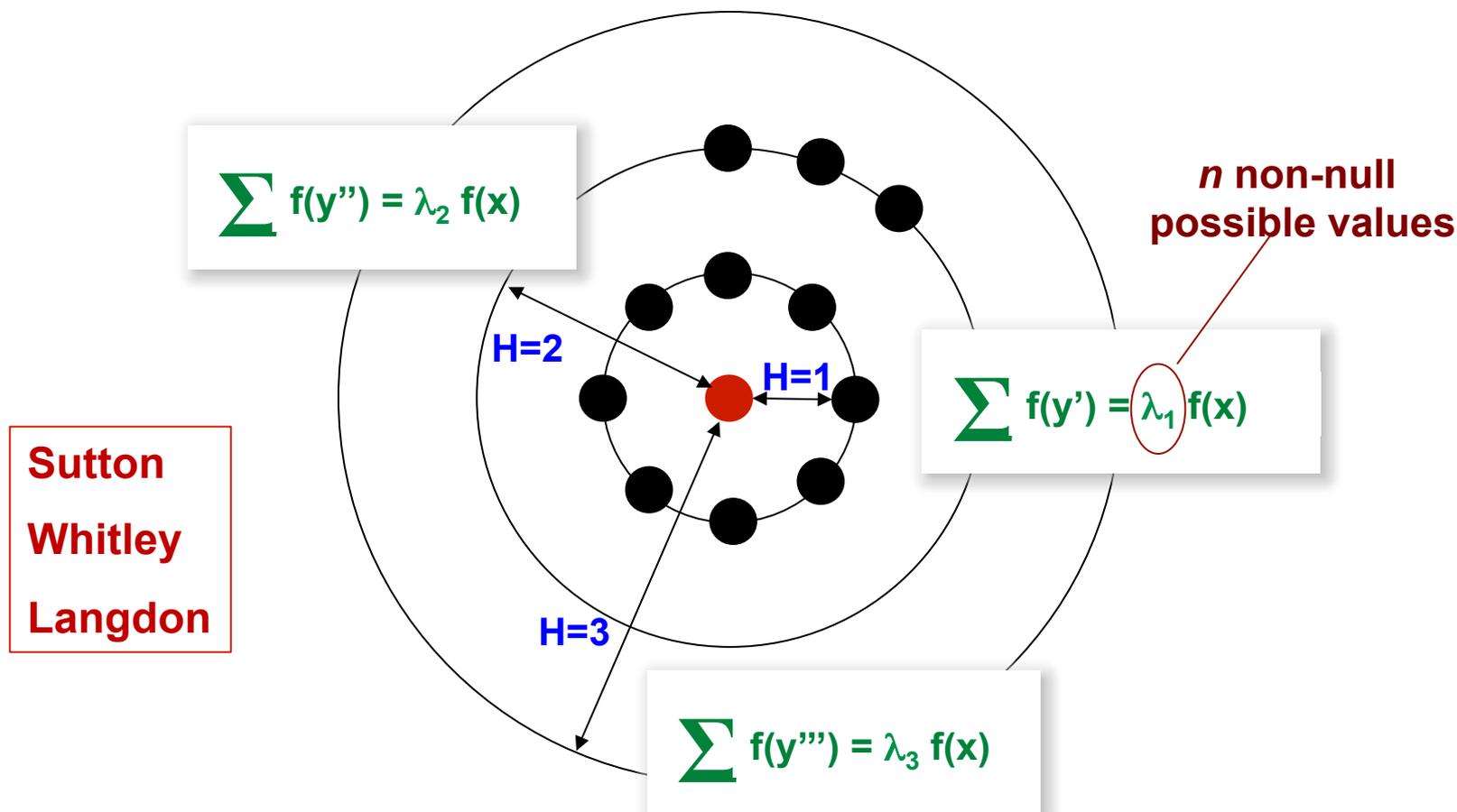
Eigenvalue

$$\bar{f} = \frac{1}{|X|} \sum_{y \in X} f(y)$$



# Spheres around a Solution

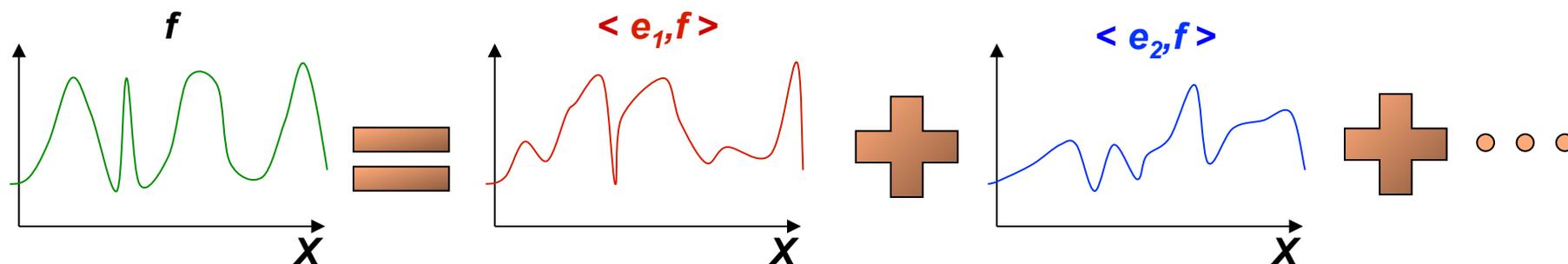
- If  $f$  is elementary, the average of  $f$  in any sphere and ball of any size around  $x$  is a linear expression of  $f(x)$ !!!



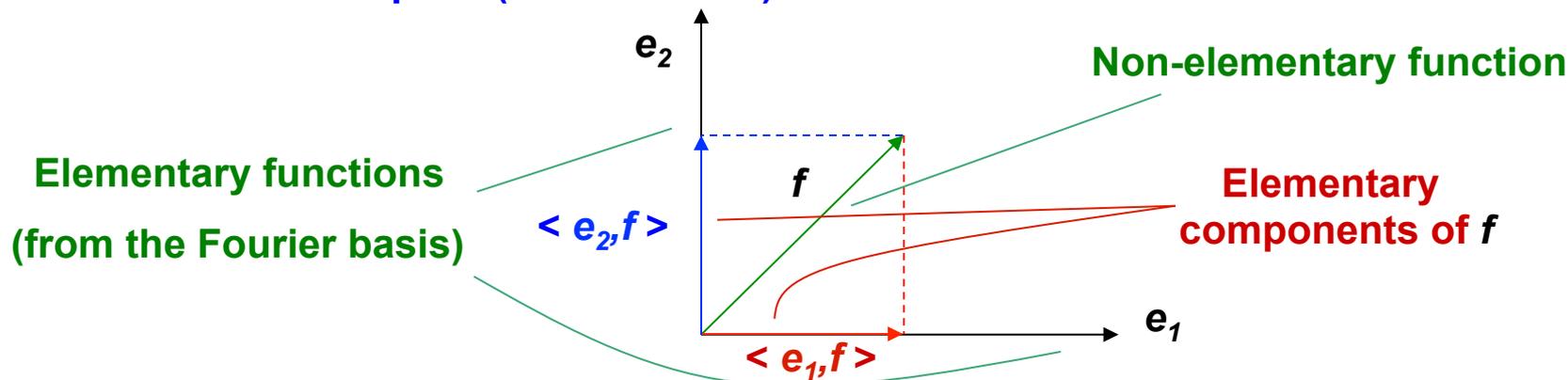


# Landscape Decomposition

- What if the landscape is **not elementary**?
- Any landscape can be written as the **sum of elementary landscapes**



- There exists a set of **eigenfunctions of  $\Delta$**  that form a basis of the function space (**Fourier basis**)





# Elementary Landscape Decomposition of $f$

- The elementary landscape decomposition of

$$f(x) = cov(x) - c \cdot cost(x)$$

Computable in  
 $O(nk)$

is

Tests that cover  $e_i$

$$f^{(0)}(x) = \sum_{i=1}^k \left( 1 - \frac{1}{2^{|V_i|}} \right) - c \cdot \frac{n}{2} \quad \leftarrow \text{constant expression}$$

$$f^{(1)}(x) = - \sum_{i=1}^k \frac{1}{2^{|V_i|}} (-1)^{n_1^{(i)}} \mathcal{K}_{|V_i|-1, n_1^{(i)}}^{|V_i|} - c \cdot \left( ones(x) - \frac{n}{2} \right)$$

Krawtchouk matrix

$$f^{(p)}(x) = - \sum_{i=1}^k \frac{1}{2^{|V_i|}} (-1)^{n_1^{(i)}} \mathcal{K}_{|V_i|-p, n_1^{(i)}}^{|V_i|} \quad \text{where } 1 < p \leq n$$

Tests in the solution that cover  $e_i$

F. Chicano et al., SSBSE 2011



# Elementary Landscape Decomposition of $f^2$

- The elementary landscape decomposition of  $f^2$  is

$$(f^2)^{(0)}(x) = \beta^2 + \frac{c^2}{4}n - \sum_{i=1}^k \frac{c|V_i| + 2\beta}{2^{|V_i|}} + \sum_{i,i'=1}^k \frac{1}{2^{|V_i \cup V_{i'}|}}$$

Computable in  
 $O(nk^2)$

$$\beta = k - cn/2$$

Number of tests that cover  $e_i$  or  $e_{i'}$

$$(f^2)^{(p)}(x) = - \sum_{i=1}^k \left( \frac{(c|V_i| + 2\beta)(-1)^{n_1^{(i)}}}{2^{|V_i|}} \mathcal{K}_{|V_i|-p, n_1^{(i)}} \right) \quad p > 2$$

$$+ \sum_{i,i'=1}^k \left( \frac{(-1)^{n_1^{(i \vee i')}}}{2^{|V_i \cup V_{i'}|}} \mathcal{K}_{|V_i \cup V_{i'}|-p, n_1^{(i \vee i')}} \right)$$

$$- c \sum_{i=1}^k \frac{(-1)^{n_1^{(i)}}}{2^{|V_i|}} \mathcal{K}_{|V_i|-p+1, n_1^{(i)}} \left( n - 2 \text{ones}(x) - |V_i| + 2n_1^{(i)} \right)$$

Number of tests in  
the solution that  
cover  $e_i$  or  $e_{i'}$



# Guarded Local Search

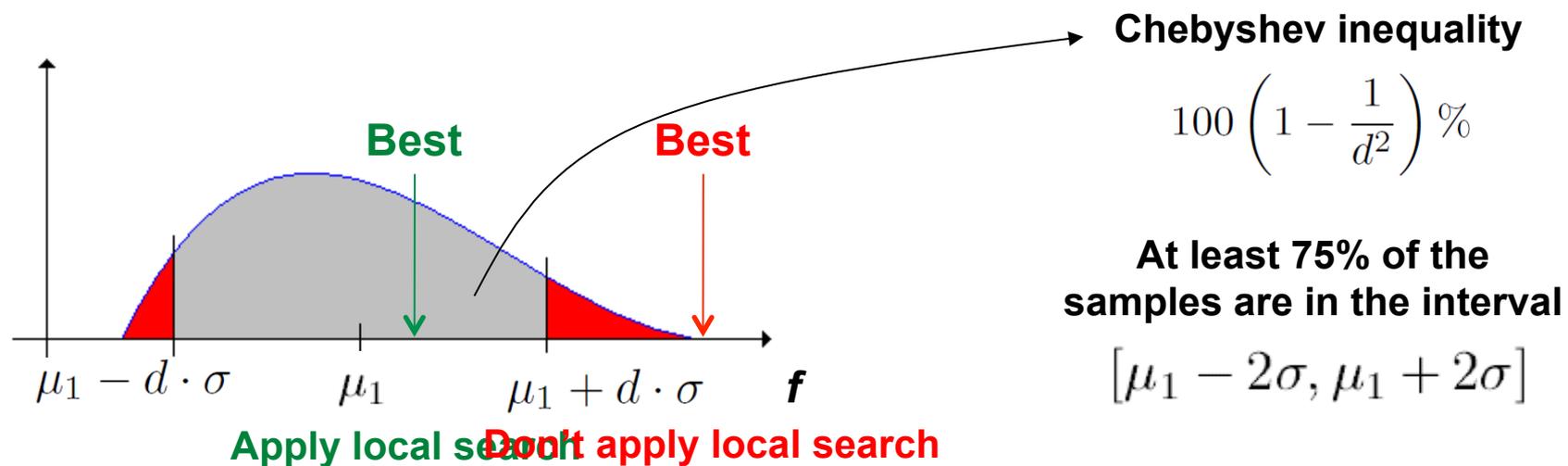
- With the Elementary Landscape Decomposition (ELD) we can compute:

$$\mu_c = \text{avg}_{y|\mathcal{H}(y,x)=r} \{f^c(y)\} = \binom{n}{r}^{-1} \sum_{p=0}^n \mathcal{K}_{r,p}^{(n)} (f^c)^{(p)}(x)$$

- With the ELD of  $f$  and  $f^2$  we can compute for any sphere and ball around a solution:

$$\mu_1 : \text{the average} \quad \sigma = \sqrt{\mu_2 - \mu_1^2} : \text{the standard deviation}$$

- Distribution of values around the average



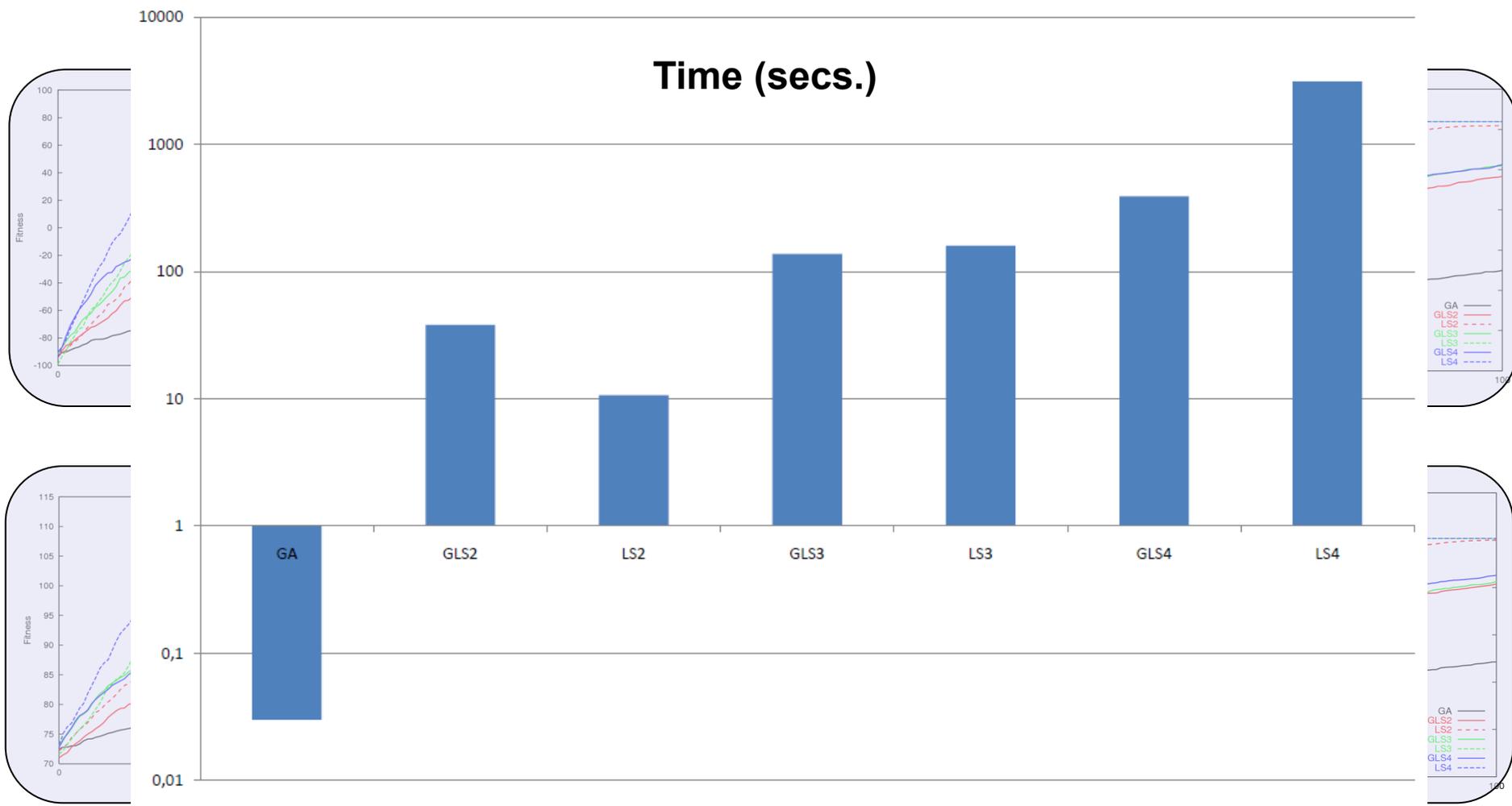


# Guarded Local Search: Experimental Setting

- **Steady state genetic algorithm**: bit-flip ( $p=0.01$ ), one-point crossover, elitist replacement
    - **GA** (no local search)
    - **GLSr** (guarded local search up to radius  $r$ )
    - **LSr** (always local search in a ball of radius  $r$ )
  - **Instances from the Software-artifact Infrastructure Repository (SIR)**
    - printtokens
    - printtokens2
    - schedule
    - schedule2
    - totinfo
    - replace
- Oracle cost  $c=1..5$**   
 **$n=100$  test cases**  
 **$k=100-200$  items to cover**  
**100 independent runs**



# Guarded Local Search: Results





# NP-hard Problems

In many papers we can read...

“Our optimization problem is NP-hard, and for this reason we use...

- **Metaheuristic techniques**
- **Heuristic algorithms**
- **Stochastic algorithms**

... which do not ensure an optimal solution but they are able to find good solutions in a reasonable time.”

As far as we know: **no efficient** (polynomial time) algorithm exists for solving NP-hard problems

But **we know inefficient algorithms** (at least exponential time)



# The SATisfiability Problem

Can we find an assignment of boolean values (**true and false**) to the variables such that all the formulas are satisfied?

$$\neg A \wedge (B \vee C)$$

$$(A \vee B) \wedge (\neg B \vee C \vee \neg D) \wedge (D \vee \neg E)$$

$$A \vee B$$

The **first NP-complete** problem (Stephen Cook, 1971)

If it can be solved efficiently (polynomial time) then **P=NP**

The known algorithms solve this problem in **exponential time (worst case)**

## State-of-the-art algorithms in SAT

Nowadays, SAT solvers can solve instances with **500 000 boolean variables**

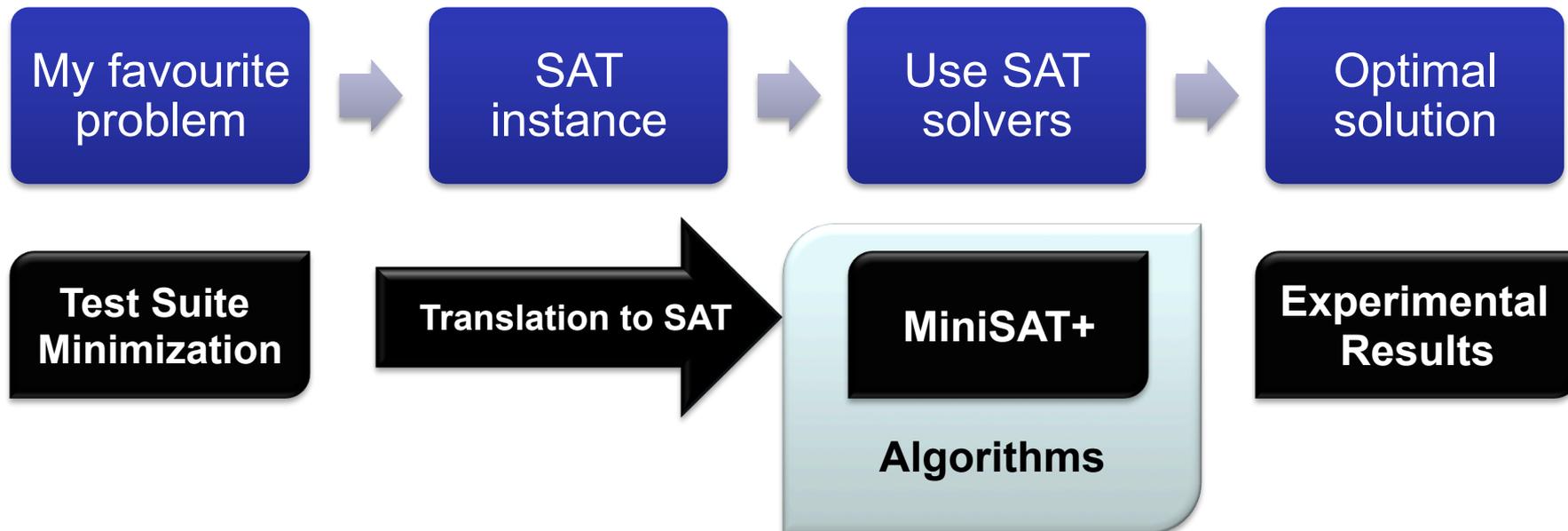
This means a search space of  **$2^{500\,000} \approx 10^{150514}$**



# The SATisfiability Problem

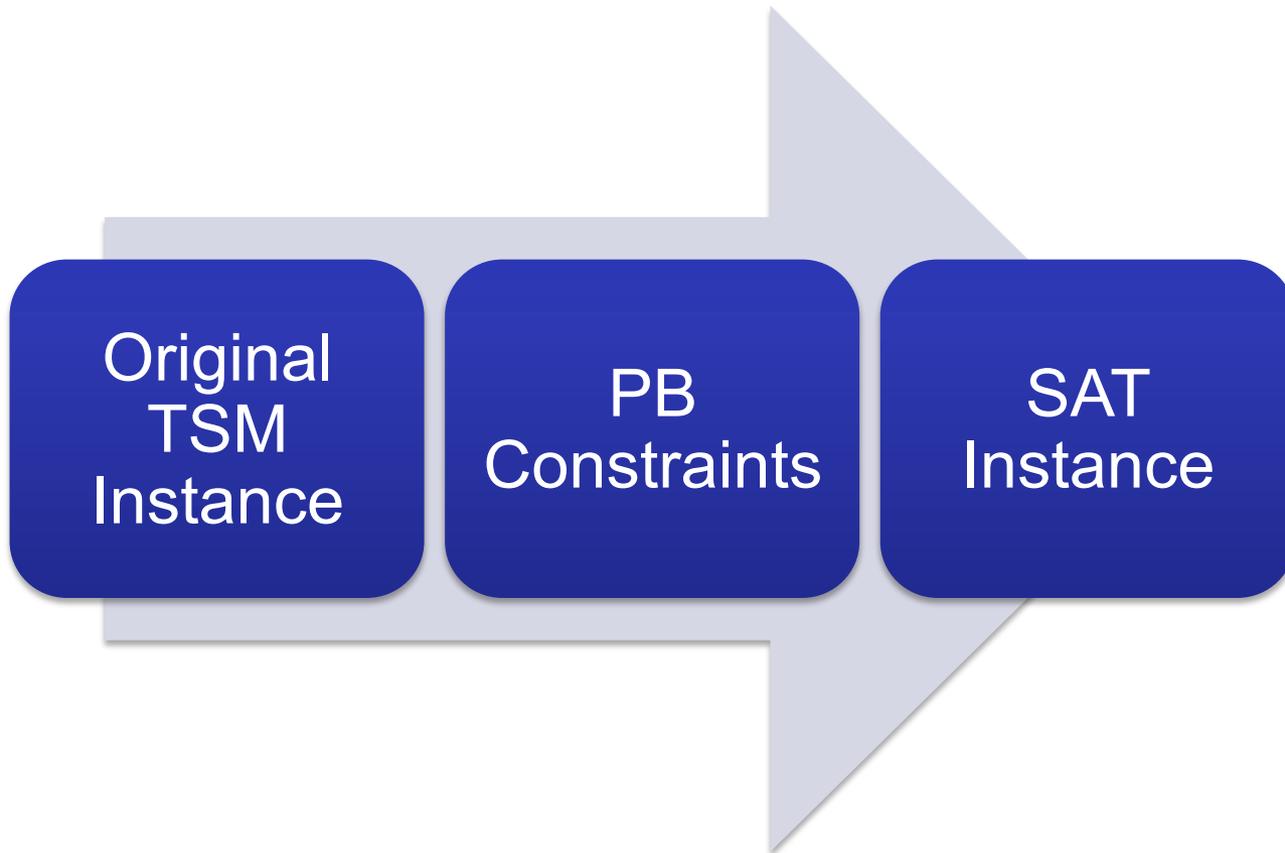
**Main research question:**

**Can we use the advances of SAT solvers to solve optimization algorithms up to optimality?**





# Outline





# Pseudo-Boolean Constraints

A Pseudo-Boolean (PB) constraint has the form:

$$\sum_{i=1}^n a_i x_i \odot B$$

where

$$\odot \in \{<, \leq, =, \neq, >, \geq\}$$

$$a_i, B \in \mathbb{Z} \quad x_i \in \{0, 1\}$$

Can be translated to SAT instances (**usually efficient**)

Are a **higher level formalism** to specify a decision problem

Can be the input for **MiniSAT+**



# Translating Optimization to Decision Problems

Let us assume we want to minimize  $f(x)$

**Check Check Check Check**

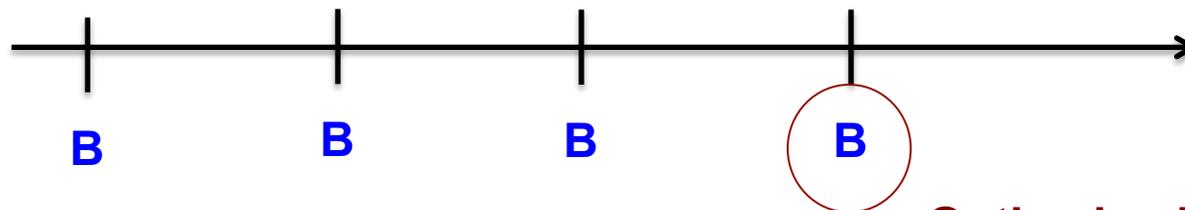
$$f(x) \leq \cancel{f(x)} \leq \cancel{f(x)} \leq \cancel{f(x)} \leq B$$

no

no

no

yes



**Optimal solution found**

The same can be done with **multi-objective problems**, but we need more PB constraints

$$f_1(y) \leq B_1 \quad f_2(y) \leq B_2 \quad \dots \quad f_m(y) \leq B_m$$



# PB Constraints for the TSM Problem

$$\mathbf{M} =$$

	$e_1$	$e_2$	$e_3$	...	$e_m$
$t_1$	1	0	1	...	1
$t_2$	0	0	1	...	0
...	...	...	...	...	...
$t_n$	1	1	0	...	0

$$m_{ij} = \begin{cases} 1 & \text{if element } e_j \text{ is covered by test } t_i \\ 0 & \text{otherwise} \end{cases}$$

$$e_j \leq \sum_{i=1}^n m_{ij} t_i \leq n \cdot e_j \quad 1 \leq j \leq m$$

## Cost

$$\sum_{i=1}^n c_i t_i \leq B$$

## Coverage

$$\sum_{j=1}^m e_j \geq P$$



# Example

	$e_1$	$e_2$	$e_3$	$e_4$
$t_1$	1	0	1	0
$t_2$	1	1	0	0
$t_3$	0	0	1	0
$t_4$	1	0	0	0
$t_5$	1	0	0	1
$t_6$	0	1	1	0

**Bi-objective problem**

$$\left\{ \begin{array}{l} e_1 \leq t_1 + t_2 + t_4 + t_5 \leq 6e_1 \\ e_2 \leq t_2 + t_6 \leq 6e_2 \\ e_3 \leq t_1 + t_3 + t_6 \leq 6e_3 \\ e_4 \leq t_5 \leq 6e_4 \end{array} \right.$$

$$\left\{ \begin{array}{l} t_1 + t_2 + t_3 + t_4 + t_5 + t_6 \leq B \\ e_1 + e_2 + e_3 + e_4 \geq P \end{array} \right.$$

**Single-objective problem  
(total coverage)**

$$t_1 + t_2 + t_4 + t_5 \geq 1$$

$$t_2 + t_6 \geq 1$$

$$t_1 + t_3 + t_6 \geq 1$$

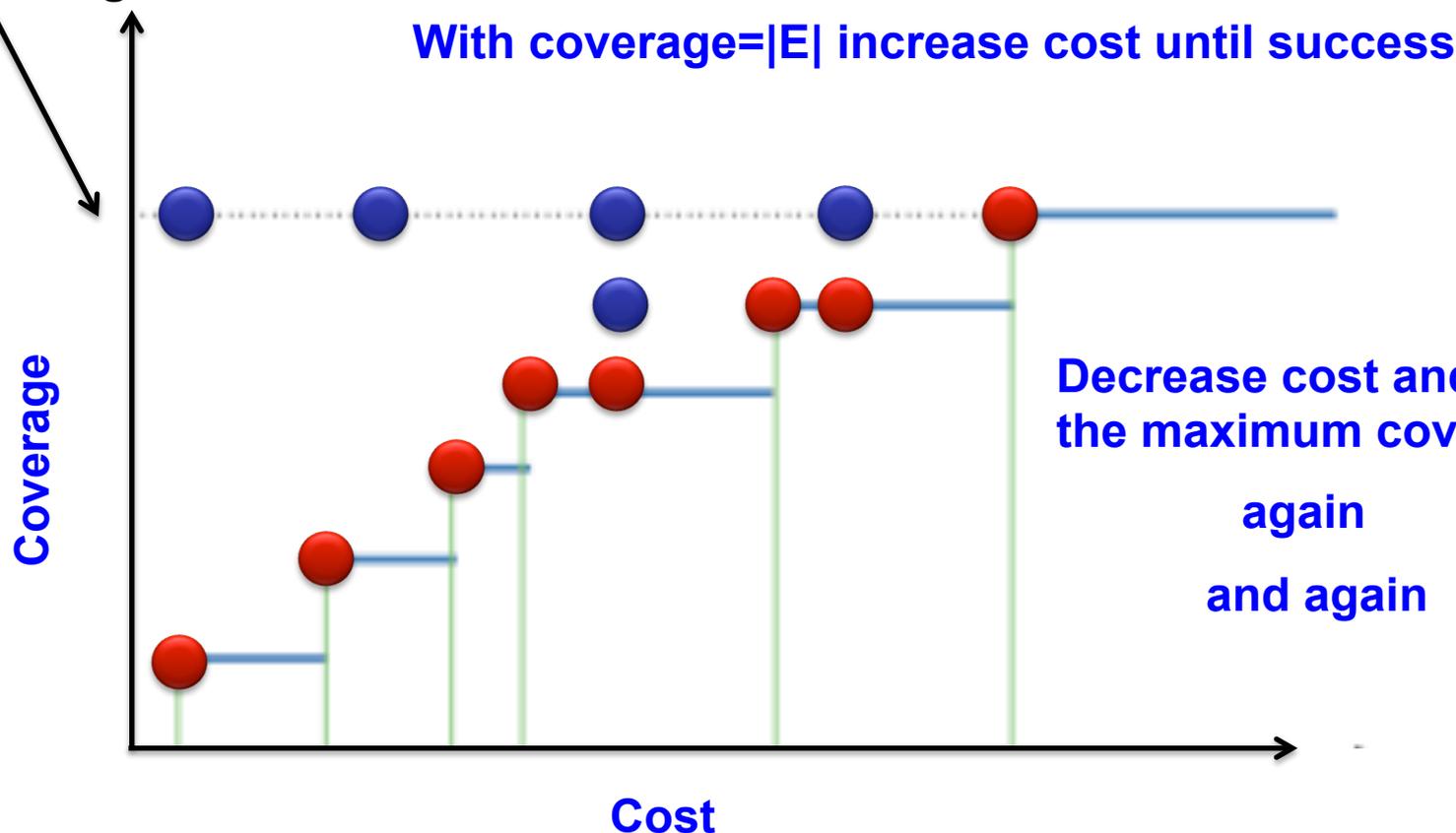
$$t_5 \geq 1$$

$$t_1 + t_2 + t_3 + t_4 + t_5 + t_6 \leq B$$



# Algorithm for Solving the 2-obj TSM

Total coverage





# TSM Instances

Instances from the **Software-artifact Infrastructure Repository (SIR)**

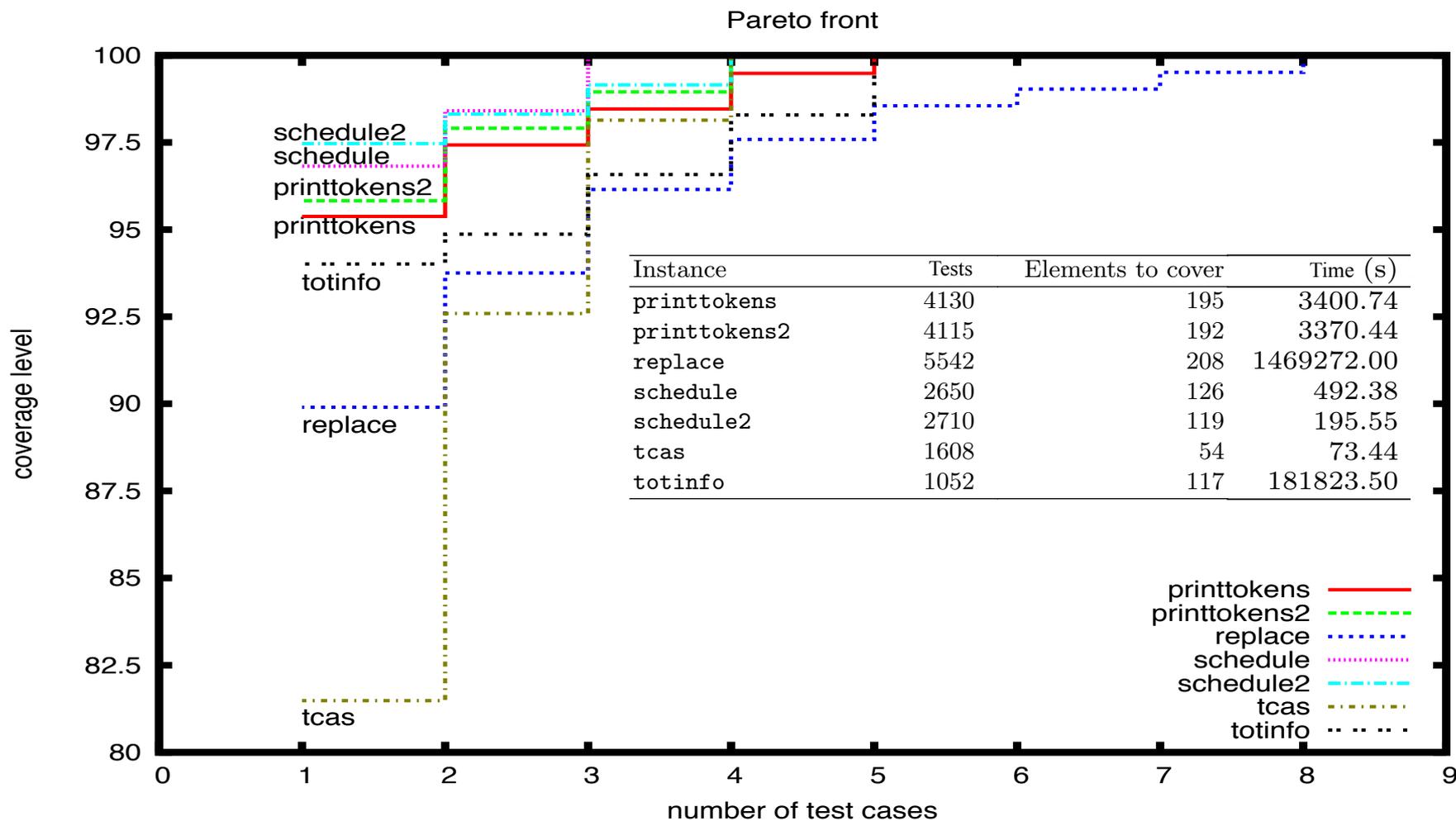
<http://sir.unl.edu/portal/index.php>

Instance	Tests	Elements to cover
printtokens	4130	195
printtokens2	4115	192
replace	5542	208
schedule	2650	126
schedule2	2710	119
tcas	1608	54
totinfo	1052	117

Cost of each test: 1



# Pareto Front





# Pareto Front

Instance	Elements	Tests	Coverage	Solution
printtokens	195	5	100%	( <i>t</i> <sub>2222</sub> , <i>t</i> <sub>2375</sub> , <i>t</i> <sub>3438</sub> , <i>t</i> <sub>4100</sub> , <i>t</i> <sub>4101</sub> )
	194	4	99.48%	( <i>t</i> <sub>1908</sub> , <i>t</i> <sub>2375</sub> , <i>t</i> <sub>4099</sub> , <i>t</i> <sub>4101</sub> )
	192	3	98.46%	( <i>t</i> <sub>1658</sub> , <i>t</i> <sub>2363</sub> , <i>t</i> <sub>4072</sub> )
	190	2	97.43%	( <i>t</i> <sub>1658</sub> , <i>t</i> <sub>3669</sub> )
	186	1	95.38%	( <i>t</i> <sub>2597</sub> )
printtokens2	192	4	100%	( <i>t</i> <sub>2521</sub> , <i>t</i> <sub>2526</sub> , <i>t</i> <sub>4085</sub> , <i>t</i> <sub>4088</sub> )
	190	3	98.95%	( <i>t</i> <sub>457</sub> , <i>t</i> <sub>3717</sub> , <i>t</i> <sub>4098</sub> )
	188	2	97.91%	( <i>t</i> <sub>2190</sub> , <i>t</i> <sub>3282</sub> )
	184	1	95.83%	( <i>t</i> <sub>3717</sub> )
replace	208	8	100%	( <i>t</i> <sub>306</sub> , <i>t</i> <sub>410</sub> , <i>t</i> <sub>653</sub> , <i>t</i> <sub>1279</sub> , <i>t</i> <sub>1301</sub> , <i>t</i> <sub>3134</sub> , <i>t</i> <sub>4057</sub> , <i>t</i> <sub>4328</sub> )
	207	7	99.51%	( <i>t</i> <sub>309</sub> , <i>t</i> <sub>358</sub> , <i>t</i> <sub>653</sub> , <i>t</i> <sub>776</sub> , <i>t</i> <sub>1279</sub> , <i>t</i> <sub>1795</sub> , <i>t</i> <sub>3248</sub> )
	206	6	99.03%	( <i>t</i> <sub>275</sub> , <i>t</i> <sub>290</sub> , <i>t</i> <sub>1279</sub> , <i>t</i> <sub>1938</sub> , <i>t</i> <sub>2723</sub> , <i>t</i> <sub>2785</sub> )
	205	5	98.55%	( <i>t</i> <sub>426</sub> , <i>t</i> <sub>1279</sub> , <i>t</i> <sub>1898</sub> , <i>t</i> <sub>2875</sub> , <i>t</i> <sub>3324</sub> )
	203	4	97.59%	( <i>t</i> <sub>298</sub> , <i>t</i> <sub>653</sub> , <i>t</i> <sub>3324</sub> , <i>t</i> <sub>5054</sub> )
	200	3	96.15%	( <i>t</i> <sub>2723</sub> , <i>t</i> <sub>2901</sub> , <i>t</i> <sub>3324</sub> )
	195	2	93.75%	( <i>t</i> <sub>358</sub> , <i>t</i> <sub>5387</sub> )
	187	1	89.90%	( <i>t</i> <sub>358</sub> )
schedule	126	3	100%	( <i>t</i> <sub>1403</sub> , <i>t</i> <sub>1559</sub> , <i>t</i> <sub>1564</sub> )
	124	2	98.41%	( <i>t</i> <sub>1570</sub> , <i>t</i> <sub>1595</sub> )
	122	1	96.82%	( <i>t</i> <sub>1572</sub> )
schedule2	119	4	100%	( <i>t</i> <sub>2226</sub> , <i>t</i> <sub>2458</sub> , <i>t</i> <sub>2462</sub> , <i>t</i> <sub>2681</sub> )
	118	3	99.15%	( <i>t</i> <sub>101</sub> , <i>t</i> <sub>1406</sub> , <i>t</i> <sub>2516</sub> )
	117	2	98.31%	( <i>t</i> <sub>2461</sub> , <i>t</i> <sub>2710</sub> )
	116	1	97.47%	( <i>t</i> <sub>1584</sub> )
tcas	54	4	100%	( <i>t</i> <sub>5</sub> , <i>t</i> <sub>1191</sub> , <i>t</i> <sub>1229</sub> , <i>t</i> <sub>1608</sub> )
	53	3	98.14%	( <i>t</i> <sub>13</sub> , <i>t</i> <sub>25</sub> , <i>t</i> <sub>1581</sub> )
	50	2	92.59%	( <i>t</i> <sub>72</sub> , <i>t</i> <sub>1584</sub> )
	44	1	81.48%	( <i>t</i> <sub>217</sub> )
totinfo	117	5	100%	( <i>t</i> <sub>62</sub> , <i>t</i> <sub>118</sub> , <i>t</i> <sub>218</sub> , <i>t</i> <sub>1000</sub> , <i>t</i> <sub>1038</sub> )
	115	4	98.29%	( <i>t</i> <sub>62</sub> , <i>t</i> <sub>118</sub> , <i>t</i> <sub>913</sub> , <i>t</i> <sub>1016</sub> )
	113	3	96.58%	( <i>t</i> <sub>65</sub> , <i>t</i> <sub>216</sub> , <i>t</i> <sub>913</sub> )
	111	2	94.87%	( <i>t</i> <sub>65</sub> , <i>t</i> <sub>919</sub> )
	110	1	94.01%	( <i>t</i> <sub>179</sub> )



# Reduction in the Number of Test Cases

Since we are considering cost 1 for the tests, we can apply an a priori reduction in the original test suite

	$e_1$	$e_2$	$e_3$	...	$e_m$
$t_1$	1	0	0	...	1
$t_2$	1	0	1	...	1
...	...	...	...	...	...
$t_n$	1	1	0	...	0

Test  $t_1$  can be removed

Instance	Original Size	Reduced Size	Elements to cover
printtokens	4130	40	195
printtokens2	4115	28	192
replace	5542	215	208
schedule	2650	4	126
schedule2	2710	13	119
tcas	1608	5	54
totinfo	1052	21	117



# Results with the Reduction

The optimal Pareto Front for the reduced test suite can be found from **200 to 180 000 times faster**

	Original (s)	Reduced (s)
printtokens	3400.74	2.17
printtokens2	3370.44	1.43
replace	1469272.00	345.62
schedule	492.38	0.24
schedule2	195.55	0.27
tcas	73.44	0.33
totinfo	181823.50	0.96



# Software Product Lines Testing

R. Lopez-Herrejon et al., ICSM 2013



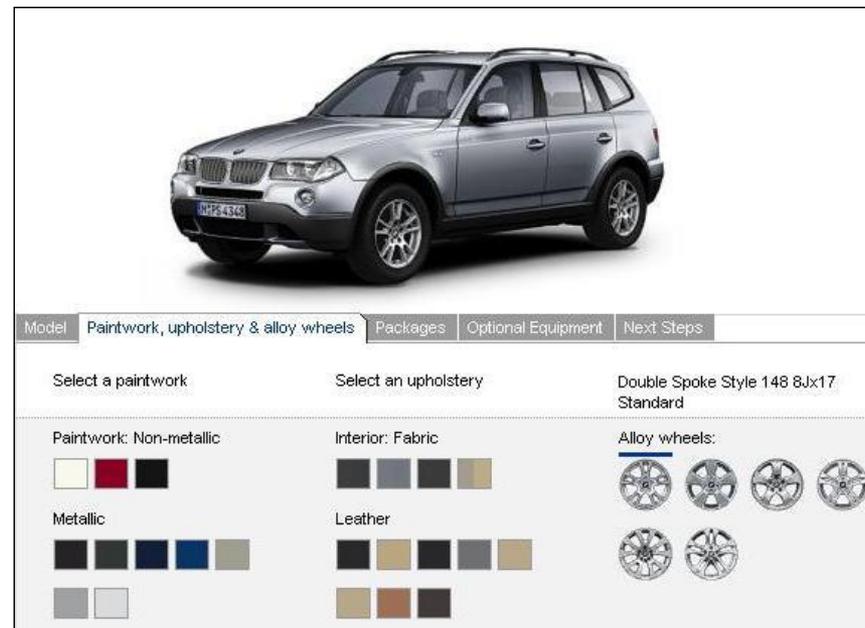
# Software Product Lines

A **product line** is a set of related products developed from a shared set of assets

- The products have similar characteristics
- The products have unique characteristics

## Advantages

- Support customization
- Improves reuse
- Reduce time to market

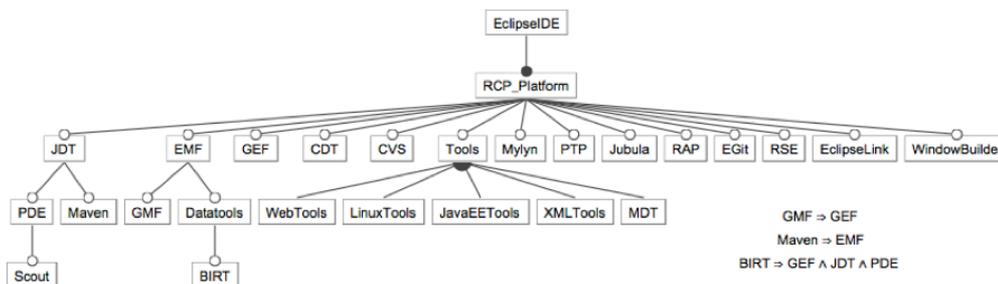




# Software Product Lines

In **Software Product Lines** the product is **Software**

They are modelled using **Feature Models**



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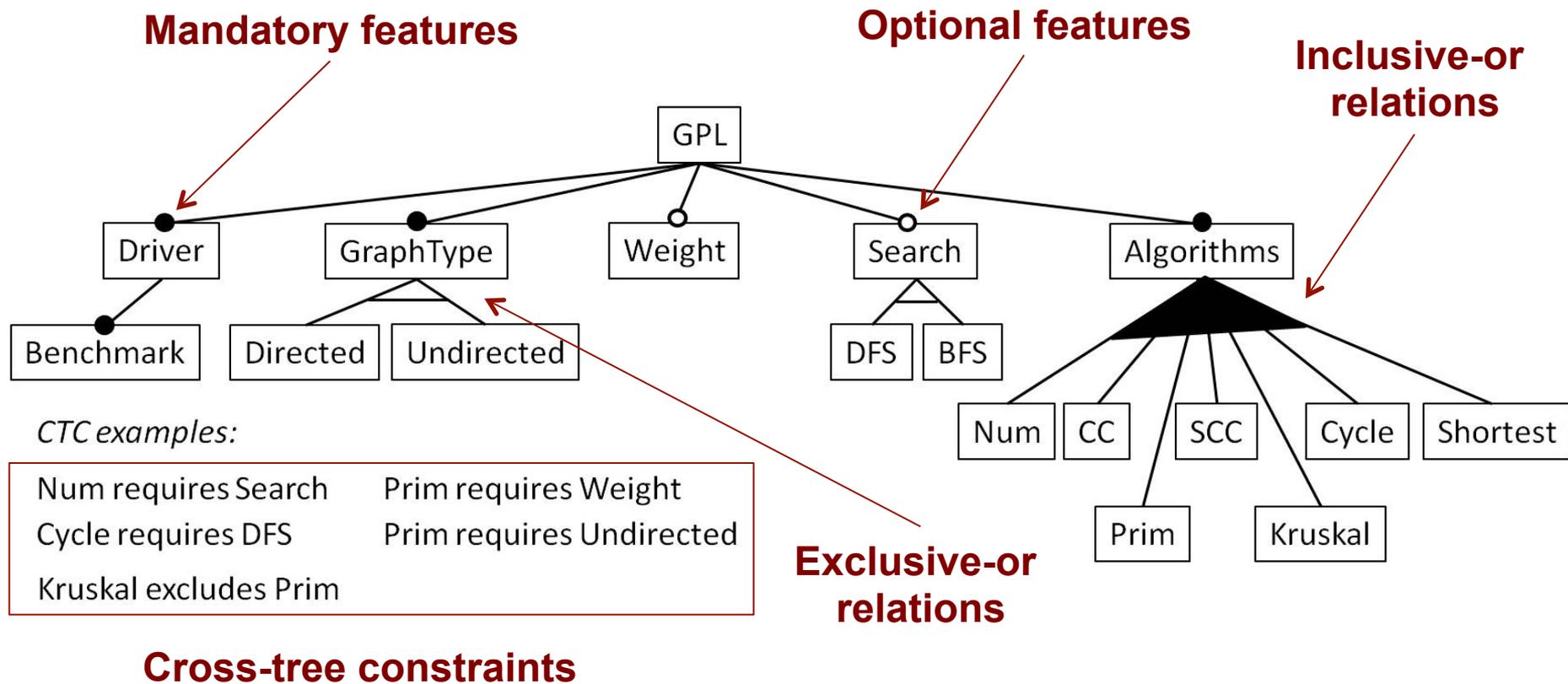
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# Feature Models

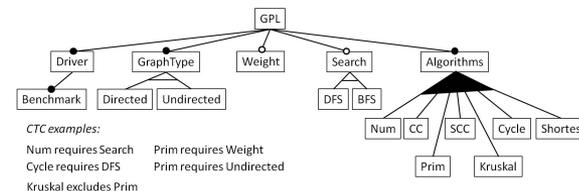


## Graph Product Line Feature Model

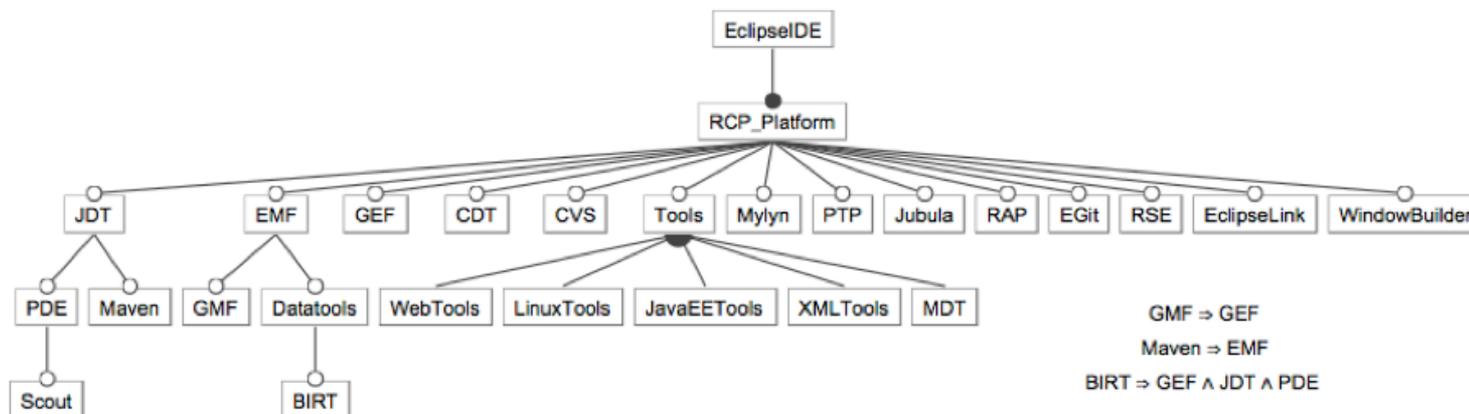


# Testing of Software Product Lines

The GPL Feature Model is small: **73 distinct products**



But the number of products **grows exponentially** with the number of features...



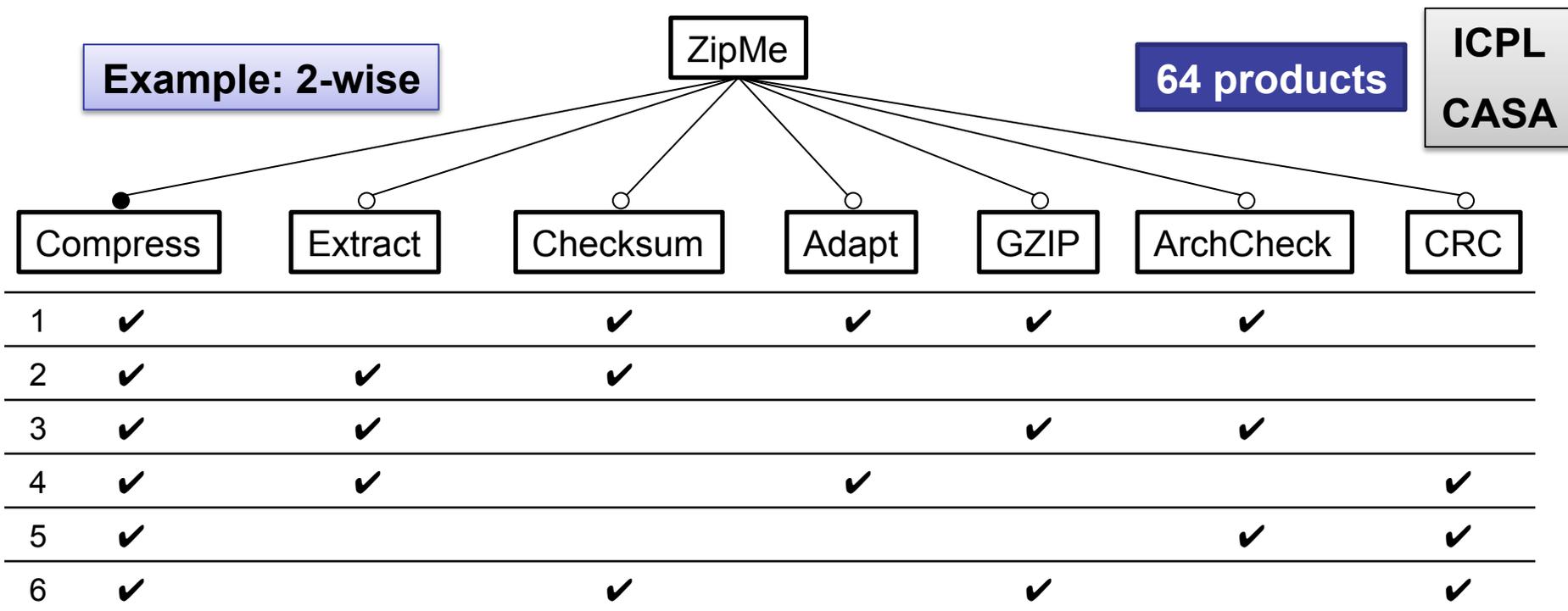
... and testing each particular product is not viable



# Testing of SPLs: Combinatorial Interaction Testing

Assuming each features has been tested in isolation, most of the defects come from the **interaction between features**

**Combinatorial Interaction Testing** consists in selecting the minimum number of products that covers all  $t$ -wise interactions ( **$t$ -wise coverage**).





# Testing of SPLs: Multi-Objective Formulation

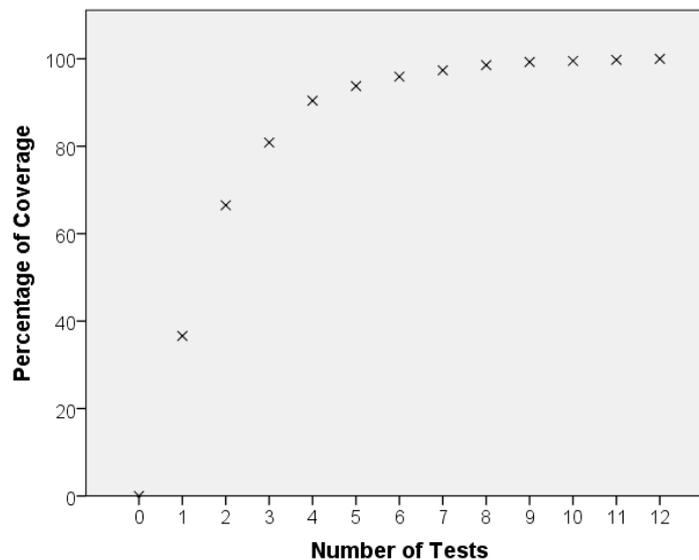
If we don't have the resources to run all the tests, which one to choose?

Multi-objective formulation:

minimize the **number of products**

maximize the **coverage (t-wise interactions)**

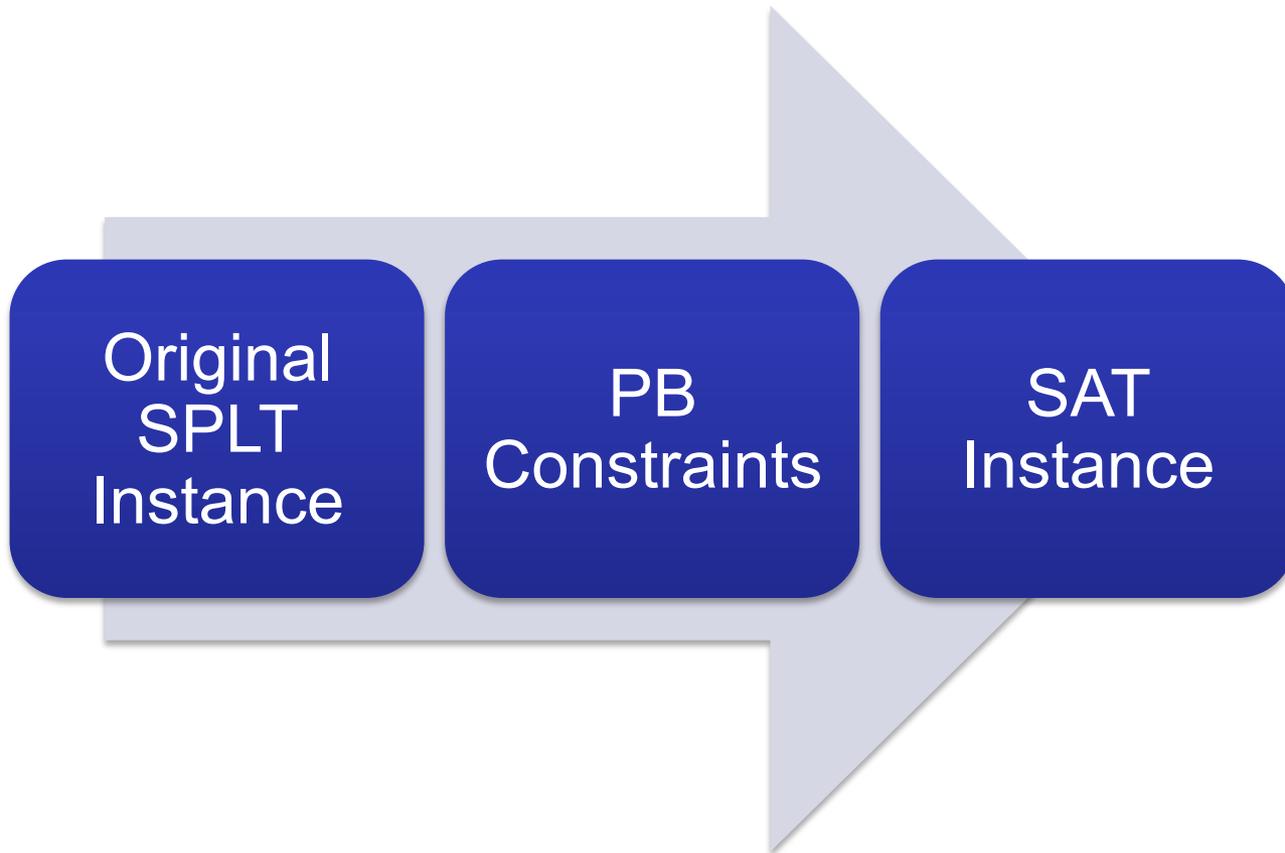
The solution is not anymore a table of products, but a Pareto set



**GPL**  
**2-wise interactions**



# Testing of SPLs: Approach





# Testing of SPLs: Approach

## Modelling SPLT using PseudoBoolean constraints

Variable	Meaning
$x_{p,i}$	Presence of feature $i$ in product $p$
$c_{p,i,j,k}$	Product $p$ covers the pair $(i, j)$ with signature $k$
$d_{i,j,k}$	The pair $(i, j)$ with signature $k$ is covered by some product

$k$  takes values 0, 1, 2 and 3.

**All the variables are boolean  $\{0,1\}$**

**The values of the signature are:**

- **00 (both unselected)**
- **10 (only first selected)**
- **01 (only second selected)**
- **11 (both selected)**



# Testing of SPLs: Approach

## Equations of the model

- For each product  $p$ 
  - Constraints imposed by the Feature Model
- For each product  $p$  and pair of features  $i$  and  $j$

$$2c_{p,i,j,3} \leq x_{p,i} + x_{p,j} \leq 1 + c_{p,i,j,3}$$

$$2c_{p,i,j,2} \leq x_{p,i} + (1 - x_{p,j}) \leq 1 + c_{p,i,j,3}$$

$$2c_{p,i,j,1} \leq (1 - x_{p,i}) + x_{p,j} \leq 1 + c_{p,i,j,3}$$

$$2c_{p,i,j,0} \leq (1 - x_{p,i}) + (1 - x_{p,j}) \leq 1 + c_{p,i,j,3}$$



# Testing of SPLs: Approach

## Equations of the model (cont.)

- For each pair of features  $i$  and  $j$  and signature  $k$

$$d_{i,j,k} \leq \sum_p c_{p,i,j,k} \leq n d_{i,j,k}$$

- $n$  is the number of products
- Objective: maximize coverage

$$\max : \sum_{i,j,k} d_{i,j,k}$$



# Testing of SPLs: Approach

---

**Algorithm 1** Algorithm for obtaining the optimal Pareto set.

---

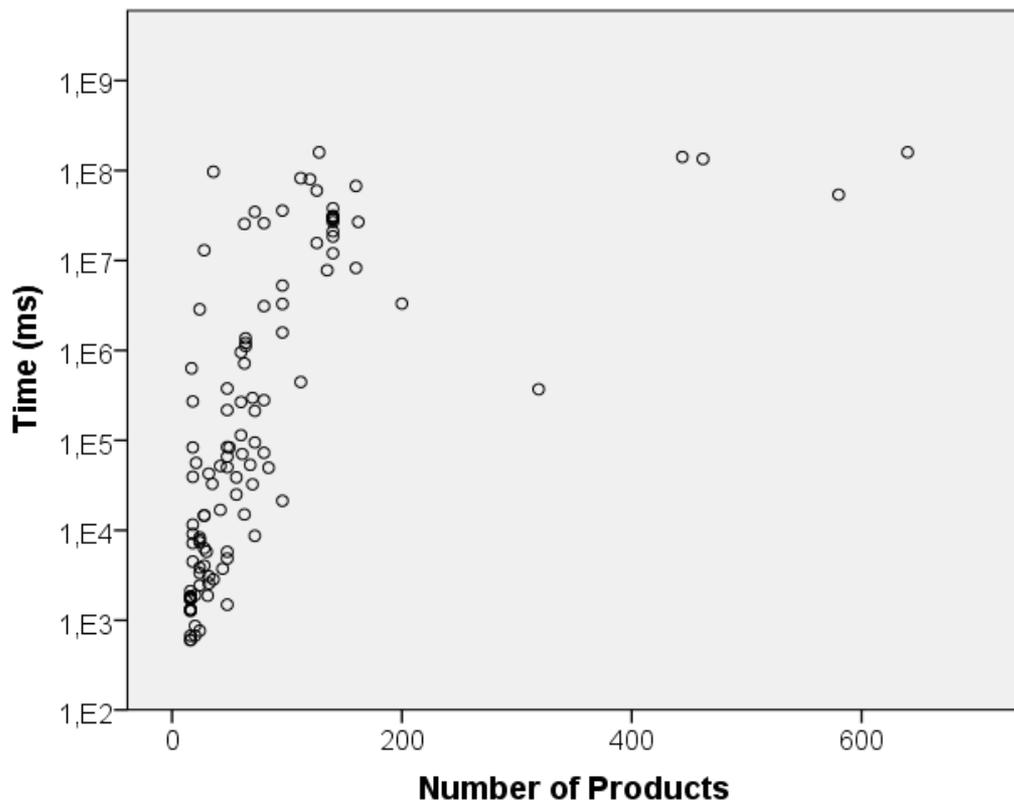
```
optimal_set  $\leftarrow$   $\{\emptyset\}$ ;  
cov[0]  $\leftarrow$  0;  
cov[1]  $\leftarrow$   $C_2^f$ ;  
sol  $\leftarrow$  arbitraryValidSolution(fm);  
i  $\leftarrow$  1;  
while cov[i]  $\neq$  cov[i - 1] do  
    optimal_set  $\leftarrow$  optimal_set  $\cup$  {sol};  
    i  $\leftarrow$  i + 1;  
    m  $\leftarrow$  prepareMathModel(fm,i);  
    sol  $\leftarrow$  solveMathModel(m);  
    cov[i]  $\leftarrow$  |sol|;  
end while
```

---



# Testing of SPLs: Results

Experiments on **118 feature models** taken from  
**SPLIT repository** (<http://www.splot-research.org>)  
**SPL Conqueror** (<http://www.witi.cs.uni-magdeburg.de/~nsiegmun/SPLConqueror/>)



**16 to 640 products**

**Intel Core2 Quad Q9400**  
**2.66 GHz, 4 GB**



# Prioritized Pairwise Combinatorial Interaction Testing

J. Ferrer et al., GECCO 2012

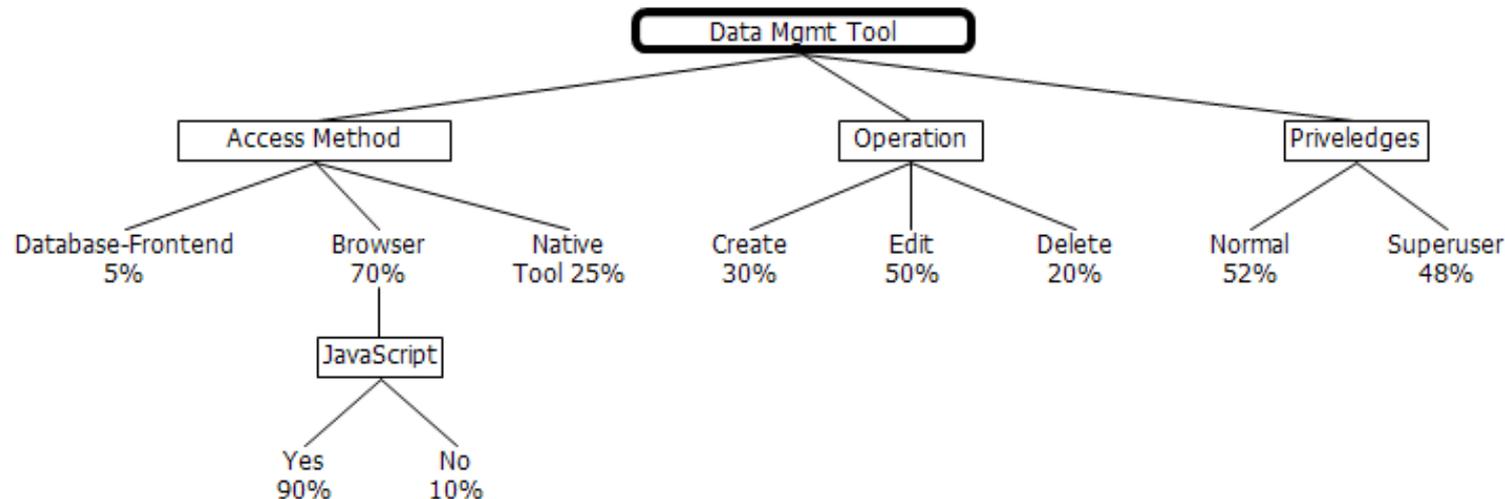


# Combinatorial Interaction Testing

The tester identifies the relevant test aspects (*parameters*) and defines corresponding classes (*parameter values*)

A test case is a set of  $n$  values, one for each parameter

A kind of **functional (black-box)** testing





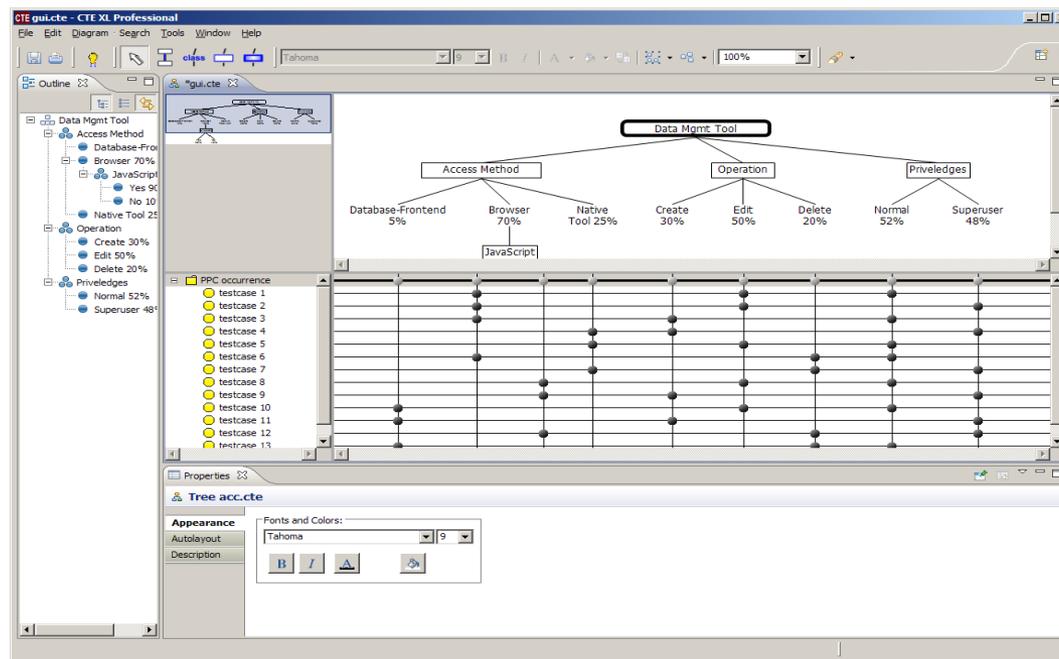
# Prioritized Combinatorial Interaction Testing

The coverage criterion will determine the **degree of parameter interaction**

The coverage criterion is defined by its **strength  $t$  ( $t$ -wise)**

In prioritized CIT, **each  $t$ -tuple has a weight that measures the importance**

Tool Support: **CTE XL**





# Coverage

## Each Used Coverage (EUC)

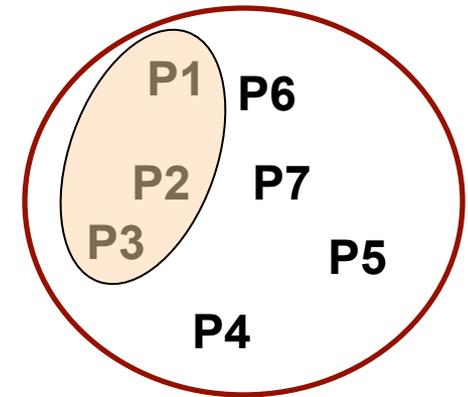
$$EUC = \frac{\text{number of covered class pairs}}{\text{number of coverable class pairs}}$$

$$EUC = 3 / 7 = 0.43$$

## Weight Coverage (WC)

$$WC = \frac{\text{sum of weights of covered class pairs}}{\text{sum of weights of all coverable class pairs}}$$

$$WC = (0.20 + 0.25 + 0.15) / 0.9 = 0.66$$



Pair	Weight
P1	0.20
P2	0.25
P3	0.15
P4	0.10
P5	0.10
P6	0.05
P7	0.05
$\sum P_i$	0.9



# Coverage: example

#	Access Method	Operation	Priv.	EUC	WC
1	Browser (with JavaScript)	Edit	Normal	0.12	0.30
2	Browser (with JavaScript)	Edit	Superuser	0.19	0.48
3	Browser (with JavaScript)	Create	Normal	0.27	0.60
4	Native Tool	Create	Superuser	0.38	0.71
5	Native Tool	Edit	Normal	0.50	0.80
6	Browser (with JavaScript)	Delete	Normal	0.58	0.88
7	Native Tool	Delete	Superuser	0.62	0.92
8	Browser (no JavaScript)	Edit	Normal	0.69	0.94
9	Browser (no JavaScript)	Create	Superuser	0.77	0.96
10	Database-Frontend	Edit	Normal	0.85	0.98
11	Database-Frontend	Create	Superuser	0.92	0.99
12	Browser (no JavaScript)	Delete	Superuser	0.96	0.99
13	Database-Frontend	Delete	Normal	1.00	1.00

30% weight  
coverage with  
one test case

**With the weight  
coverage we cover  
most important  
interactions of  
components in the  
first test cases**



# Coverage: example

#	Access Method	Operation	Priv.	EUC	WC
1	Browser (with JavaScript)	Edit	Normal	0.12	0.30
2	Browser (with JavaScript)	Edit	Superuser	0.19	0.48
3	Browser (with JavaScript)	Create	Normal	0.27	0.60
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9	Browser (no JavaScript)	Create	Superuser	0.77	0.96
10	Database-Frontend	Edit	Normal	0.85	0.98
11	Database-Frontend	Create	Superuser	0.92	0.99
12	Browser (no JavaScript)	Delete	Superuser	0.96	0.99
13	Database-Frontend	Delete	Normal	1.00	1.00

60% weight  
coverage with  
only three  
test cases

With the weight  
coverage we cover  
most important  
interactions of  
components in the  
first test cases



# Coverage: example

#	Access Method	Operation	Priv.	EUC	WC
1	Browser (with JavaScript)	Edit	Normal	0.12	0.30
2	Browser (with JavaScript)	Edit	Superuser	0.19	0.48
3	Browser (with JavaScript)	Create	Normal	0.27	0.60
4	Native Tool	Create	Superuser	0.38	0.71
5	Native Tool	Edit	Normal	0.50	0.80
6	Browser (with JavaScript)	Delete	Normal	0.58	0.88
7	Native Tool	Delete	Superuser	0.62	0.92
8	Browser (no JavaScript)	Edit	Normal	0.69	0.94
9	Browser (no JavaScript)	Create	Superuser	0.77	0.96
10	Database-Frontend	Edit	Normal	0.85	0.98
11	Database-Frontend	Create	Superuser	0.92	0.99
12	Browser (no JavaScript)	Delete	Superuser	0.96	0.99
13	Database-Frontend	Delete	Normal	1.00	1.00

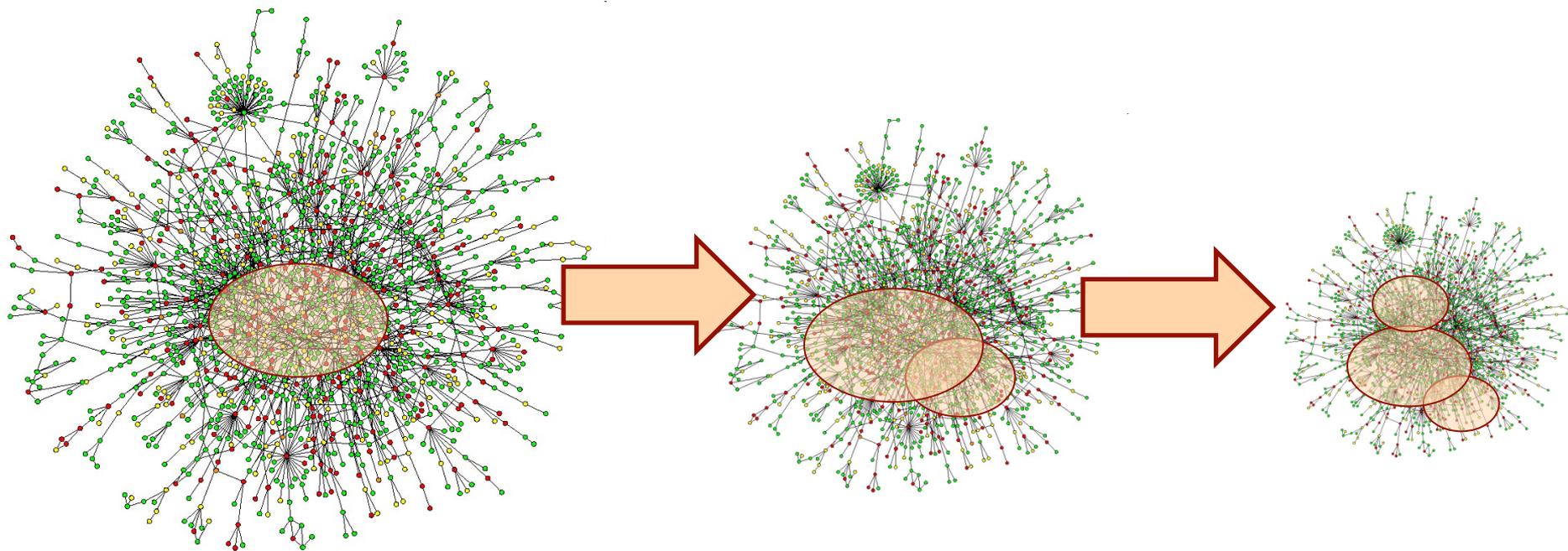
92% weight  
coverage with  
just seven  
test cases

The six less  
important test  
cases just  
suppose 8%



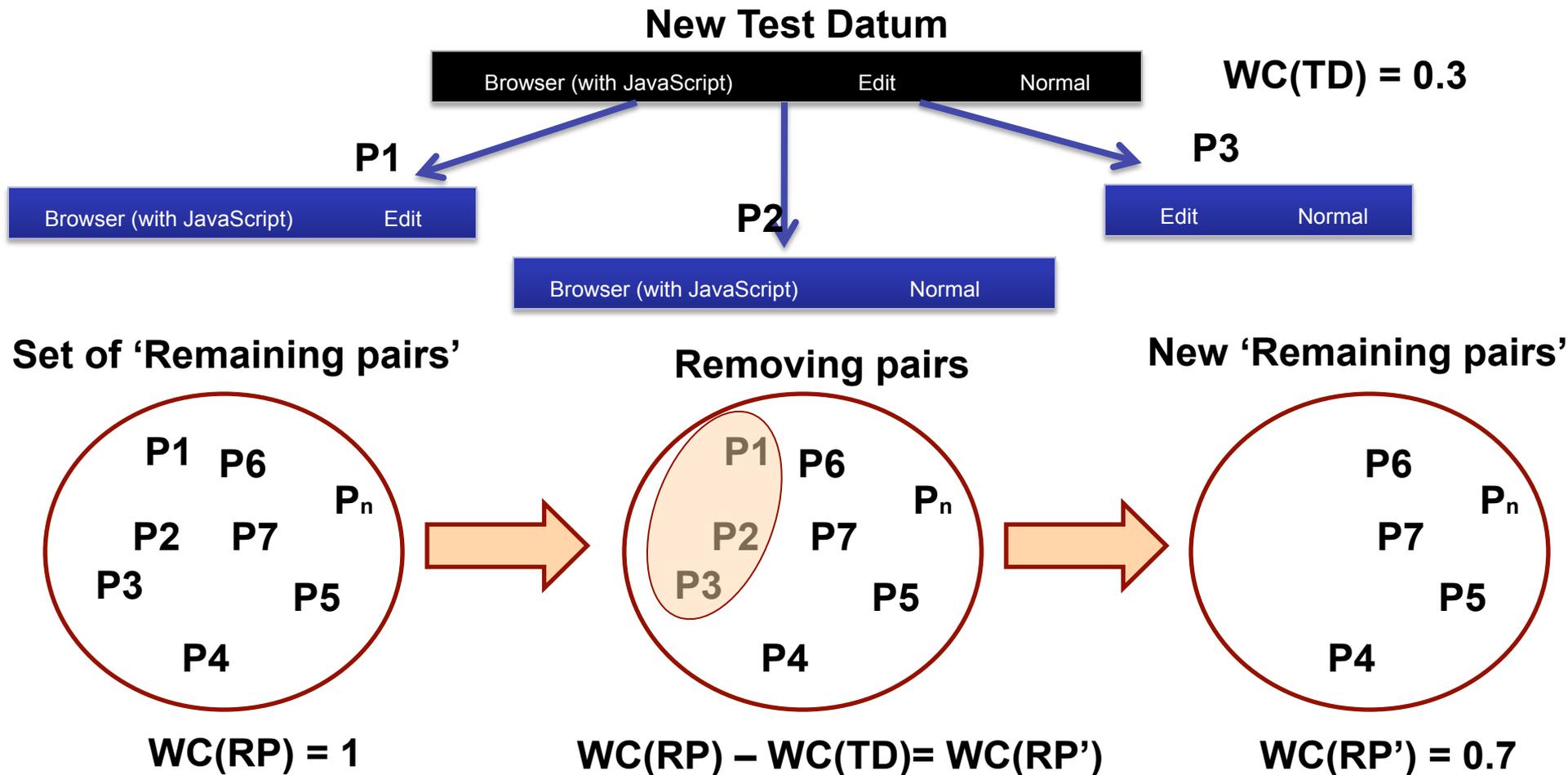
# Proposal: Genetic Solver

**GS is a constructive algorithm that reduces the problem step by step  
It constructs the solution by generating the best test datum at a time**





# Proposal: Genetic Solver





# Results: Experimental Evaluation

Set of benchmarks and distributions proposed by Bryce and Colbourn.

Scenario	# Classes	Distribution	Description
S1	$3^4$	D1 (equal weights)	All classes have the same weight
S2	$10^{20}$	D2 (50/50 split)	Half of the weight for each classification are set to 0.9, the other half to 0.1
S3	$3^{100}$		
S4	$10^{19^1} 8^{17^1} 6^{15^1} 4^{13^1} 2^1$	D3 ( $1/vmax^2$ split)	All weights of classes for a classification are equal to $1/vmax^2$ , where $vmax$ is the number of classes associated with the classification.
S5	$8^2 7^2 6^2 2^4$		
S6	$15^1 10^5 5^1 4^1$		
S7	$3^{50} 2^{50}$	D4 (random)	Weights are randomly distributed
S8	$20^2 10^2 3^{100}$		



# Results: Comparison with PPC and PPS (B&M)

We compare 8 scenarios, 4 distributions, and different coverage values

- Coverage values: 25%, 50%, 66%, 75%, 90%, 95%, and 99%

GS is the best in 6 out of 8 scenarios

GS is the best for all distributions

Times one algorithm is better than the others

Scenario	GS	PPC	PPS
S1	0	0	12
S2	8	18	0
S3	9	3	0
S4	14	9	1
S5	13	6	3
S6	24	1	0
S7	5	2	0
S8	19	6	-
<b>Total</b>	<b>92</b>	<b>45</b>	<b>19</b>

Times a significant difference between GS and the others exists

Distribution	PPC		PPS	
D1-GS	28↑	10↓	29↑	8↓
D2-GS	26↑	9↓	42↑	3↓
D3-GS	19↑	10↓	29↑	8↓
D4-GS	22↑	6↓	41↑	4↓
<b>Total</b>	<b>95↑</b>	<b>35↓</b>	<b>141↑</b>	<b>23↓</b>



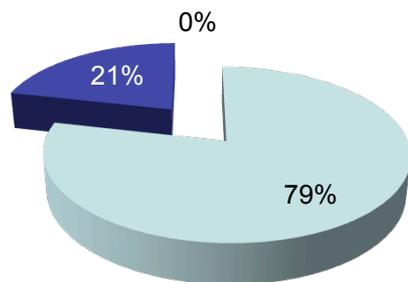
# Results: Comparison with PPC and PPS (B&M)

We compared the algorithm focused on different coverage values

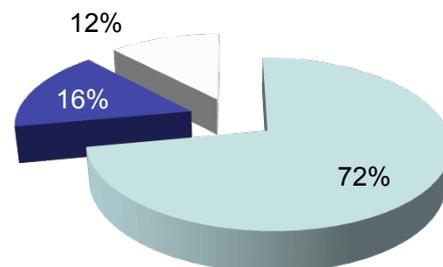
It is important to obtain the best results for intermediate values of coverage

The GS always performs better than the others for these coverage values

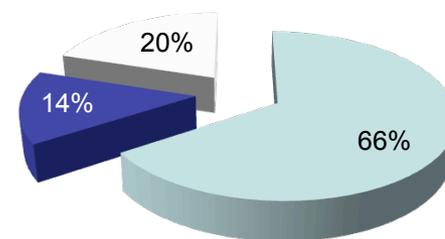
### 50% Coverage



### 75% Coverage



### 100% Coverage



■ GS    ■ PPC    ■ PPS



# Results: Comparison with DDA and BDD

Comparison among GS and the state-of-the-art algorithms:

**Deterministic Density Algorithm (DDA):** Bryce and Colbourn (2006)

**Binary Decision Diagrams (BDD):** Salecker et al. (2011)

GS is the best in 7 out of 8 scenarios. It draws on the scenario S1.

GS is the best in 3 out of 4 distributions. It draws in D1 with DDA.

Times one algorithm is better  
than the others

Scenario	GS	DDA	BDD
S1	2	2	2
S2	11	0	0
S3	6	1	0
S4	8	0	2
S5	7	3	0
S6	11	0	0
S7	3	0	1
S8	3	1	0
<b>Totals</b>	<b>51</b>	<b>7</b>	<b>5</b>

Times there exist significant  
differences between the algorithms

Distribution	DDA		BDD	
D1-GS	7↑	7↓	15↑	5↓
D2-GS	10↑	1↓	16↑	2↓
D3-GS	16↑	0↓	18↑	1↓
D4-GS	16↑	2↓	22↑	1↓
<b>Totals</b>	<b>49↑</b>	<b>10↓</b>	<b>71↑</b>	<b>9↓</b>

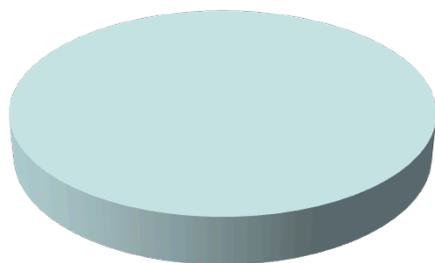


# Results: Comparison with DDA and BDD

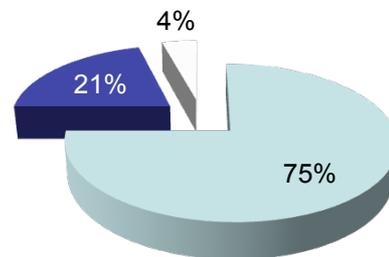
**GS always performs better than the state-of-the-art algorithms**

**It is always better than the other algorithms for all scenarios and distributions for 50% weight coverage.**

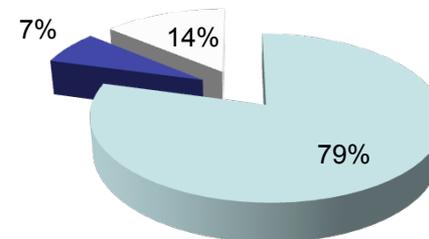
### 50% Coverage



### 75% Coverage



### 100% Coverage



■ GS    ■ DDA    ■ BDD



# Testing Complexity

J. Ferrer et al., Inf. & Soft. Tech. 2013



# Motivation

**How difficult is to test the Software using  
automatic test data generation?**

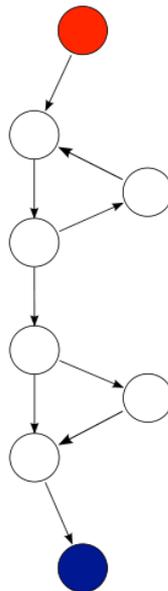
**Can we estimate the difficulty  
analyzing the program?**

**This kind of measure would be useful  
to estimate the testing costs**



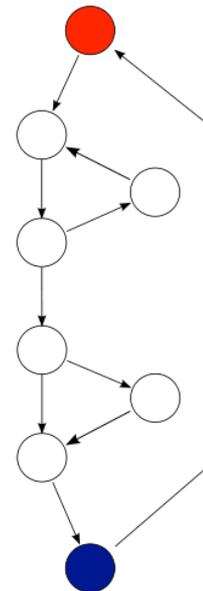
# McCabe's Cyclomatic Complexity

$$v(G) = E - N + 2$$



One entry and exit node

$$v(G) = E - N + 1$$



Strongly connected graph

## What does it mean?

- Number of linearly independent paths of the graph
- Linearly independent paths find errors with high probability
- The measure is an estimation of the cost of testing the code



# Other Measures

- Lines of Code (*LOC*)
- Source Lines of Code (*SLOC*)
- Lines of Code Equivalent (*LOCE*)
- Total Number of Disjunctions (*TND<sub>j</sub>*)
- Total Number of Conjunctions (*TNC<sub>j</sub>*)
- Total Number of Equalities (*TNE*)
- Total Number of Inequalities (*TNI*)
- Total Number of Decisions (*TND*)
- Number of Atomic Conditions per Decision (*CpD*)
- Nesting Degree (*N*)
- Halstead's Complexity (*HD*)
- McCabe's Cyclomatic Complexity (*MC*)
- Halstead Length (HL):  $N = N1 + N2$
- Halstead Vocabulary (HV):  $n = n1 + n2$
- Halstead Volume (HVL):  $V = N * \log_2 n$
- Halstead Difficulty (HD):  $HD = \frac{n1}{2} * \frac{N2}{n2}$
- Halstead Level (HLV):  $L = \frac{1}{HD}$
- Halstead Effort (HE):  $E = HD * V$
- Halstead Time (HT):  $T = \frac{E}{18}$
- Halstead Bugs (HB):  $B = \frac{V}{3000}$
- Density of Decisions (DD) =  $TND/LOC$ .
- Density of LOCE (DLOCE) =  $LOCE/LOC$ .

## Legend

- $n1$  = the number of distinct operators
- $n2$  = the number of distinct operands
- $N1$  = the total number of operators
- $N2$  = the total number of operands



# Our Proposal: Branch Coverage Expectation

```

/* BB1 */
if (x < 0) || (y < 2)
{
    /* BB2 */
    y=5;
}
else
{
    /* BB3 */
    x=y-3;
    while (y > 5) || (x > 5)
    {
        /* BB4 */
        y=x-5;
    }
    /* BB5 */
    x=x-3;
}
/* BB6 */

```

$$P(c1 \&\& c2) = P(c1) * P(c2),$$

$$P(c1 || c2) = P(c1) + P(c2) - P(c1) * P(c2),$$

$$P(\neg c1) = 1 - P(c1),$$

$$P(a < b) = \frac{1}{2},$$

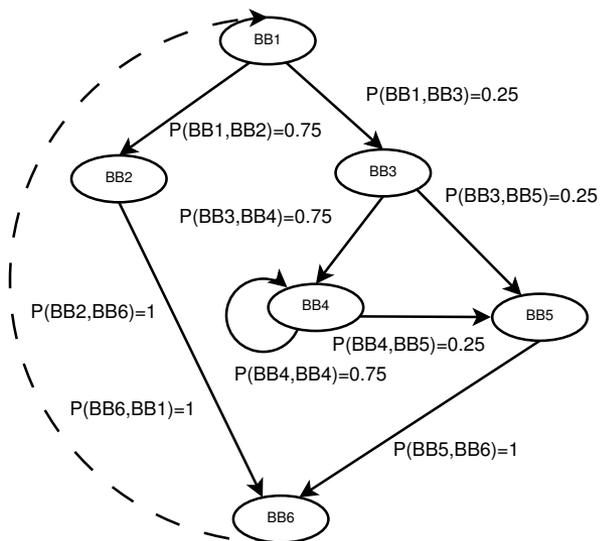
$$P(a \leq b) = \frac{1}{2},$$

$$P(a > b) = \frac{1}{2},$$

$$P(a \geq b) = \frac{1}{2},$$

$$P(a == b) = q,$$

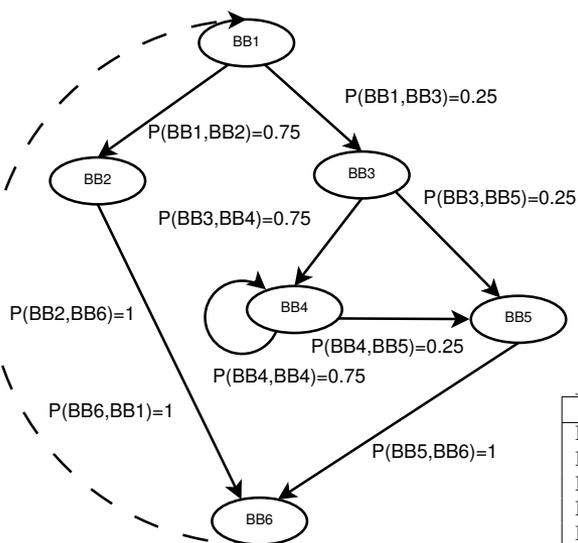
$$P(a != b) = 1 - q,$$





# Our Proposal: Branch Coverage Expectation

## Markov Chain



Compute  
stationary  
distribution

$$\pi^T P = \pi^T,$$

$$\pi^T \mathbf{1} = 1.$$

	Stationary Probabilities $\pi_i$	Frequency of Appearance $E[BB_i]$
BB1	0.2500	1.00
BB2	0.1875	0.75
BB3	0.0625	0.25
BB4	0.1875	0.75
BB5	0.0625	0.25
BB6	0.2500	1.00

Expected BB executions in 1 run

Expected branch execution in 1 run

$$E[BB_i, BB_j] = E[BB_i] * P_{ij}$$

$$E[BB_i] = \frac{\pi_i}{\pi_1},$$



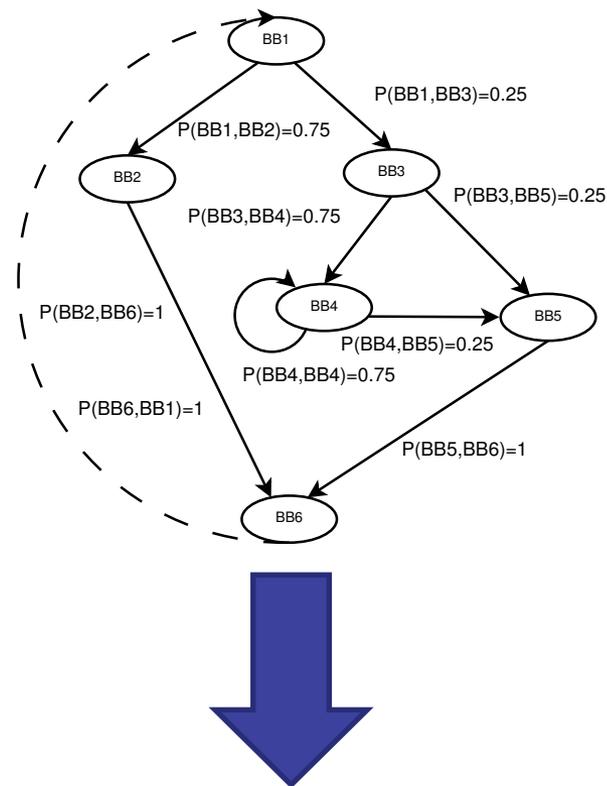
# Our Proposal: Branch Coverage Expectation

## Most difficult branches to cover

$$A = \left\{ (i, j) \mid E[BB_i, BB_j] < \frac{1}{2} \right\}.$$

## Branch Coverage Expectation

$$BCE = \frac{1}{|A|} \sum_{(i,j) \in A} E[BB_i, BB_j].$$



$$BCE = \frac{E[BB_1, BB_3] + E[BB_3, BB_4] + E[BB_3, BB_5] + E[BB_4, BB_5] + E[BB_5, BB_6]}{5} = \frac{\frac{1}{4} + \frac{3}{16} + \frac{1}{16} + \frac{3}{16} + \frac{1}{4}}{5} = \frac{3}{16} = 0.1875.$$



# Correlation Study with All the Measures

Table A.10: The correlation coefficients among all the measures analyzed in the benchmark 100%CP

	HD	MC	LOCE	N	DD	DLOCE	BCE	LOC	SLOC	TNDj	TNCj	TNE	TNI	TND	CpD	HL	HV	HVL	HLV	HE	HT	HB	ES	GA	RND
HD	-	0.796	0.786	-0.108	0.052	-0.035	0.285	0.932	0.853	0.742	0.731	0.644	0.639	0.799	0.454	0.870	0.842	0.864	1.0	0.920	0.920	0.864	0.070	-0.101	0.077
MC	0.796	-	0.965	0.266	0.519	0.408	0.025	0.805	0.962	0.925	0.934	0.829	0.811	0.985	0.524	0.976	0.969	0.977	-0.796	0.954	0.954	0.977	-0.150	-0.226	-0.074
LOCE	0.786	0.965	-	0.344	0.515	0.474	-0.038	0.796	0.974	0.884	0.882	0.822	0.789	0.976	0.501	0.945	0.938	0.945	-0.786	0.921	0.921	0.945	-0.186	-0.251	-0.133
N	-0.108	0.266	0.344	-	0.765	0.877	-0.540	-0.207	0.180	0.235	0.240	0.311	0.234	0.276	0.136	0.138	0.127	0.139	0.108	0.089	0.089	0.139	-0.543	-0.381	-0.434
DD	0.052	0.519	0.515	0.765	-	0.912	-0.377	-0.043	0.405	0.449	0.489	0.485	0.437	0.538	0.283	0.368	0.367	0.372	-0.052	0.302	0.302	0.372	-0.439	-0.304	-0.311
DLOCE	-0.035	0.408	0.474	0.877	0.912	-	-0.485	-0.132	0.336	0.352	0.380	0.410	0.353	0.418	0.217	0.270	0.258	0.271	0.035	0.208	0.208	0.271	-0.504	-0.345	-0.397
BCE	0.285	0.025	-0.038	-0.540	-0.377	-0.485	-	0.307	0.081	0.065	0.008	-0.124	0.009	0.017	0.078	0.121	0.129	0.120	-0.285	0.159	0.159	0.120	0.510	0.375	0.534
LOC	0.932	0.805	0.796	-0.207	-0.043	-0.132	0.307	-	0.879	0.753	0.730	0.634	0.646	0.810	0.419	0.891	0.892	0.890	-0.932	0.910	0.910	0.890	0.136	-0.053	0.120
SLOC	0.853	0.962	0.974	0.180	0.405	0.336	0.081	0.879	-	0.884	0.878	0.794	0.778	0.973	0.492	0.975	0.970	0.975	-0.853	0.960	0.960	0.975	-0.091	-0.194	-0.050
TNDj	0.742	0.925	0.884	0.235	0.449	0.352	0.065	0.753	0.884	-	0.773	0.813	0.719	0.897	0.515	0.919	0.908	0.919	-0.742	0.900	0.900	0.919	-0.119	-0.175	-0.036
TNCj	0.731	0.934	0.882	0.240	0.489	0.380	0.008	0.730	0.878	0.773	-	0.734	0.806	0.905	0.497	0.913	0.901	0.913	-0.731	0.895	0.895	0.913	-0.158	-0.235	-0.072
TNE	0.644	0.829	0.822	0.311	0.485	0.410	-0.124	0.634	0.794	0.813	0.734	-	0.618	0.822	0.435	0.798	0.785	0.797	-0.644	0.779	0.779	0.797	-0.272	-0.279	-0.207
TNI	0.639	0.811	0.789	0.234	0.437	0.353	0.009	0.646	0.778	0.719	0.806	0.618	-	0.799	0.439	0.794	0.791	0.795	-0.639	0.774	0.774	0.795	-0.121	-0.201	-0.095
TND	0.799	0.985	0.976	0.276	0.538	0.418	0.017	0.810	0.973	0.897	0.905	0.822	0.799	-	0.503	0.961	0.959	0.962	-0.799	0.935	0.935	0.962	-0.147	-0.226	-0.082
CpD	0.454	0.524	0.501	0.136	0.283	0.217	0.078	0.419	0.492	0.515	0.497	0.435	0.439	0.503	-	0.524	0.518	0.523	-0.454	0.514	0.514	0.523	-0.089	-0.132	0.035
HL	0.870	0.976	0.945	0.138	0.368	0.270	0.121	0.891	0.975	0.919	0.913	0.798	0.794	0.961	0.524	-	0.991	1.0	-0.870	0.989	0.989	1.0	-0.071	-0.180	-0.012
HV	0.842	0.969	0.938	0.127	0.367	0.258	0.129	0.892	0.970	0.908	0.901	0.785	0.791	0.959	0.518	0.991	-	0.994	-0.842	0.971	0.971	0.994	-0.061	-0.172	-0.003
HVL	0.864	0.977	0.945	0.139	0.372	0.271	0.120	0.890	0.975	0.919	0.913	0.797	0.795	0.962	0.523	1.0	0.994	-	-0.864	0.987	0.987	1.0	-0.072	-0.181	-0.011
HLV	-1.0	-0.796	-0.786	0.108	-0.052	0.035	-0.285	-0.932	-0.853	-0.742	-0.731	-0.644	-0.639	-0.799	-0.454	-0.870	-0.842	-0.864	-	-0.920	-0.920	-0.864	-0.070	0.101	-0.077
HE	0.920	0.954	0.921	0.089	0.302	0.208	0.159	0.910	0.960	0.900	0.895	0.779	0.774	0.935	0.514	0.989	0.971	0.987	-0.920	-	1.0	0.987	-0.046	-0.168	0.006
HT	0.920	0.954	0.921	0.089	0.302	0.208	0.159	0.910	0.960	0.900	0.895	0.779	0.774	0.935	0.514	0.989	0.971	0.987	-0.920	1.0	-	0.987	-0.046	-0.168	0.006
HB	0.864	0.977	0.945	0.139	0.372	0.271	0.120	0.890	0.975	0.919	0.913	0.797	0.795	0.962	0.523	1.0	0.994	1.0	-0.864	0.987	0.987	-	-0.072	-0.181	-0.011
ES	0.070	-0.150	-0.186	-0.543	-0.439	-0.504	0.120	0.136	-0.091	-0.119	-0.158	-0.272	-0.121	-0.147	-0.089	-0.071	-0.061	-0.072	-0.070	-0.046	-0.046	-0.072	-	0.365	0.445
GA	-0.101	-0.226	-0.251	-0.381	-0.304	-0.345	0.375	-0.053	-0.194	-0.175	-0.235	-0.279	-0.201	-0.226	-0.132	-0.180	-0.172	-0.181	0.101	-0.168	-0.168	-0.181	0.365	-	0.403
RND	0.077	-0.074	-0.133	-0.434	-0.311	-0.397	0.534	0.120	-0.050	-0.036	-0.072	-0.207	-0.095	-0.082	0.035	-0.012	-0.003	-0.011	-0.077	0.006	0.006	-0.011	0.445	0.403	-

Study over  
2600 programs

Table A.11: The correlation coefficients among all the measures analyzed in the benchmark -100%CP

	HD	MC	LOCE	N	DD	DLOCE	BCE	LOC	SLOC	TNDj	TNCj	TNE	TNI	TND	CpD	HL	HV	HVL	HLV	HE	HT	HB	ES	GA	RND
HD	-	0.698	0.359	-0.062	0.023	0.014	0.051	0.664	0.648	0.653	0.651	0.557	0.569	0.463	0.441	0.764	0.576	0.747	-1.0	0.872	0.872	0.747	0.069	0.067	0.079
MC	0.698	-	0.571	0.257	0.432	0.351	-0.142	0.472	0.667	0.936	0.937	0.803	0.827	0.718	0.671	0.782	0.762	0.786	-0.698	0.803	0.803	0.786	-0.177	-0.168	-0.173
LOCE	0.359	0.571	-	0.692	0.590	0.833	-0.461	0.414	0.717	0.435	0.432	0.479	0.485	0.814	0.086	0.564	0.503	0.560	-0.359	0.524	0.524	0.560	-0.461	-0.452	-0.476
N	-0.062	0.257	0.692	-	0.708	0.870	-0.575	-0.160	0.190	0.163	0.161	0.229	0.220	0.502	0.031	0.020	0.009	0.019	0.062	-0.007	-0.007	0.019	-0.563	-0.554	-0.589
DD	0.023	0.432	0.590	0.708	-	0.774	-0.426	-0.178	0.280	0.306	0.304	0.385	0.372	0.723	0.026	0.089	0.056	0.087	-0.023	0.070	0.070	0.087	-0.476	-0.473	-0.497
DLOCE	0.014	0.351	0.833	0.870	0.774	-	-	-0.113	0.284	0.247	0.243	0.308	0.291	0.593	0.013	0.096	0.076	0.095	-0.014	0.073	0.073	0.095	-0.577	-0.564	-0.602
BCE	0.051	-0.142	-0.461	-0.575	-0.426	-0.556	-	0.075	-0.143	-0.078	-0.079	-0.200	-0.138	-0.318	0.080	-0.021	-0.006	-0.020	-0.051	0.001	0.001	-0.020	0.714	0.698	0.732
LOC	0.664	0.472	0.414	-0.160	-0.178	-0.113	0.075	-	0.857	0.398	0.397	0.386	0.406	0.494	0.144	0.906	0.821	0.901	-0.664	0.874	0.874	0.901	0.102	0.099	0.116
SLOC	0.648	0.667	0.717	0.190	0.280	0.284	-0.143	0.857	-	0.533	0.532	0.549	0.572	0.834	0.152	0.916	0.813	0.910	-0.648	0.875	0.875	0.910	-0.137	-0.137	-0.137
TNDj	0.653	0.936	0.435	0.163	0.306	0.247	-0.078	0.398	0.533	-	0.849	0.753	0.781	0.555	0.747	0.702	0.697	0.707	-0.653	0.731	0.731	0.707	-0.110	-0.101	-0.102
TNCj	0.651	0.937	0.432	0.161	0.304	0.243	-0.079	0.397	0.532	0.849	-	0.753	0.771	0.551	0.746	0.702	0.697	0.707	-0.651	0.731	0.731	0.707	-0.116	-0.107	-0.111
TNE	0.557	0.803	0.479	0.229	0.385	0.308	-0.200	0.386	0.549	0.753	0.753	-	0.623	0.600	0.544	0.633	0.619	0.636	-0.557	0.646	0.646	0.636	-0.278	-0.270	-0.270
TNI	0.569	0.827	0.485	0.220	0.372	0.291	-0.138	0.406	0.572	0.771	0.771	0.623	-	0.619	0.559	0.658	0.645	0.662	-0.569	0.671	0.671	0.662	-0.207	-0.198	-0.204
TND	0.463	0.718	0.814	0.502	0.723	0.593	-0.318	0.494	0.834	0.555	0.551	0.600	0.619	-	0.132	0.688	0.605	0.683	-0.463	0.648	0.648	0.683	-0.338	-0.336	-0.348
CpD	0.441	0.671	0.086	-0.031	0.026	0.013	0.080	0.144	0.152	0.747	0.746	0.544	0.559	0.132	-	0.394	0.436	0.402	-0.441	0.437	0.437	0.402	0.026	0.026	0.031
HL	0.764	0.782	0.564	0.020	0.089	0.096	-0.021	0.906	0.916	0.702	0.702	0.633	0.658	0.688	0.394	-	0.932	0.999	-0.764	0.980	0.980	0.999	-0.021	-0.018	-0.010
HV	0.576	0.762	0.503	0.009	0.056	0.076	-0.006	0.821	0.813	0.697	0.697	0.619	0.645	0.605	0.436	0.932	-	0.946	-0.576	0.874	0.874	0.946	-0.040	-0.030	-0.022
HVL	0.747	0.786	0.560	0.019	0.087	0.095	-0.020	0.901	0.910	0.707	0.707	0.636	0.662	0.683	0.402	0.999	0.946	-	-0.747	0.974	0.974	1.0	-0.023	-0.020	-0.011
HLV	-1.0	-0.698	-0.359	0.062	-0.023	-0.014	-0.051	-0.664	-0.648	-0.653	-0.651	-0.557	-0.569	-0.463	-0.401	-0.764	-0.576	-0.747	-	-0.872	-0.872	-0.747	-0.069	-0.067	-0.079
HE	0.872	0.803	0.524	-0.007	0.070	0.073	0.001	0.874	0.875	0.731	0.731	0.646	0.671	0.648	0.437	0.980	0.874	0.974							



# Correlation with Cov. of an Automatic TD Gen.

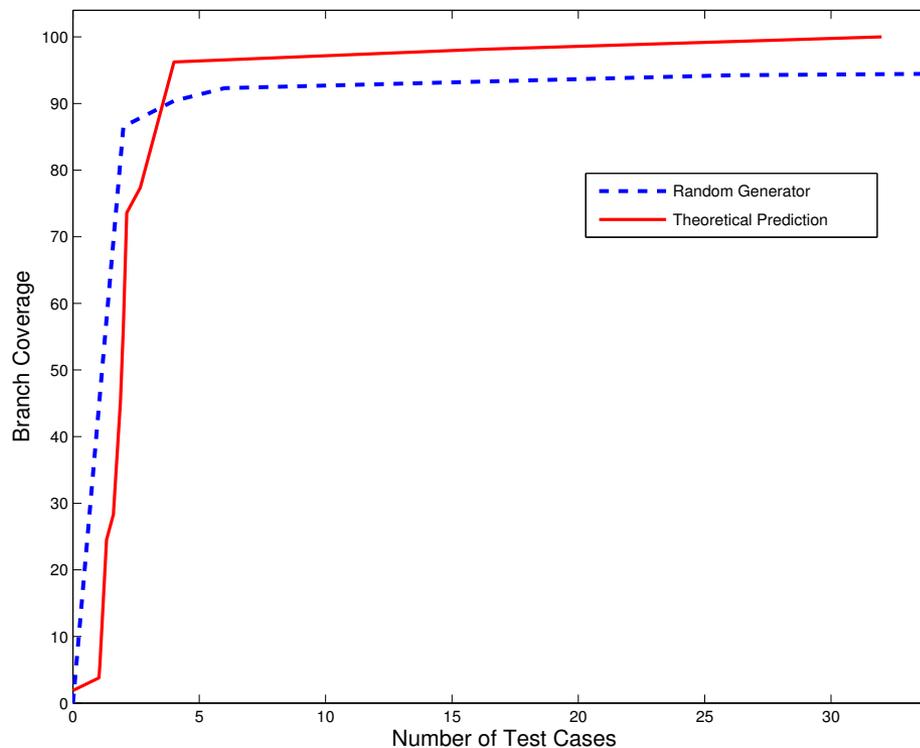
Study over  
2600 programs

	$\tilde{100\%CP}$			$\neg 100\%CP$		
	ES	GA	RND	ES	GA	RND
MC	-0.150	-0.226	-0.074	-0.177	-0.168	-0.173
HD	0.070	-0.101	0.077	0.069	0.067	0.079
LOCE	-0.186	-0.251	-0.133	-0.461	-0.452	-0.476
N	-0.543	-0.381	-0.434	-0.563	-0.554	-0.589
DD	-0.439	-0.304	-0.311	-0.476	-0.473	-0.497
DLOCE	-0.504	-0.345	-0.397	-0.577	-0.564	-0.602
BCE	0.510	0.375	0.534	0.714	0.698	0.732



# Approximated Behaviour of RND

$$f(x) = \left| \left\{ (i, j) \left| \frac{1}{E[BB_i, BB_j]} \leq x \right. \right\} \right|.$$



**Approximated  
number of TCs to  
cover the branch**

# Recent Research on Search Based software Testing



Thanks for your attention !!!

