



# *Emergent Optimization: Design and Applications in Telecommunications and Bioinformatics*

PhD Thesis Dissertation

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UNIVERSIDAD DE MÁLAGA

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Introduction	Fundamentals	Algorithm Proposals and Validation	Real World Applications	Conclusions & Future Work	LENGUAJES Y CIENCIAS DE LA COMPUTACIÓN UNIVERSIDAD DE MÁLAGA
Objectives	Organization				
Object	ives				Part I
Work h	ypothesis:				

<u>I.H:</u> Particle Swarm Optimization is a first class base-line optimizer able of the best performance in modern benchmarking, as well as in present real-world optimization problems

OTHER **METAHEURISTICS** (DE, GA, ES, MTS,...) An ideal approach should have: HYBRIDIZATION **EVOLVABILITY** BENCHMARKING Design and analysis of new SOFTWARE PSO proposals and their PARTICLE SWARM LIBRARIES MULTIOBJECTIVE PROBLEM **OPTIMIZATION** validation on standard **INSTANCES** SOLUTION benchmarks REPRESENTATIONS (CONTINUOUS, BINARY, PARALLEL INTEGER) DISTRIBUTED **REAL WORLD** COMMUNICATION **APPLICATIONS** Application to real world PROTOCOL TUNING IN GENE SELECTION IN problems in different areas of VANETS DNA MICROARRAYS engineering TRAFFIC LIGHTS SIMULATION SIGNAL TIMING



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Nature inspired techniques based on swarm dynamics and search strategies

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- Designed in 1995 by Kennedy and Eberhart
- Inspired on the Nature: Swarm of birds and fish schooling, modeling movements and reactions
- Solutions are encoded as particles that
  - are moved using a velocity equation
  - the velocity depends on the position of other particles

### Popular metaheuristic nowadays

- Fast convergence
- Easy to understand and implement





$$\vec{x}_{i}^{t+1} = \vec{x}_{i}^{t} + \vec{v}_{i}^{t+1}$$
$$\vec{v}_{i}^{t+1} = \omega \cdot v_{i}^{t} + U^{t}[0,\rho] \cdot (\vec{p}_{i}^{t} - \vec{x}_{i}^{t}) + U^{t}[0,\rho] \cdot (\vec{b}_{i}^{t} - \vec{x}_{i}^{t})$$
Individual factor Social factor









### Real world

applications

- PSO Standards 2006, 2007, and 2011
- DE (rand/1)
- GA, SA, ES
- Random Search
- Deterministic SGCP



 $10^{4}$ 

10<sup>5</sup> 10<sup>6</sup>

10<sup>7</sup> 10<sup>8</sup>

10<sup>3</sup>

10







- In PSO, modify the learning procedure to induce an improved performance usually means a reformulation to have a new velocity vector equation
- We have opted for several mechanisms:

Mechanism	Description	Proposals
Hybridization	Using differential evolution operators	DEPSO
Velocity modulation	Constraining velocity to the search range	RPSO-vm
Multi-objective	Using velocity modulation and leader selection from non-dominated set	SMPSO
Neighborhood topology & number of informants	Discovering a quasi-optimal information scheme	<b>PSO</b> 6 ± 2
Interdependency of variables	Hybridizing with local search & range decisions	PSO6-MtsIs
Parallel swarm	Structuring swarms in parallel	PMSO



► Main idea

For each particle, the velocity is updated according to two main influences: **social** and **differential variation** operators

New learning procedure:

$$\vec{v}_{i}^{t+1} = \omega \cdot v_{i}^{t} + F \underbrace{(\vec{x}_{r1}^{t} - \vec{x}_{r2}^{t})}_{(\vec{v}_{r1}^{t} - \vec{x}_{r2}^{t})} + U^{t}[0,\rho] \cdot \underbrace{(\vec{b}_{i}^{t} - \vec{x}_{i}^{t})}_{(\vec{v}_{r1}^{t} - \vec{v}_{r2}^{t})}$$

**Differential variation** 

Social factor

Crossover and trial selection are applied as in DE



Introduction	Fundamentals	Algorithm Prop and Validati	osals on	Real World Applications	Conclusio Future W	ns & Cork	LENGUAJES CIENCIAS DE L COMPUTACIÓ UNIVERSIDAD DE MÁLA
DEPSO   R	PSO-vm   SMP	SO			Ċ		
DEPS	O: Exter	nsive Ex	xper	rimental	Frame	ework	Part II
Resul		МАЕВ'09 Г	)10				
						G-CMA-E	S
	and and in Othern			ain anta far D 10		GADEDIS	ST
► R	anked in <b>3th po</b>	DSITION OUT OF A		cipants for D=10		DEPSO	
► S	tatistically simila	ar to G-CMA-E	S and to	o the best one: S	515	DE	
						MOS3	
[GAA09a] J. (	García-Nieto, J. Apollo	ni, and E. Alba. Algor	itmo Basa	do en Cúmulos de		MOS1	
Partículas y	/ en Evolución Difere	ncial para Optimizad	ción Contir	nua, MAEB 2009.		MOS4	
					-	MOS2	
Rosul	ts on BBOB'	na	1.0			DMO	
P Resul		00			AMaLGaM IDEA iAMaLGaM IDEA iPOP-SEP-CMA-ES		
			0.8		EDA-PSD MA-LS-Chain CauchyEDA	BFPS	Λ <i>Ι</i>
► N	oiseless: accu	rate coverage		*/ [	POEMS ALPS-GA	ACOR-SI MALSChain-C	
for s	separate and w	eakly	0.6		PSO-Bounds BayEDAcG		
Struc	ctured					ACOR-SIMF	и FX
			0.4	1.5	G3-PCX NEWUOA (1+1)-GMA-ES	GDGA	
► N	oisy: accurate	coverage for	0.2	it frage	INELDER (Han) GLOBAL DASA.	AEF	
mode	erate and sever	e noise			LSstep LSfminbnd – – – Monte Çarlo	BLXRL	
multi	modal		0.0 10 <sup>0</sup> 10 <sup>1</sup>	$10^2$ $10^3$ $10^4$ $10^5$ $10^6$	BFGS Rosenbrock	CIXL2R	L
						CIXL1R	L
[GAA09c] J. G	arcía-Nieto, E. Alba ar	nd J. Apolloni. <b>Particle</b>	∋ Swarm H	ybridized with Differe	ntial	SBXRL	
Evo	lution: Black-Box Op	timization for Noisy	Functions	s, GECCO 2009.			
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- For certain kinds of complex problems (deceiving), the velocity grows and takes particles out of the variable ranges
- Moreover, for large scale problems (with a huge number of variables) this usually leads PSO to perform an erratic behavior



### Restarting:

- when std approaches zero
  - to avoid particles to fall into local basins of attraction
- when the overall fitness does not improve for
  - a number of steps
  - to control particles dispersion in deceiving landscapes





[GA11] J. García-Nieto, E. Alba. Restart Particle Swarm Optimization with Velocity Modulation: A Scalability Test. Soft Computing (2011)

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1.00E+00

50 100 200

500

1000

**Algorithm Proposals** and Validation

**Real World** Applications **Conclusions &** Future Work



#### DEPSO | RPSO-vm | SMPSO

## Multi-Objective PSO

- **MO Problems** have more than one objective function which are in conflict with each other
  - Pareto dominance
  - The search process does not seek a single solution
  - Set of non-dominated solutions: Pareto optimal set
- In MOPSO, some issues have to be considered:
  - How to select a leader from the set of non-dominated solutions
  - How to keep non-dominated solutions
  - How to maintain diversity



A dominates to B and C  $f_2$ 





[DGNCLA09] J.J. Durillo, J. García-Nieto, A.J. Nebro, C.A. Coello Coello, F. Luna and E. Alba. Multi-Objective Particle Swarm Optimizers: An Exprimental Comparison, EMO 2009

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DEPSO   RPSO-vm   SMPSO								
Comparison of Multi-Objective PSOs								

- ► First, we made a comparison of six representative MOPSOS in the state of the art
- On benchmarks of MO problems: ZDT. DTLZ, and WFG



- Main drawback observed in existing techniques
  - difficulties with multi-modal problems
  - erratic movements in particles' velocity



Number of times out of the 21 evaluated problems in which the best value in each indicator has been obtained Number of times out of the 21 evaluated problems in which the best value in each indicator has been obtained



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Algorithm Proposals and Validation Real World Applications Conclusions & Future Work



Part II

PSO6 | Evolvability | PSO6-Mtsls

## Quest for an Optimal Number of Informants

In Canonical and Standard PSO (2006, 2007, and 2011), the calculation of a new particle's velocity is influenced by just two informant terms: the particle's best previous location, and the best previous location of any of its neighbors

$$\mathbf{v}_i^{t+1} = \chi \left( \mathbf{v}_i^t + U^t[0,\varphi_1] \cdot \left( \mathbf{p}_i^t - \mathbf{x}_i^t \right) + U^t[0,\varphi_2] \cdot \left( \mathbf{b}_i^t - \mathbf{x}_i^t \right) \right)$$

Mendes et al. 2004 proposed the Fully Informed PSO (FIPS): particle's velocity can be adjusted by any number of terms, since important information given by other neighbors may be neglected through overemphasis on the single best neighbor

$$\mathbf{v}_{i}^{t+1} = \chi \left[ \mathbf{v}_{i}^{t} + \sum_{j \in \mathcal{N}_{i}} U^{t} \left[ 0, \varphi_{j} \right] \cdot \left( \mathbf{p}_{j}^{t} - \mathbf{x}_{i}^{t} \right) \right]$$

In FIPS, the neighborhood of informants is arranged in structured topologies



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Motivation: generalize the number of neighbors that inform particles, in order to discover whether there exists a quasi-optimal number of informants for a particular problem

<u>Research question:</u> certain numbers (sets) of informant neighbors may provide new essential information about the search process, hence leading the PSO to perform more accurately than existing versions

[GA11] J. García-Nieto, and E. Alba. Empirical Computation of the Quasi-optimal Number of Informants in Particle Swarm Optimization. GECCO'11



- Providing each k neighborhood with structured topologies is impracticable (enormous number of graphs combinations)
- We simply select k random (uniform) neighbors in the swarm, for each particle i and each time step t (topology independent)

 $\mathcal{N}_i^t = \{n_1, \dots, n_k\} \mid \mathcal{N}_i^t \subset S^t, \forall n_j, n_h \in \mathcal{N}_i^t, n_h \neq n_j \neq i$ 



Part II

#### **PSO6** | Evolvability | PSO6-Mtsls

## Understanding our Quest

- Experimental phase
  - ▶ 30 PSOk versions (*k*=1..30)
  - 25 Benchmark functions (CEC'2005)
  - 25 Independent runs
  - A total number of 18,750 (30x25x50) experiments
- For each problem function: the maximum, median, mean, and minimum error fitness are plotted

For each $k = \{1S\}$ , a different algorithm	
can be developed	

Swarm size	Ss	30
Acceleration coefficient	$\varphi$	4.1
Constriction coefficient	x	0.7298

### PSOk's Performances for f18





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Algorithm Proposals and Validation Real World Applications Conclusions & Future Work



Part II

#### PSO6 | Evolvability | PSO6-Mtsls

## Impact of the Number of Informants

- Observations and implications
  - The interval between 5 and 8 informants concentrates most of successful runs
  - Combining 6 and 8 informants could be a source of new competitive algorithms
  - There are sets of functions that share similar curve shapes.
  - In fact, biased functions to the same optimum share similar curve shapes. Is it because of an unknown feature of CEC'05 functions?
  - Similar curve shapes observed for different benchmarks (CEC'08) and dimensions (30, 50, 100, and 500)





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PSO6   Evo	olvability   PSO6	S-Mtsls						
Perfor	mance (	Comparisor	າຣ		Part II			
The best PSOk (and its combinations) against FIPS-Usquare (the best one in Mendes et al. 2004), FIPS-ALL, and the Standard PSO 2007								
	Algorithm	Best perform functions (CE	ance in Number C'2005) functio	r of Statistical ns (Friedr	Ranking man)			
A.	<b>PSOHE</b> {6,8}	f1, f5, f7, f9 f19, f20, f22,	), f18, 10 f24, f25	2.5	8			
A.	PSO6	f1, f2, f3, f0 f19, f20, f24	3, f7,	2.8	6			
	FIPS-Usquare	f1, f3, f6, f10 f13, f15, f10	), f12,	2.8	8			
A.	§ PSOU[6,8]	f1, f14, f21	, f23 4	3.20	6			
	FIPS-ALL	f11	1	3.7	6			
	Standard 200 <sup>°</sup>	<b>7</b> f8	1	5.6	6			

\*Two new combinations of PSO6 and PSO8: PSOHE{6,8} and PSOU[6,8]



Algorithm Proposals and Validation Real World Applications Conclusions & Future Work



Part II

#### PSO6 | Evolvability | PSO6-Mtsls

## Evolvability: A Step Beyond

Here, we analyze the internal behavior of PSO from the point of view of the evolvability



- Def. Capacity of algorithm's operators to improve the fitness quality for a given problem
- It is also possible to distinguish which algorithm has larger search capabilities, and (to have an idea of) why



Our motivation is to find evidences of why neighborhoods with 6±2 informant particles perform better than other combinations of informants

> [GA12] J. García-Nieto, and E. Alba. Why Six Informants Is Optimal in PSO. ACM GECCO'12

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Part II

PSO6 | Evolvability | PSO6-Mtsls

## Metrics to Measure Evolvability

- Fitness-distance (fitness distance correlation) using PSO informants as neighbors
  - Correlation: both, fitness and distance to optimum decreases

$$r_{fdc} = \frac{c_{fd}}{s_f \cdot s_d}, being \ c_{fd} = \frac{1}{n} \sum_{i=1}^n (f_i - \overline{f}) \cdot (d_i - \overline{d})$$

rfdc: interpretation
+1: convex
0: plateau
-1: deceiving

### Fitness-fitness (fitness cloud)

In our case: plot of fitness of a new particle that is generated from its informants, and the mean fitness of these informants

 $\{(f_1,\overline{f_1}),\ldots,(f_n,\overline{f_n})\}$ 

### Escape probability

Average number of steps required to scape from a local optimum

$$P(\bar{f}_i) = \frac{1}{S_i}$$



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local optimum, e.g., better fitness values





#### PSO6 | Evolvability | PSO6-Mtsls

## Hybrid PSO6 with Multiple Trajectory Search

- A moderate performance is still observed in PSO6 ± 2 for non-separable complex problems
  - Particles move dimension by dimension, which makes hard to find the problem optimum when variables are interdependent
- Incorporation of a local search method to our PSO6 to allow particles to explore their regional neighborhoods in the context of variations of dependent variables



[GA13] J. García-Nieto, and E. Alba. **Hybrid PSO6 for Hard Continuous Optimization**. IEEE Trans. on Sys. Man & Cyb. Part B, (2013). Under review

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PSO6   Evolvability   PSO6-Mtsls									
PSO6-Mtsls: Results									
Results on SOCO'10: Friedman's ranking with Holm's correction									O'10
<b>3</b>									
Our proposal is in the top of best algorithms									tsls
	with statist	ically simila	r distributio	on of results	for			IPSO-Po	well
	all dimensi	ons: 50, 10	0, 200, and	1 500				Sade-MMTS	
		,	, ,					GaDE	
Results	s on an exte	ended ben	chmark <sup>.</sup> c	FC'05+SOC	<b>O'10</b> (40 p	roblem	functions)	SOUPE	
	mparison wit	h other tech	nniques hv	pridized with	h Mtsls	represent	i anotiono)	GODE	
	I	DCOC M						DE-D40-Mm	
features	G-CMA-ES	IPSO-Powell	IPSO-Mtsls	ACOr-Mtsls				RPSO-vr	n
Separable	(6, 1, 0)	(0, 4, 0)	(0, 3, 0)	(0, 4, 0)	50 - 0	EC 105+9		DE	
Non-separabl	(12, 4, 6)	(13, 9, 2)	(9, 12, 3)	(9, 12, 5)		Mtolo	(22/40)	EvoPSOr	ot
Multimoda	$\begin{array}{c c} (1, 2, 1) \\ (17, 3, 5) \end{array}$	(1, 5, 1) (12, 8, 1)	(1, 5, 1) (8, 10, 2)	(1, 5, 1) (8, 11, 4)	F300		(23/40)		
Rotated	(7, 2, 5)	(7, 3, 0)	(7, 3, 0)	(7, 4, 0)	IACO	r-Witsis	(21/40)	F300	
Non rot.	(10, 3, 1)	(6, 10, 2)	(2, 12, 3)	(2, 12, 5)	IPSO-	Mtsls	(18/40)	VXQR1	
SOCO'10	(10, 3, 1)	(5, 10, 2)	(1, 12, 3)	(1, 12, 2)	IPSO-	Powell	(14/40)	MA-SSV	
Total	(8, 2, 5) (18, 5, 6)	(3, 3, 0) (13, 13, 2)	(3, 3, 1) (9, 15, 3)	(8, 4, 3) (9, 16, 5)	G-CM	A-ES	(11/40)	G-CMA-E	ES
	<b>PSO6-Mtsls</b> r	number of (w	/in, draw. lo	se)				СНС	
		- (	,,	,				*Control M	IOS-DE



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DNA Microarrays allow scientists to simultaneously analyze thousands of genes, thus providing important insights about cells' functions



- Involving a vast amount of data
- Machine learning techniques can help us to discover subsets with high predictive power: *classification*
- complex and costly (computationally speaking)
- An intelligent reduction pre-process is required: feature selection

**Objective:** to discover small subsets of genes able to predict the class of an external (independent) gene sample as much as possible



- Our proposal, PMSO: island model Geometric PSO for binary optimization
- SPMBCX particle's movement operator in GPSO is specially well adapted to feature selection (*García-Nieto et al. CEC'07*)



- Classification & validation: SVM with 10-fold cross-validation
- Final validation with external test set

[GA12] J. García-Nieto, and E. Alba. **Parallel Multi-Swarm Optimizer for Gene Selection in DNA Microarray**. Applied Intelligence (2012)



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Vehicular Ad Hoc Networks (VANETs) are composed of a set of communicating vehicles (nodes) equipped with devices which are able to spontaneously interconnect to each other without any pre-existing infrastructure

### VANETs implications:

- no service provider
- limited coverage
- high dynamism
- non structured topology
- VANETs applications:
  - safety
  - traffic management
  - defense
  - transportation

**Objective:** to find optimized sets of parameters to fine-tune communication protocols in VANETs



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**PSO**: shows the best configuration in terms of **effective data rate** 

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QoS results: effective data rate (the better the larger)





- Nowadays, the intense vehicular traffic in current cities provokes severe problems related to: pollution, congestion, security, noise, and many others
- Signal lights (SL) are configurable devices that partially control the flow of vehicles. However, the increasing number of SL's require a highly complex scheduling

<u>Objective:</u> to find optimized timing programs (TPs) for all the SLs in a given area.



Our proposal: PSO-SL coupled with SUMO, to automatically search quasi-optimal solutions





 Solution encoding: vector of integers where each element represents a phase duration of one state of SLs in intersections (SUMO structure of TPs)



 Optimization strategy: optimization algorithm (PSO) with offline simulation procedure (SUMO)



 Two realistic instances located at Málaga (Spain) and Bahía-Blanca (Argentina) from real digital maps

[GOA12] J. García-Nieto, E. Alba and C. Olivera. **Swarm intelligence for traffic light scheduling: Application to real urban areas**. Eng. Apps of Art.Intel. (2012)





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Conclusions	Future Work				
Genera	al Conc	lusions			Part IV

- Methodology
  - Velocity modulation avoids particles to move out of the search problem ranges. This is a good starting PSO for multimodal problems
  - A number of  $6 \pm 2$  informant particles in the neighborhood makes the PSO to perform better than other combinations (like 2, as in the Standard PSO)
  - Hybridizing with advanced LS methods and DE operators mitigates the deficiencies observed in PSO when tackling non-separable problems

DEPSO	<ul> <li>Successful results on CEC'05 and BBOB'09</li> </ul>
RPSO-vm	<ul> <li>Scalability analysis in the scope of SOCO'10</li> </ul>
SMPSO	<ul> <li>Well adapted to multimodal problems: ZDT, DTLZ, WFG</li> </ul>
PSO6	Thorough analysis of the number of informants: CEC'05
PSO6-MtsIs	Located in the top of S.O.A. on continuous optimization: CEC'05+SOCO'10

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Conclusions	Future Work					
Gener	al Conc	lusions				Part IV

Algorithmic proposals

Mechanism	Description	Proposals
Hybridization	Using differential evolution operators and advanced local search methods	DEPSO PSO6-MtsIs
Standard Improvement	Outperforming S.O.A. proposals	RPSO-vm PSO6
Multi-objective	Accurate computation of the optimal Pareto Front	SMPSO
Parallelism	Running sub-swarms in parallel	8 Swarm-PMSO



- Real world applications
  - PSO is an excellent general purpose optimizer showing a successful performance for the three real world problems tackled here
    - Most frequently selected genes by PMSO also suggested by the reference literature: Nature & Science
    - Reported VANET protocol configurations improve over human experts
    - Resulting timing programs alleviate traffic congestion in realistic scenarios

PMSO	<ul> <li>Parallel multi-swarm Geometric PSO</li> <li>8 Island-swarm performs the best in terms of accuracy &amp; speedup</li> </ul>
PSO-SL	<ul> <li>Adaptation to integer encoding</li> <li>Outperforms Standard 2011 and DE</li> </ul>



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- Adaptive sets of informant neighbors (in run time)
  - Finding the best trade-off for exploitationexploration
- Facing dynamic problems
  - Signal light timing programs on dynamic traffic environments
- Reducing vehicle emissions and fuel consumption
  - Optimized timing programs for green smart cities
- Deploying Swarms in Smart Devices
  - Design and development of particles running on smart terminals: phones, tables, vehicle's comp., drones, etc.; to deploy physical swarms









### Thank you so much!!!



## **Comments & Questions**

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